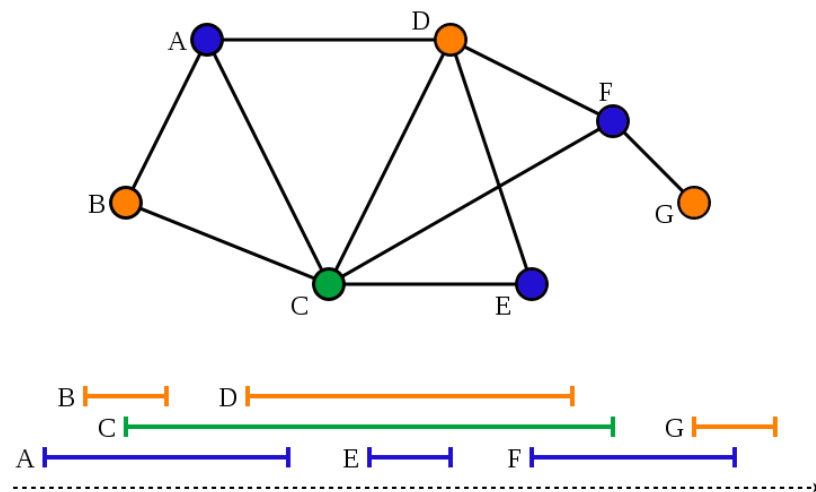


# MODEL CHECKING PARALLEL FIRST FIT GRAPH COLORING IN JAVA

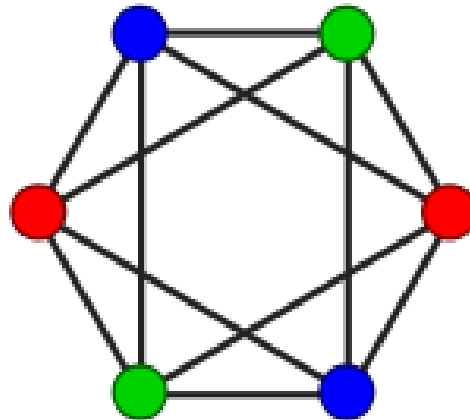
CSE 6490A Winter 2011

Loutfouz Zaman



# Vertex coloring

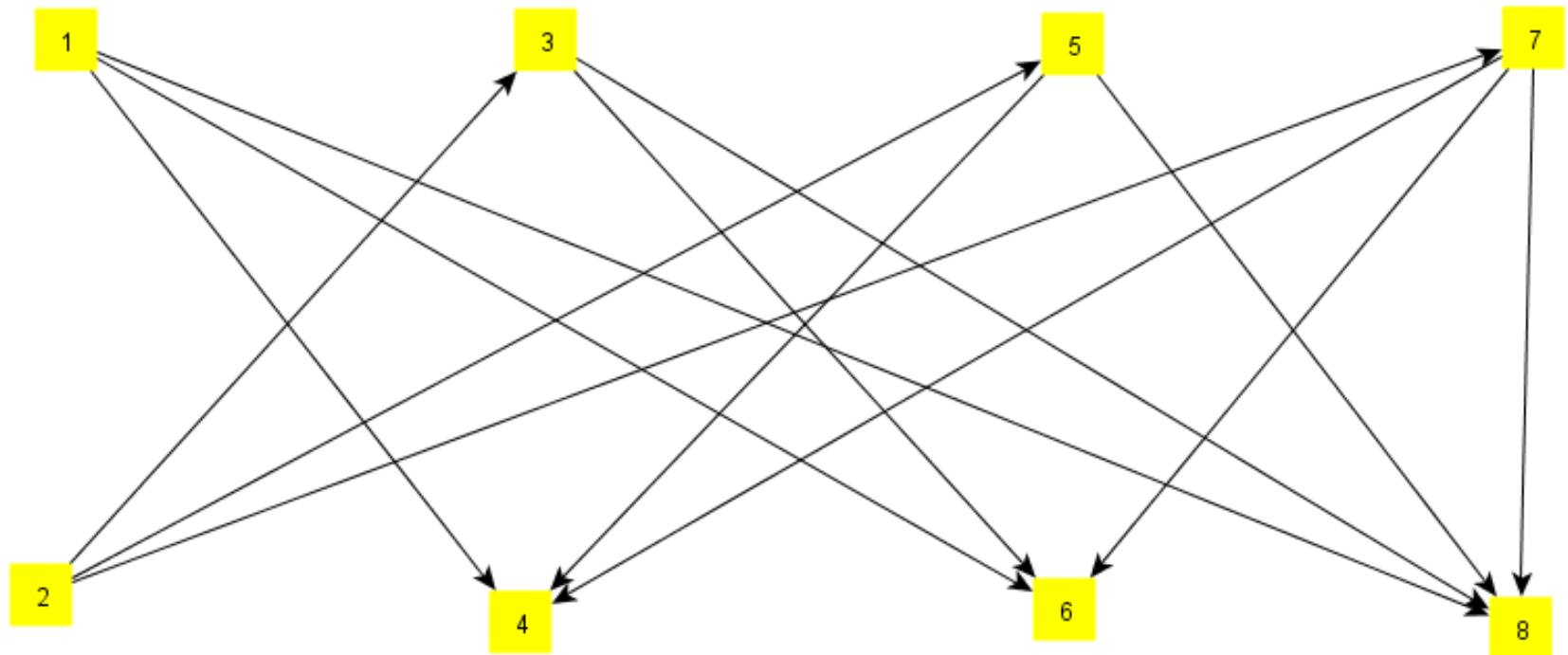
- Assignment of "colors" to vertices in a way so that no two adjacent vertices share the same color
- First-Fit is the simplest algorithm
  - works by assigning the smallest possible integer as color to the current vertex of the graph



# Sequential FF

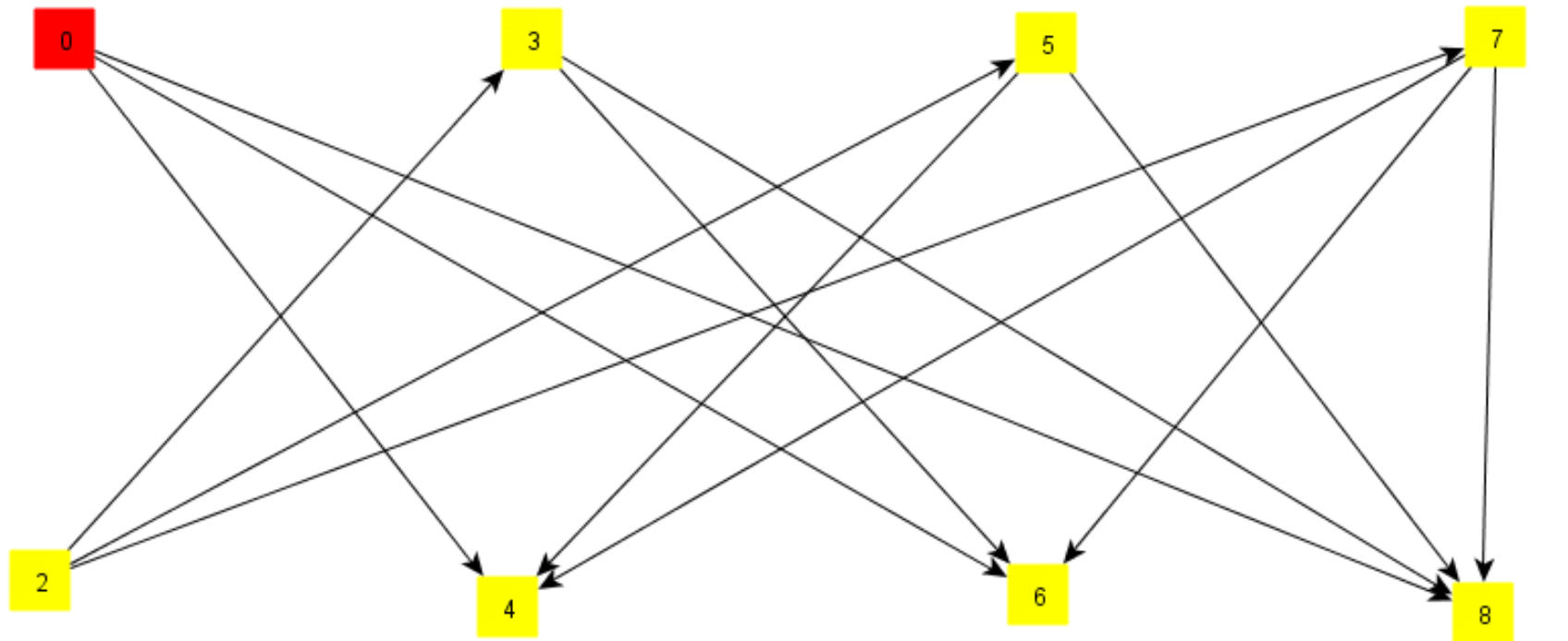
- Umland (1998) demonstrates a 2-step sequential FF algorithm:
  - **(1) *Build*( $L_i, v_j$ ):** Determine a list  $L_i$  of all possible colors for  $v_i$ , i.e. exclude colors already used by vertices  $v_j, j < i$  adjacent to  $v_i$ 
    - $L_i$  -- a boolean array (possibility list of  $v_i$ ) with property:
      - $L_i[k] = false \leftrightarrow \exists v_j$  such that  $j < i, (v_i, v_j) \in E$  and  $f(v_j) = k$
  - **(2) *Color*( $L_i, v_i$ ):** Determine the smallest of all possible colors for  $v_i$ , i.e. look for the smallest entry in  $L_i$  where  $L_i[k] = true$  and assign color  $k$  to  $v_i$

# Sequential FF E.g. Step 0



# Sequential FF E.g. Step 1

$$L_1 = \{t, t, t, t\}, k=0$$



$$L_4 = \{f, t, t, t\}$$

$$L_6 = \{f, t, t, t\}$$

$$L_8 = \{f, t, t, t\}$$

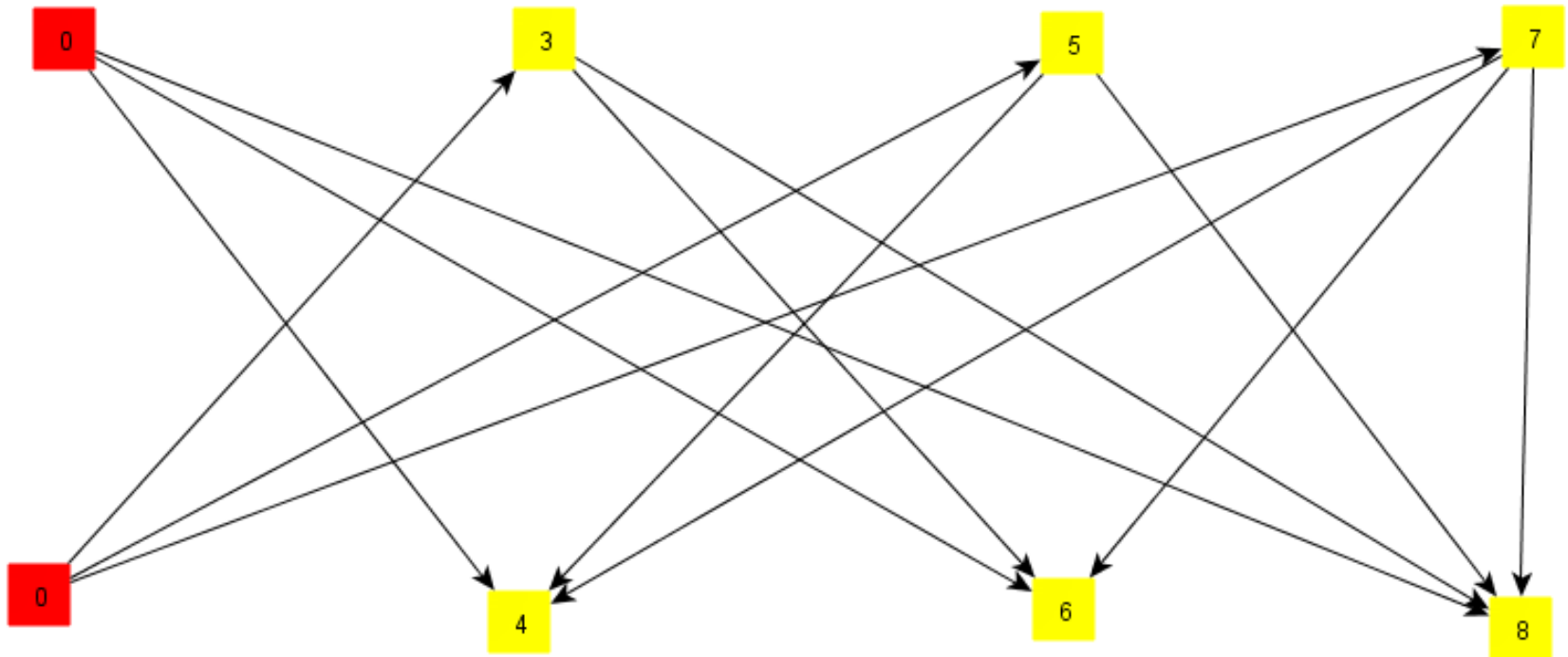
# Sequential FF E.g. Step 2

$L_1 = \{t, t, t, t\}, k=0$

$L_3 = \{f, t, t, t\}$

$L_5 = \{f, t, t, t\}$

$L_7 = \{f, t, t, t\}$



$L_2 = \{t, t, t, t\}, k=0$

$L_4 = \{f, t, t, t\}$

$L_6 = \{f, t, t, t\}$

$L_6 = \{f, t, t, t\}$

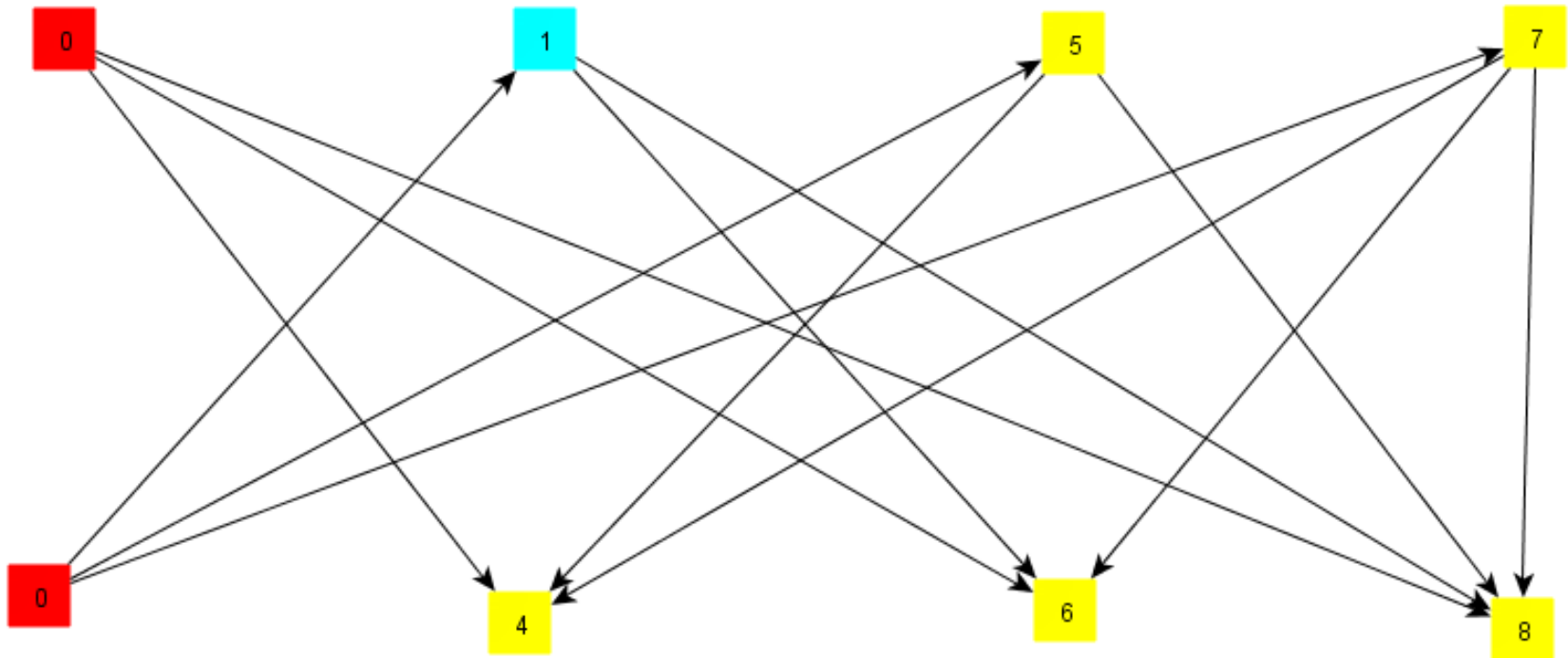
# Sequential FF E.g. Step 3

$L_1 = \{t, t, t, t\}, k=0$

$L_3 = \{f, t, t, t\}, k = 1$

$L_5 = \{f, t, t, t\}$

$L_7 = \{f, t, t, t\}$



$L_2 = \{t, t, t, t\}, k=0$

$L_4 = \{f, t, t, t\}$

$L_6 = \{f, f, t, t\}$

$L_6 = \{f, f, t, t\}$

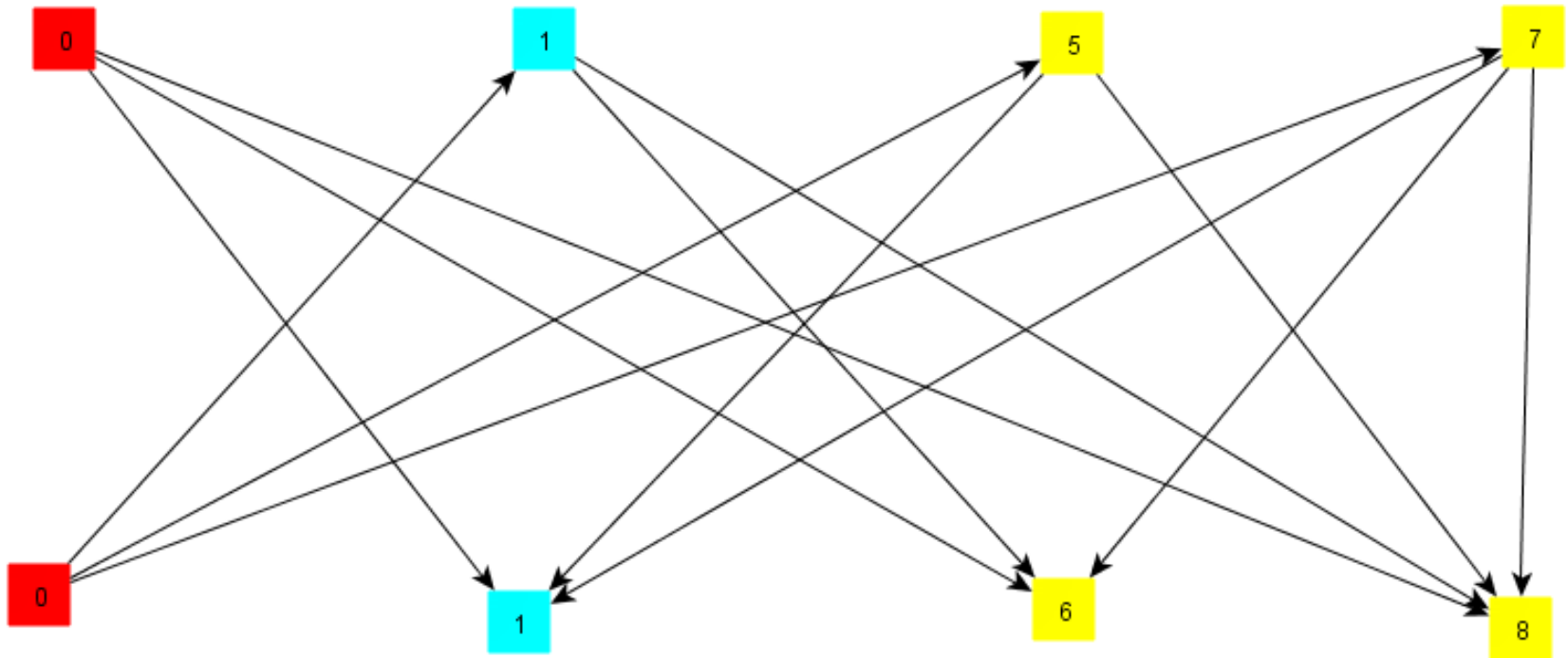
# Sequential FF E.g. Step 4

$L_1 = \{t, t, t, t\}, k=0$

$L_3 = \{f, t, t, t\}, k=1$

$L_5 = \{f, f, t, t\}$

$L_7 = \{f, f, t, t\}$



$L_2 = \{t, t, t, t\}, k=0$

$L_4 = \{f, t, t, t\}, k=1$

$L_6 = \{f, f, t, t\}$

$L_6 = \{f, f, t, t\}$



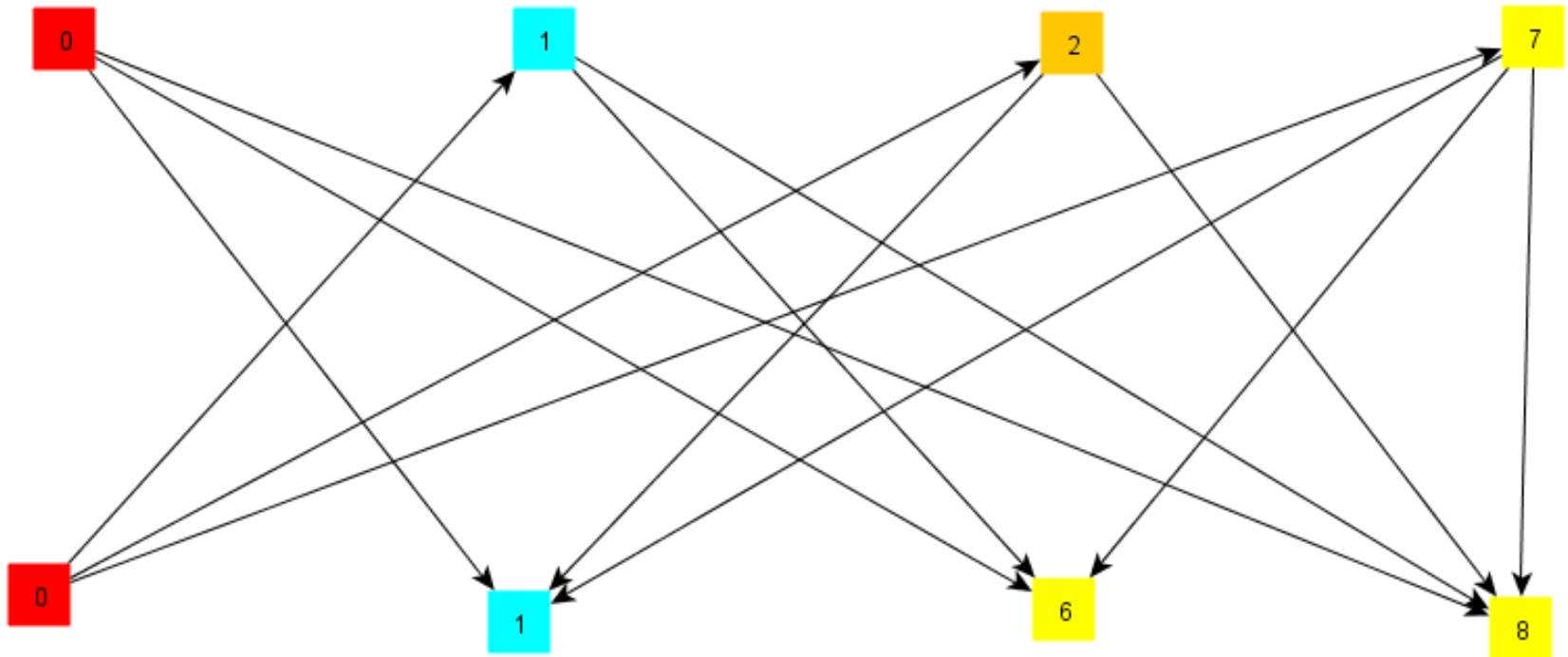
# Sequential FF E.g. Step 5

$L_1 = \{t, t, t, t\}, k=0$

$L_3 = \{f, t, t, t\}, k=1$

$L_5 = \{f, f, t, t\}, k=2$

$L_7 = \{f, f, t, t\}$



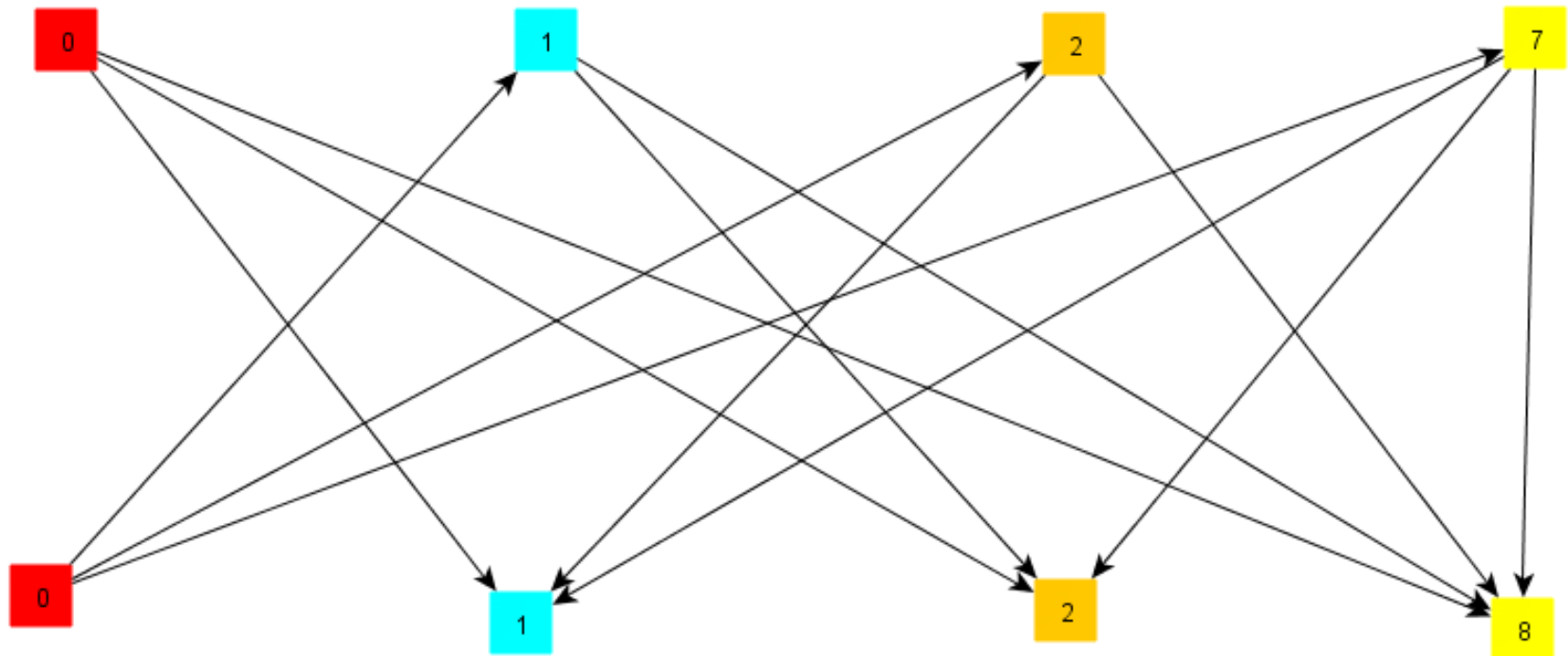
$L_2 = \{t, t, t, t\}, k=0$

$L_4 = \{f, t, t, t\}, k=1$

$L_6 = \{f, f, t, t\}$

$L_6 = \{f, f, f, t\}$

# Sequential FF E.g. Step 6

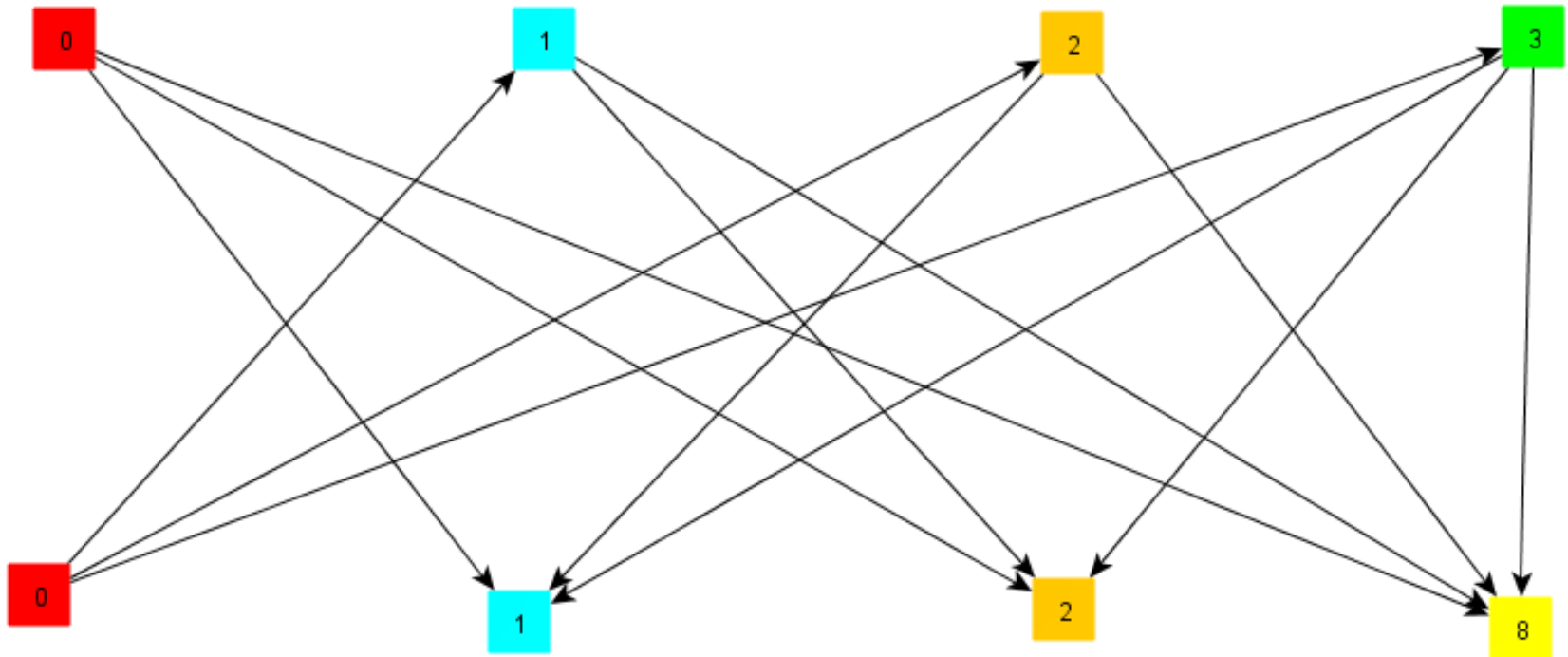
 $L_1 = \{t, t, t, t\}, k=0$ 
 $L_3 = \{f, t, t, t\}, k=1$ 
 $L_5 = \{f, f, t, t\}, k=2$ 
 $L_7 = \{f, f, f, t\}$ 

 $L_2 = \{t, t, t, t\}, k=0$ 
 $L_4 = \{f, t, t, t\}, k=1$ 
 $L_6 = \{f, f, t, t\}, k=2$ 
 $L_6 = \{f, f, f, t\}$

# Sequential FF E.g. Step 7

$L_1 = \{t, t, t, t\}, k=0$

$L_3 = \{f, t, t, t\}, k=1$

$L_5 = \{f, f, t, t\}, k=2$     $L_7 = \{f, f, f, t\}, k=3$



$L_2 = \{t, t, t, t\}, k=0$

$L_4 = \{f, t, t, t\}, k=1$

$L_6 = \{f, f, t, t\}, k=2$

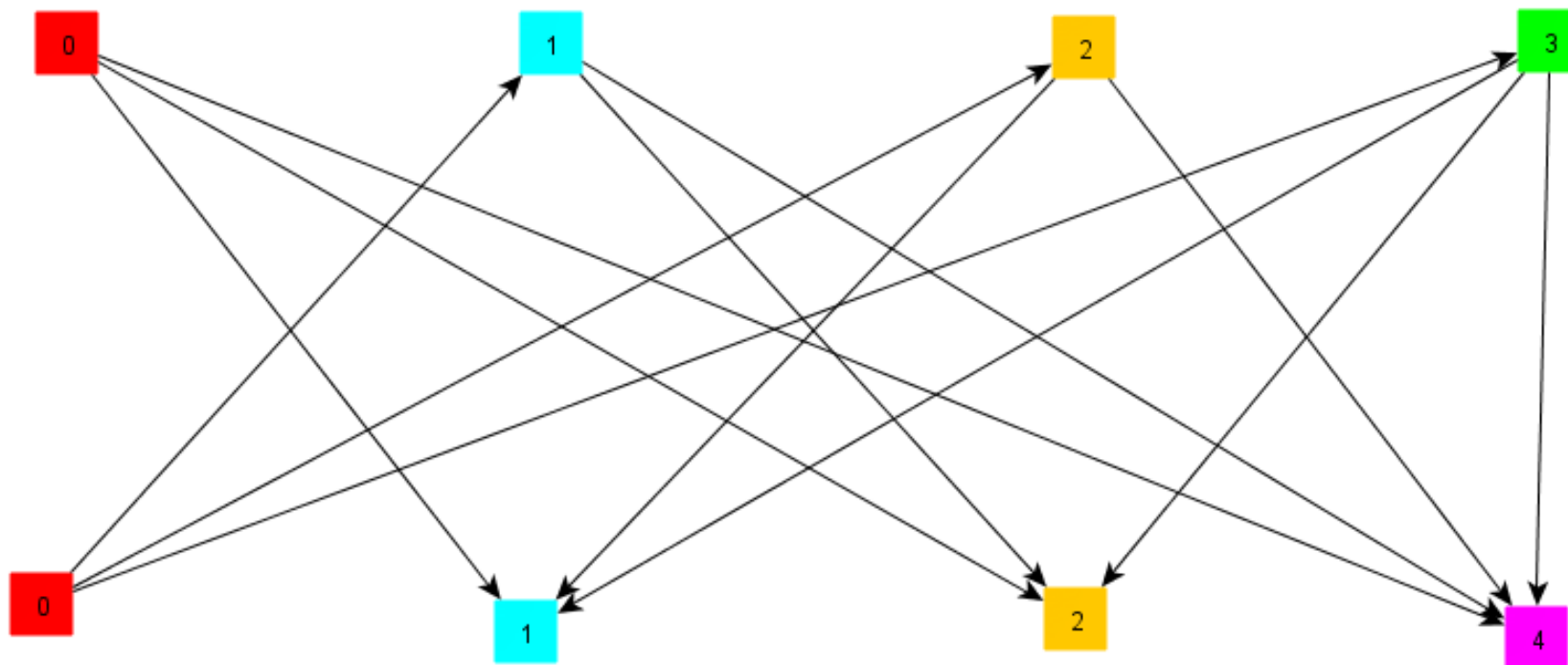
$L_6 = \{f, f, f, f\}$

# Sequential FF E.g. Step 8

$L_1 = \{t, t, t, t\}, k=0$

$L_3 = \{f, t, t, t\}, k=1$

$L_5 = \{f, f, t, t\}, k=2$      $L_7 = \{f, f, f, t\}, k=3$



$L_2 = \{t, t, t, t\}, k=0$

$L_4 = \{f, t, t, t\}, k=1$

$L_6 = \{f, f, t, t\}, k=2$

$L_6 = \{f, f, f, f\}, k=4$

# Parallel FF (Subgraph Based)

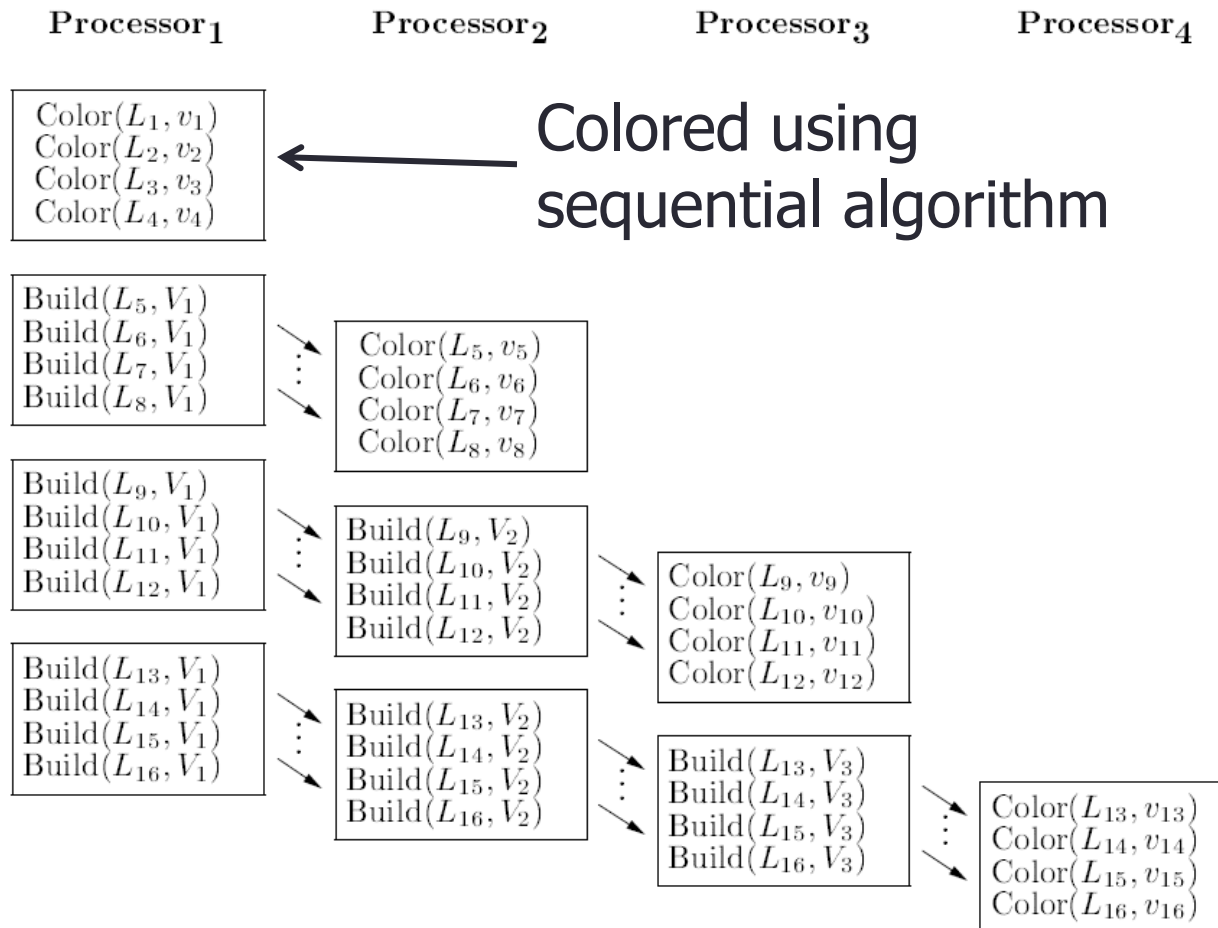
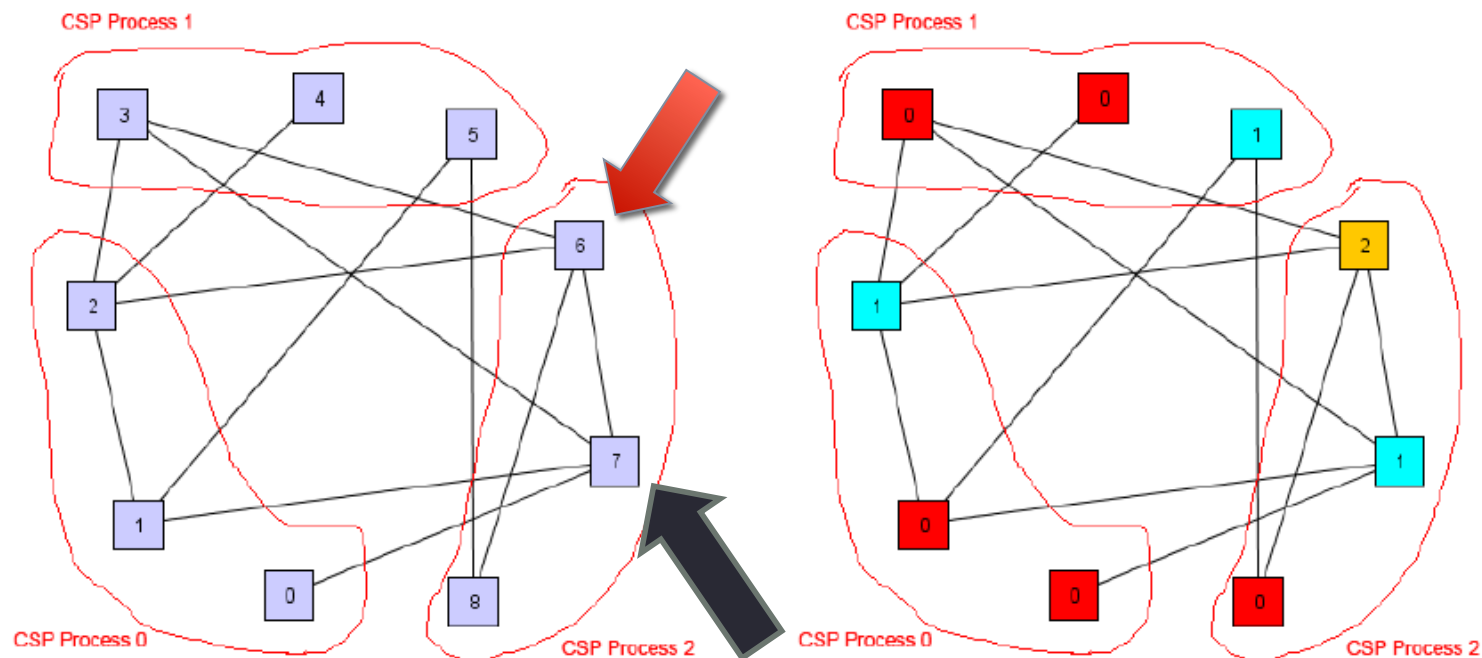


Figure 3: Generalized parallel first fit (16 vertices, 4 processors).

# Bug in the Implementation

- JPF found `java.lang.NullPointerException`
- Previously believed to be fixed



(a) Minimal graph producing the bug .

(b) The produced proper coloring.

- Before:
  - Color = Get color from a hashtable
  - Build color for  $v_i$
- After fixing:
  - Color = -1
  - While (Color == -1)
    - Color = Get color from a hashtable
    - Build color for  $v_i$

# Other Data Races

- Using **gov.nasa.jpf.listener.PreciseRaceDetector**
- Were not detected
  - Testing with JPF allowed removal of synchronized blocks which were introduced to address the bug mentioned earlier
  - Still not sure if the removal is safe, however, JPF did not detect any issues



# Correctness Test Re-visited

- Using JPF to verify proper coloring
  - for each node  $n$  in  $G$
  - for each *neighbour* of  $n$
  - assert  $\text{color}(n) \neq \text{color}(\text{neighbour})$
- No assertion violations were detected
- Can't use too large graphs
  - 2000 nodes, 999001 edges => **java.lang.StackOverflowError**

- **9 nodes 12 edges, 4 processes**

- ===== statistics
- elapsed time: 0:00:03
- states: new=1442, visited=3, backtracked=10, end=8
- search: maxDepth=1434, constraints=0
- choice generators: thread=1435, data=0
- heap: gc=1334, new=1221, free=349
- instructions: 38592
- max memory: 91MB
- loaded code: classes=161, methods=2384

- =====
- **20 nodes 190 edges, 20 processes**

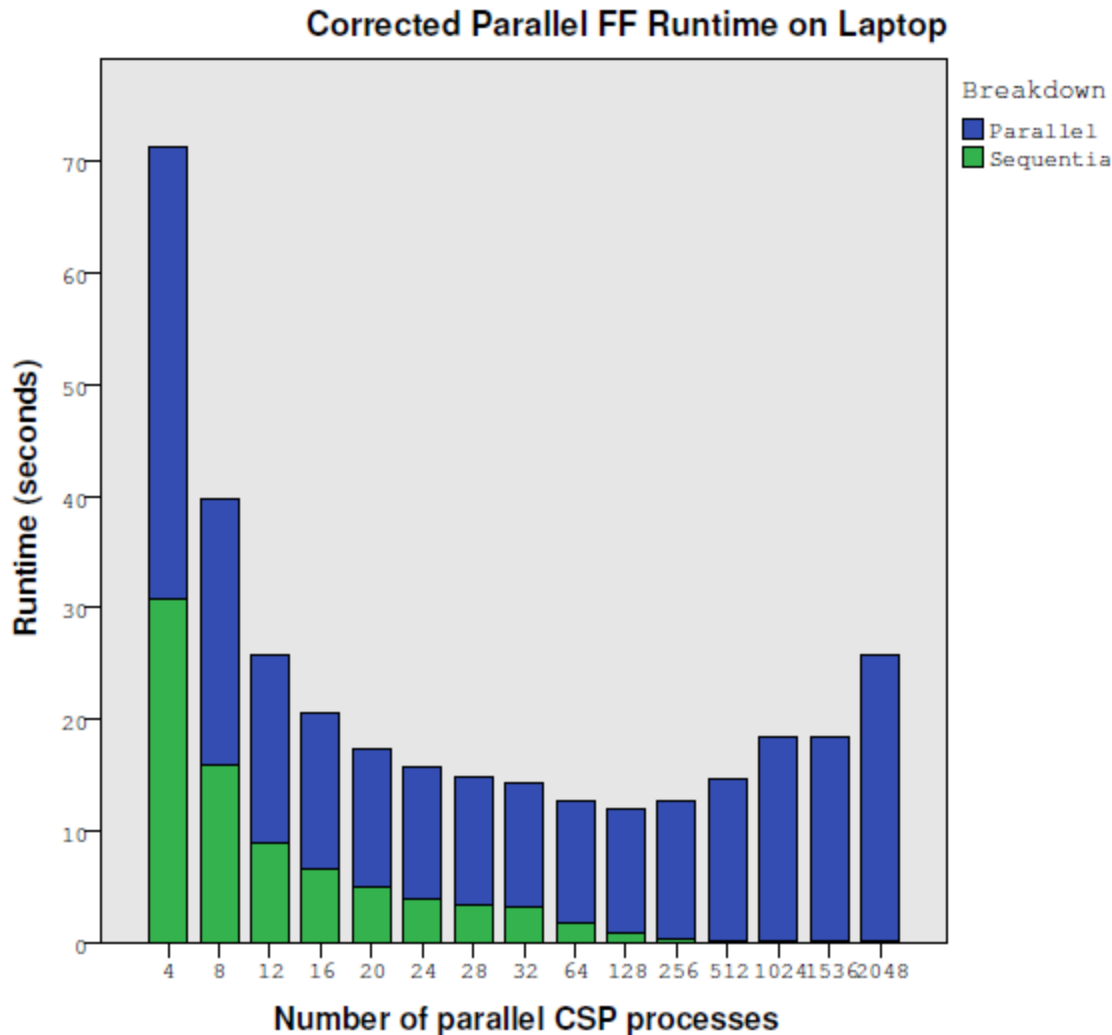
- ===== statistics
- elapsed time: 0:00:47
- states: new=24802, visited=0, backtracked=7, end=8
- search: maxDepth=24794, constraints=0
- choice generators: thread=24795, data=0
- heap: gc=24247, new=2623, free=1191
- instructions: 327855
- max memory: 453MB
- loaded code: classes=161, methods=2406

- **40 nodes 400 edges, 20 processes**

- ===== statistics
- elapsed time: 0:04:23
- states: new=98266, visited=30, backtracked=37, end=8
- search: maxDepth=98258, constraints=0
- choice generators: thread=98259, data=0
- heap: gc=95888, new=4313, free=2347
- instructions: 960172
- max memory: 1361MB
- loaded code: classes=162, methods=2408

- =====

# Performance Test Re-visited



4 trials

Same input as before

New overhead of **while** loop

Removed overhead of synched blocks

Output slightly improved overall, but it could be due to chance as well

# Bug in JCSP

- Found **gov.nasa.jpff.jvm.NotDeadlockedProperty**
- ===== snapshot #1
- thread  
index=1,name=ParallelFirstFit\$FFGeneralProcess@a998,status=WAITING,this=org.jcsp.lang.ParThread@667,waiting on: java.lang.Object@679
- call stack:
  - at org.jcsp.lang.Barrier.sync(Barrier.java:33)
  - at org.jcsp.lang.ParThread.run(ParThread.java:41)
  - ...
- The same bug was observed for a simple single One2One Channel, 2-thread reader and writer JCSP application

# Conclusion & Open Questions

- Conclusion
  - JPF can be useful for finding issues in CSP
    - But misleading when detecting deadlocks due to a bug
- Is it reasonable to keep increasing the size of input and number of processes for this kind of algorithm?
  - The bug was caught using only a 9 node and 12 edges graph among 4 processes
  - Limits on how large the input can get, particularly the edges
- Will different search strategies help?
  - Currently only the default strategy was tried