Parallel Algorithm --Minimum Spanning Tree

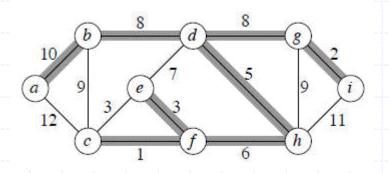
- Wrote by R. Setia, A.Nedunchezhian,
 S. Balachandaran, in HiPC 2009
- Presented by Xiwen Chen.

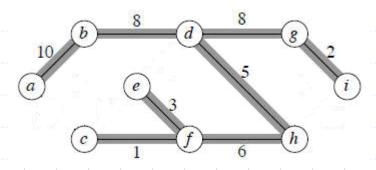
Outline

- Brief introduction.
- Sequential algorithm.
- Concurrent Prim's algorithm.
- Some related problem.

Introduction

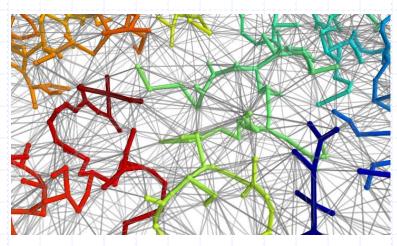
 Minimum Spanning Tree(MST) is one of the well known classical graph problems.





Applications

 Minimum Spanning Tree has many applications in VSLI layout and routing, wireless communication and various other fields.



Sequential Algorithms

 The first serial algorithm for MST was given by a Czech scientist Borůvka, 1926.



Borůvka(1899-1995)



Prim(1921-now)

Other two commonly used Greedy algorithms are Kruskal's algorithm (1956) and Prim's algorithm(1957).



Kruskal(1928-2010)

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Prim's Algorithm

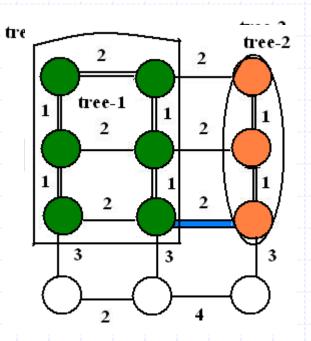
- Initialize: $V_{mst} = \{x\}, x$ is an arbitrary node from V, $E_{mst} = \{\emptyset\}$.
- Repeat until $V_{mst} = = V$
 - Choose an edge (u,v) with u is minimal weight such that u is in V_{mst} and v is not.
 - Add v to V_{mst} and (u,v) to the E_{mst} .

Concurrent Prim's Algorithm

- Key ideas:
 - Each thread grows their single trees in parallel.
 - When collision occurs between two threads i and j(i<j), thread j merges with i. i keeps growing and j chooses another node to grow a new tree.

Concurrent Prim's Algorithm

- It remains the same for growing a single tree in an individual thread.
- For the merge part, we call the MergeTree(i,j) method to do that.



Concurrent Prim's Algorithm

 Lemma 1.1 No cycles are formed during MergeTree operation.

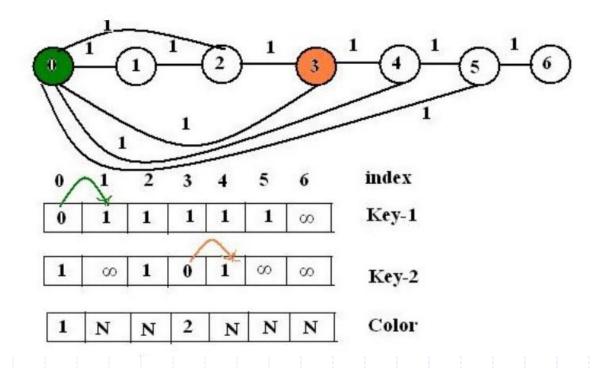
 Lemma 1.2 The edges added by the this this algorithm belong to MST.

Load Balancing scheme

- Base Problem Size
 - A threshold value for the number of uncolored nodes. If # of nodes below that threshold, we terminate the thread j instead of let it pick a new random node to grow a new tree.
 - The writer has an empirically value equal to $\frac{|V|}{p}$, if there are p threads created.

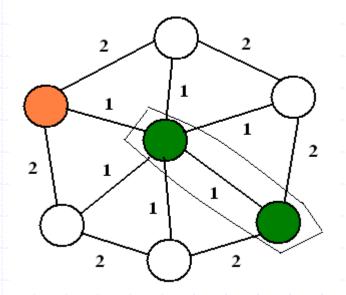
Heuristics

Warp-around find-min



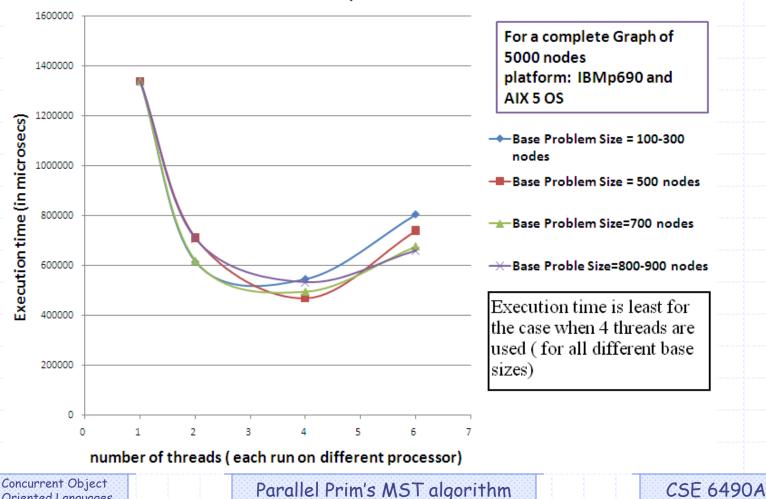
Heuristics

- Threshold nodes
 - Kill the underperformed thread



Experiments and results

Execution time vs number of processors for a given Graph and different base problem sizes



Oriented Languages