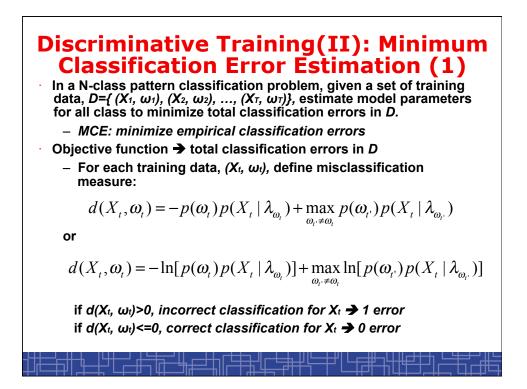


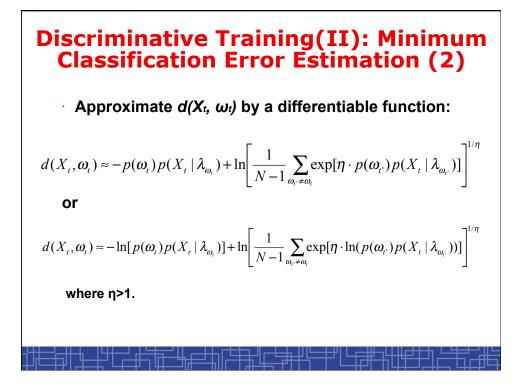
Discriminative Training(I): Maximum Mutual Information Estimation (2) • Difficulty: joint distribution $p(\omega, X)$ is unknown. • Solution: collect a representative training set $(X_1, \omega_1), (X_2, \omega_2), ..., (X_7, \omega_7)$ to approximate the joint distribution. $\{\lambda_1 \cdots \lambda_N\}_{MMI} = \underset{\lambda_1 \cdots \lambda_N}{\operatorname{arg\,max}} I(\omega, X)$ $= \underset{\lambda_1 \cdots \lambda_N}{\operatorname{arg\,max}} \sum_{\omega} \sum_{X} p(\omega, X) \log_2 \frac{p(X \mid \lambda_{\omega})}{\sum p(X \mid \lambda_{\omega})}$

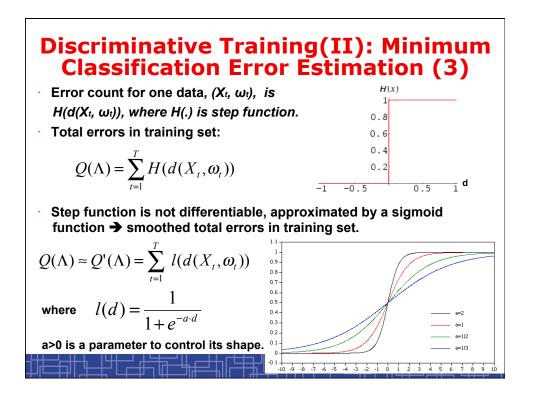
$$\approx \underset{\lambda_{1}\cdots\lambda_{N}}{\operatorname{arg\,max}} \sum_{t=1}^{T} \log_{2} \frac{p(X_{t} \mid \lambda_{\omega_{t}})}{\sum_{\omega} p(X_{t} \mid \lambda_{\omega_{t}})}$$

• Optimization:

- Iterative gradient-ascent method
- Growth-transformation method







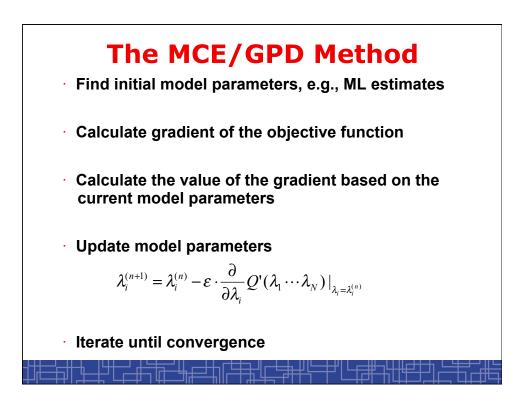
Discriminative Training(II): Minimum Classification Error Estimation (3)

• MCE estimation of model parameters for all classes:

$$\{\lambda_1 \cdots \lambda_N\}_{MCE} = \underset{\lambda_1 \cdots \lambda_N}{\operatorname{arg min}} Q'(\lambda_1 \cdots \lambda_N)$$

- Optimization: no simple solution is available
 - Iterative gradient descent method.
 - GPD (generalized probabilistic descent) method.

$$\lambda_i^{(n+1)} = \lambda_i^{(n)} - \varepsilon \cdot \frac{\partial}{\partial \lambda_i} Q'(\lambda_1 \cdots \lambda_N) \big|_{\lambda_i = \lambda_i^{(n)}}$$

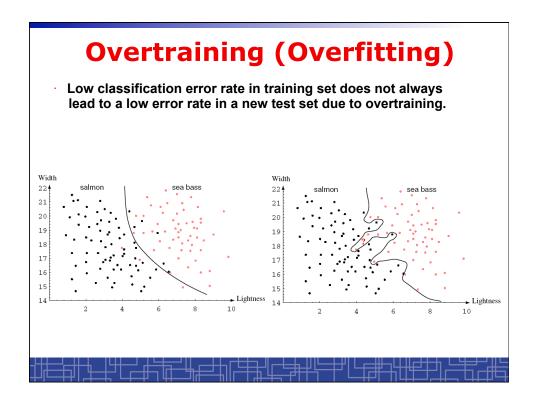


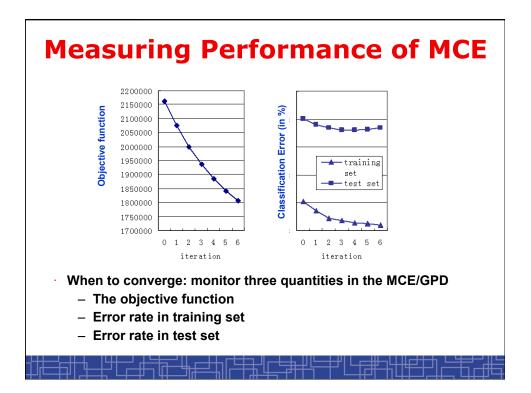
How to calculate gradient?

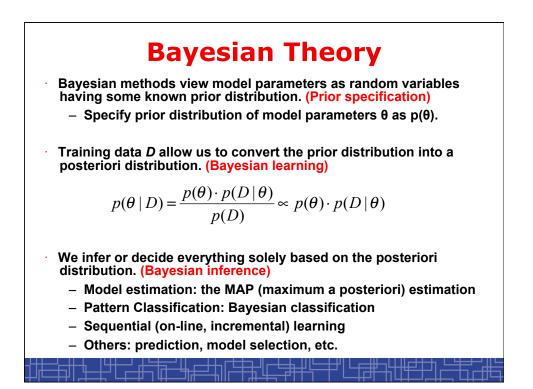
$$\frac{\partial}{\partial \lambda_i} Q'(\lambda_1 \cdots \lambda_N) = \sum_{t=1}^T \frac{\partial}{\partial \lambda_i} l[d(X_t, \omega_t)]$$

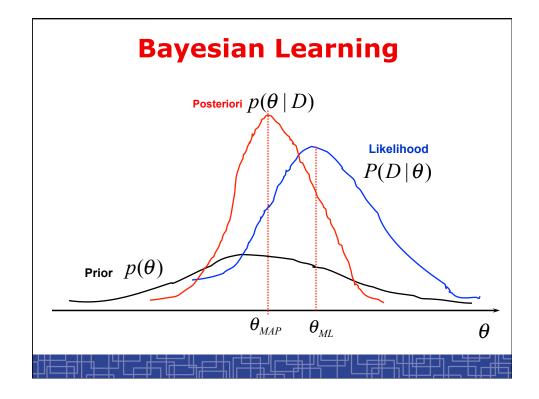
$$= \sum_{t=1}^T \frac{\partial l(d)}{\partial d} \cdot \frac{\partial d(X_t, \omega_t)}{\partial \lambda_i}$$

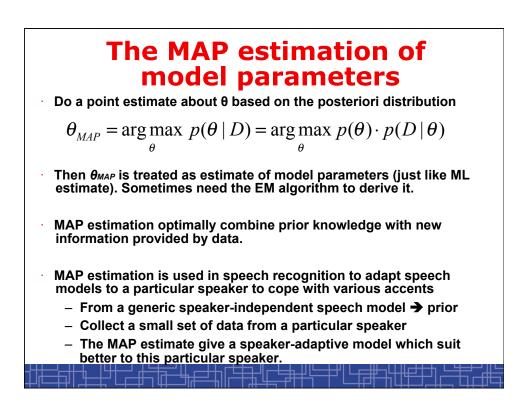
$$= \sum_{t=1}^T a \cdot l(d) \cdot [1 - l(d)] \cdot \frac{\partial d(X_t, \omega_t)}{\partial \lambda_i}$$
• The key issue in MCE/GPD is how to set a proper step size experimentally.



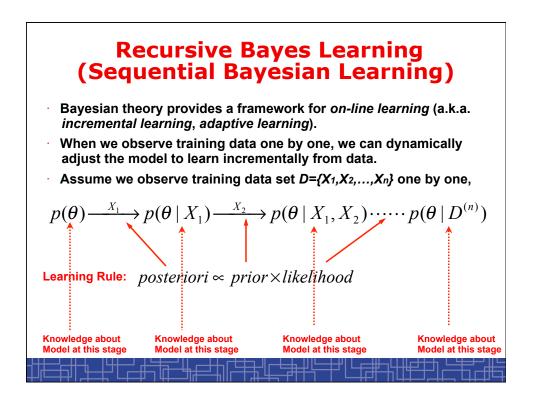


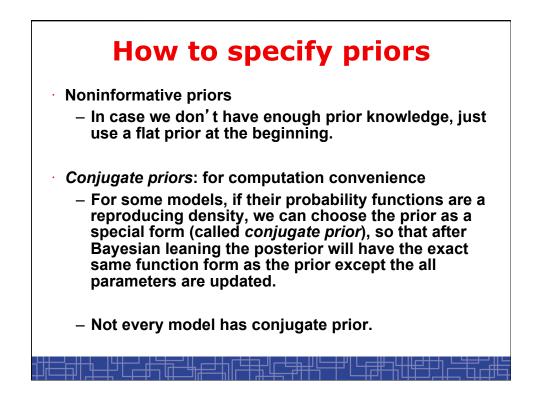




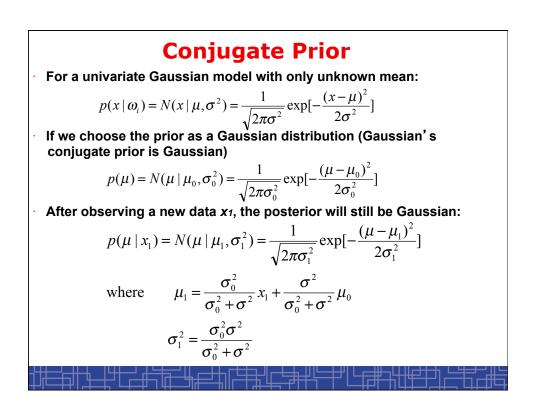


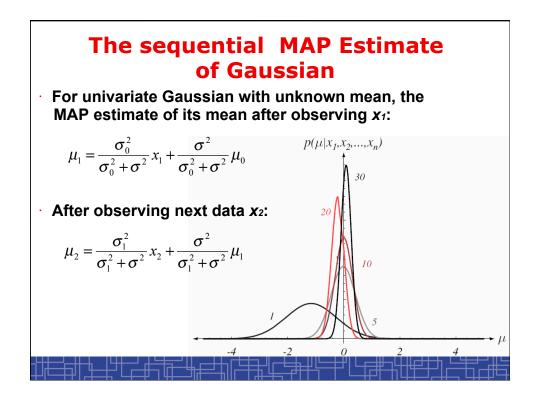
Bayesian Classification
• Assume we have *N* classes,
$$\omega_i$$
 (*i*=1,2,...,*N*), each class has a class-
conditional pdf $p(X|\omega_i,\theta_i)$ with parameters θ_i .
• The prior knowledge about θ_i is included in a prior $p(\theta_i)$.
• For each class ω_i , we have a training data set D_i .
• Problem: classify an unknown data Y into one of the classes.
• The Bayesian classification is done as:
 $\omega_Y = \arg \max_i p(Y | D_i) = \arg \max_i \int p(Y | \omega_i, \theta_i) \cdot p(\theta_i | D_i) d\theta_i$
where
 $p(\theta_i | D_i) = \frac{p(\theta_i) \cdot p(D_i | \omega_i, \theta_i)}{p(D_i)} \propto p(\theta_i) \cdot p(D_i | \omega_i, \theta_i)$

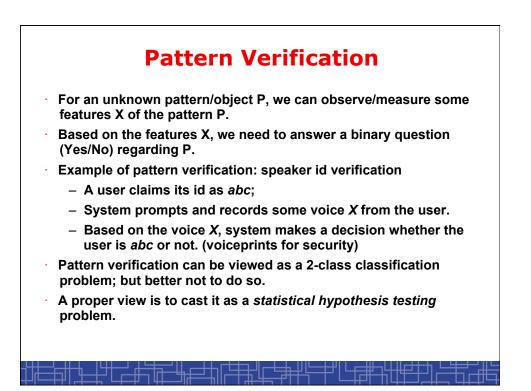


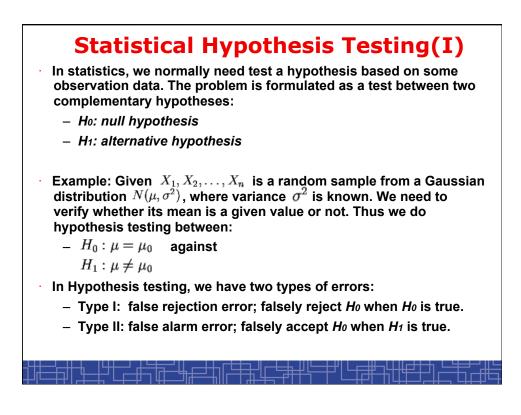


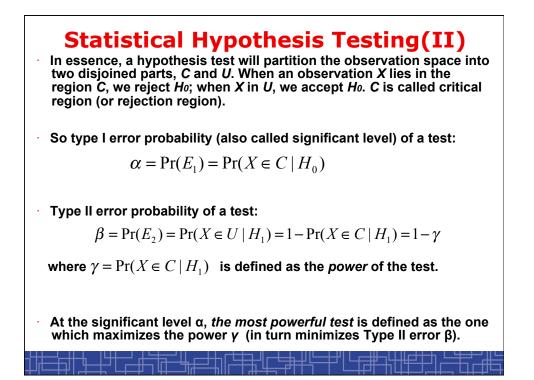
Prepared by Prof. Hui Jiang (CSE6328)

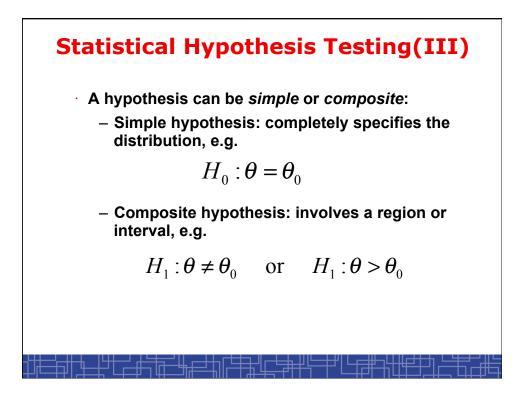


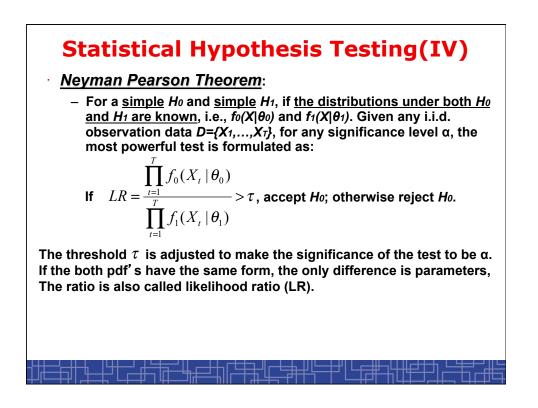


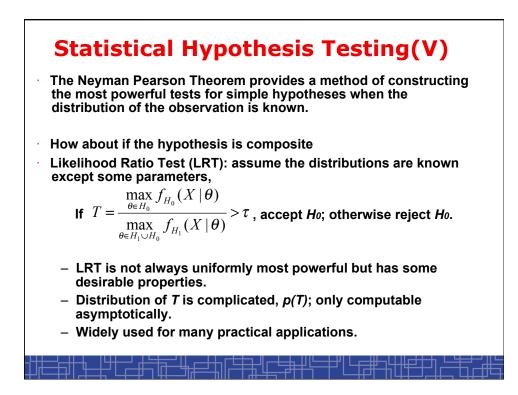


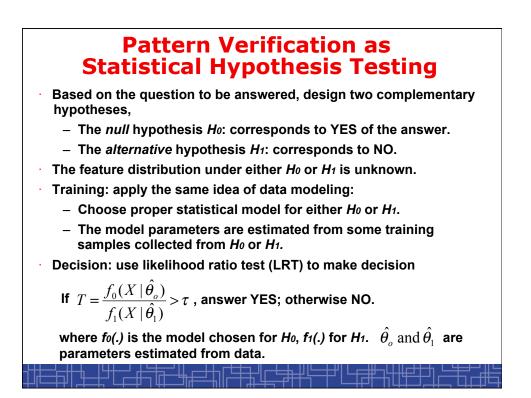


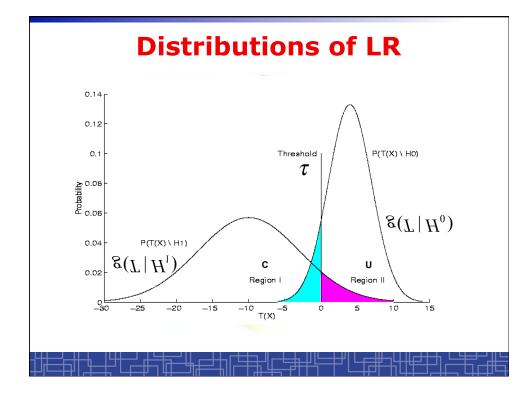


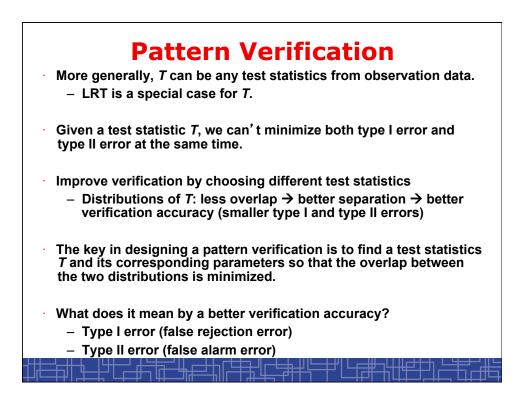


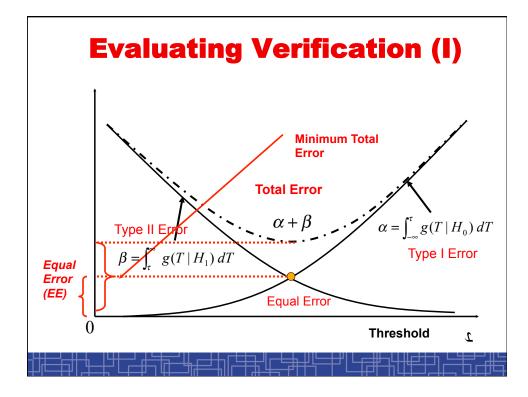


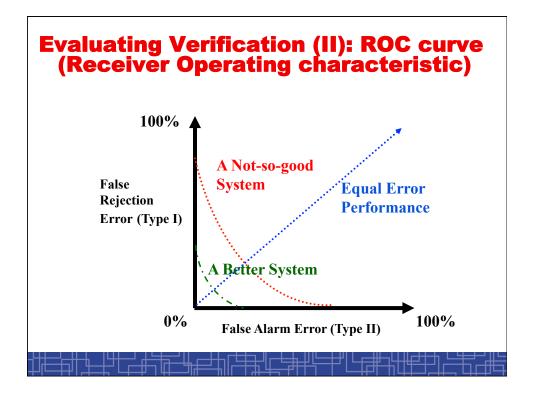


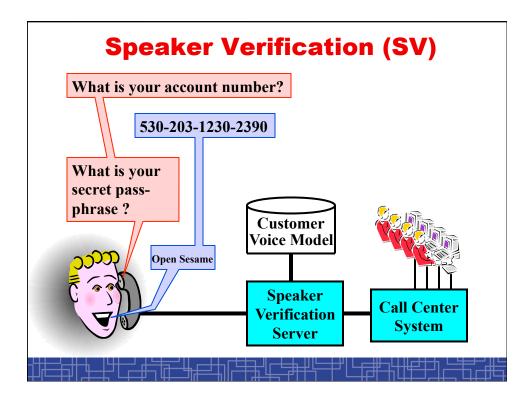












Example(I): Speaker Verification(1)

- Speaker verification: verify user ID based on the voice. The user first claims a user ID, the system records some voice sample from the user and try to answer YES/NO to the question "Is the person the claimed user or not?".
- Speaker verification: if a person claims to be the user A,

 - Ho: X is from the claimed user A.
 - H1: X is NOT from the claimed user A.
- Data modeling: commonly use GMM for both H₀ and H₁.
 - Mixture number depends on the amount of available data, usually from 16 to 256.
 - For simplicity or estimation reliability, each Gaussian mixand is assumed to be diagonal.
 - For each known user *a* registered in the system, we must estimate two GMM's Λ_a and $\overline{\Lambda}_a$ for its H_0 and H_1 .

