

# Double-Ended Queues

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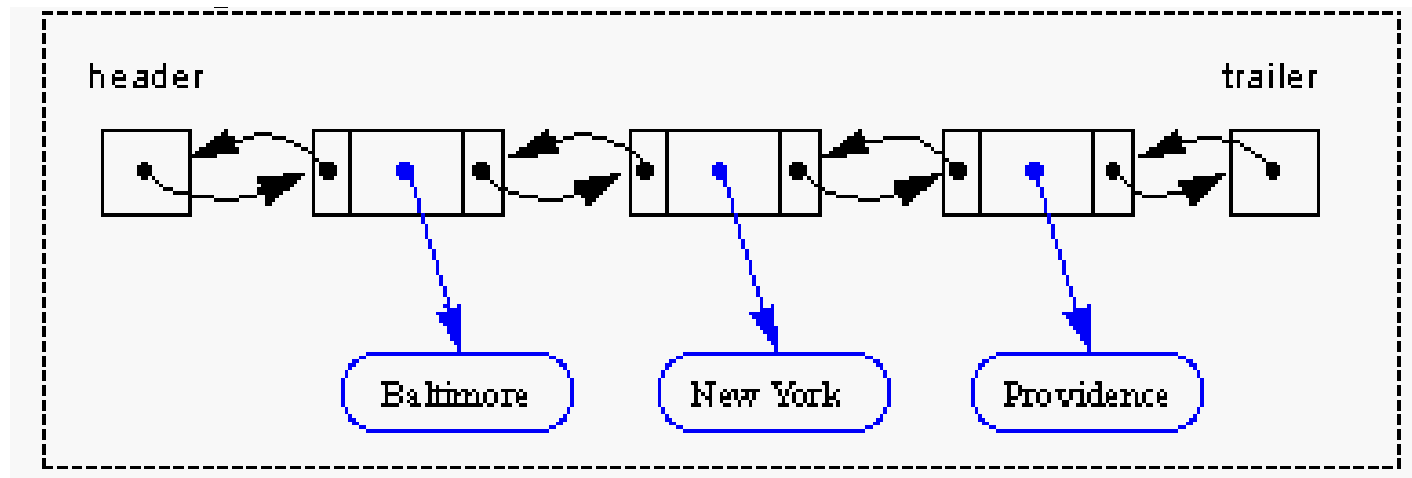
section 5.3 of textbook

# Double-Ended Queue ADT

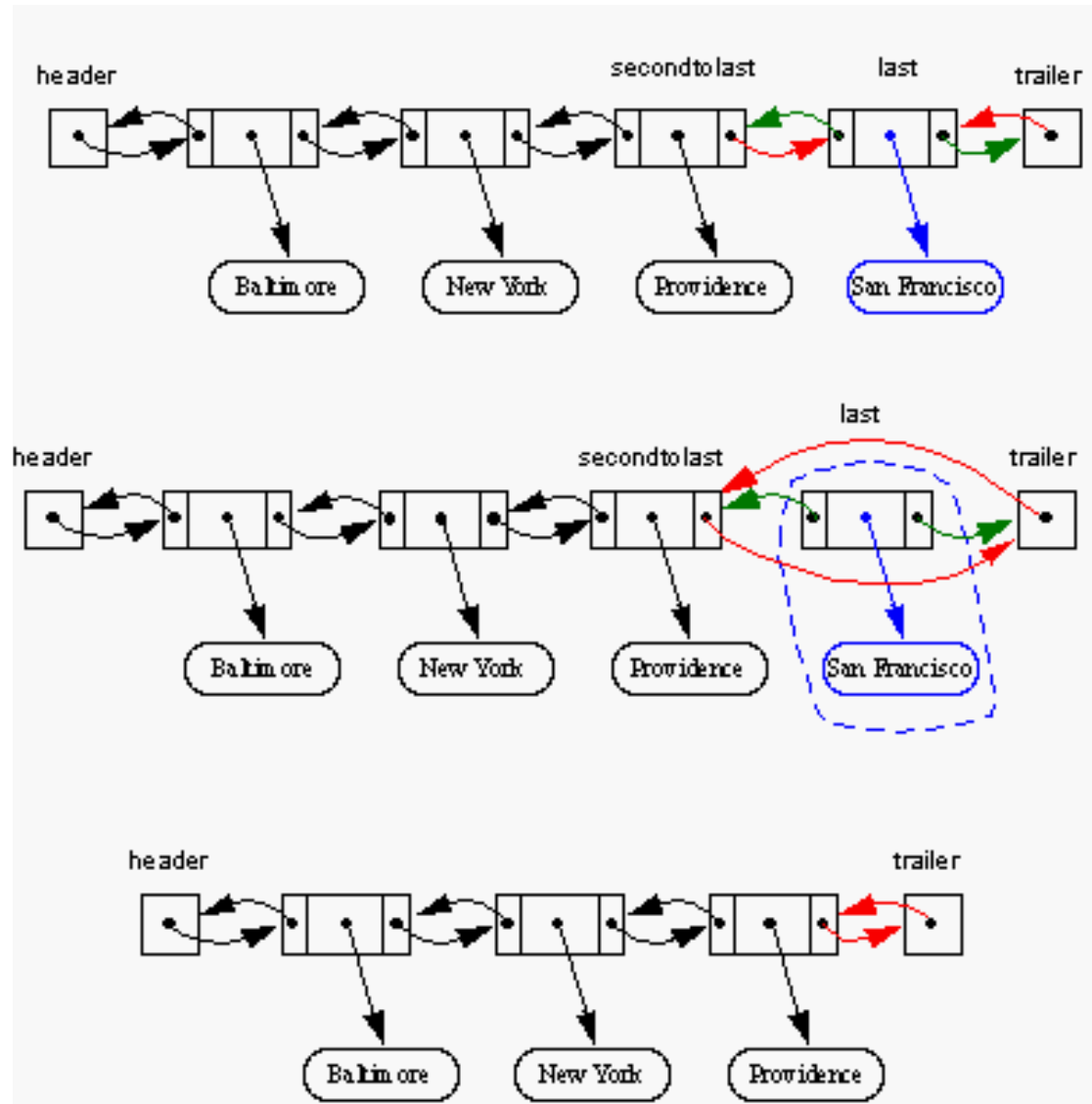
- **Deque** (pronounced “deck”)
- Allows insertion and deletion at both the **front** and the **rear** of the queue
- Deque ADT: operations
  - addFirst(e)*: insert *e* at the beginning of the deque
  - addLast(e)*: insert *e* at the end of the deque
  - removeFirst()*: remove and return the first element
  - removeLast()*: remove and return the last element
  - getFirst()*: return the first element
  - getLast()*: return the last element
  - isEmpty()*: return true if deque is empty; false otherwise
  - size()*: return the number of objects in the deque

# Implementation Choices

- Arrays
  - Similar to queue implementation ([homework](#))
- Linked lists: singly or doubly linked?
  - Removing at the tail costs  $O(n)$  for singly lined list



# *removeLast()* and *addLast()*



# Implementing Stacks and Queues with Deques

Stack Method	Deque Implementation
size()	size()
isEmpty()	isEmpty()
top()	last()
push(e)	insertLast(e)
pop()	removeLast()

Queue Method	Deque Implementation
size()	size()
isEmpty()	isEmpty()
front()	first()
enqueue()	insertLast(e)
dequeue()	removeFirst()

# The Adapter Pattern

- Using methods of one class to implement methods of another class
- Example: using Deque to implement Stack and Queue

# Extendable Arrays

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# Extendable Array Implementation

When *push()/insert()* is called and an overflow occurs ( $n = N$ ):

- Allocate a new array  $T$  of capacity  $2N$
- Copy contents of the original array  $V$  into the first half of the new array  $T$
- Set  $V = T$
- Perform the insertion using new array  $V$
- Note: when the number of elements in the list goes below a threshold (e.g.,  $N/4$ ), shrink the array by half the current size  $N$  of the array.
  - **not** to waste the memory.



# Time Analysis

- “push”: inserting an element to be the last element of a list (or top of a stack)
- $add(e) \{$ 
  - if ( full stack ) then extend the array;
  - “push”  $e$  to new array; $\}$
- Proposition 1:

Let  $S$  be a list implemented by means of an extendable array  $V$  as described before. The total time to perform a series of  $n$  “push” operations in  $S$ , starting from  $S$  being empty and  $V$  having size  $N = 1$ , is  $O(n)$ .

# Pseudo-code

```
int [ ] V = new int[1]; N = 1; top = -1;
input element e;
for( i = 0; i < n; i++ ) {
    if( stack is full ) {
        allocate a new array T of capacity 2N;
        copy V[i] to T[i] for i = 0, 1, ..., N-1;    // a for loop
        set V = T;
        N = N * 2;
    }
    top = top + 1;
    V[top] = e;
    input next element e;
}
```

# Time Analysis

1. All array **extensions**:  $O(?)$ 
  - Allocate a new array **T** of capacity **2N**
  - Copy **V[i]** to **T[i]** for  $i = 0, 1, \dots, N-1$
  - Set **V** = **T**
2. All “push” operations take  **$O(n)$**  (each “push” takes  $O(1)$ )

Running time of all array **extensions**:

- If the array is extended **k** times, then  $n = 2^k$
- The total number of copies is:  
 $1 + 2 + 4 + 8 + \dots + 2^{k-1} = 2^k - 1 = n - 1 = \mathbf{O(n)}$

Total =  **$O(n)$**  +  **$O(n)$**  =  **$O(n)$**

# Increment Strategies

- `java.util.ArrayList` and `java.util.Vector` use extendable arrays.
- *capacityIncrement* determines **how** the array grows.
- There exist two approaches.
  - *capacityIncrement* = 0:      array size doubles
  - *capacityIncrement* =  $c > 0$ :      array adds  $c$  new cells
- Proposition 2:

If we create an initially empty `java.util.Vector` object with a fixed positive *capacityIncrement* value, then performing a series of  **$n$**  push operations on this vector takes  **$\Omega(n^2)$**  time.
- $\Omega(n^2)$ : takes at least time  $n^2$

# Increment Strategies (2)

## 1. Array extensions: $O(?)$

- Let  $a$  be the initial size of array  $V$
- Let  $capacityIncrement = c$
- If the array is extended  $k$  times then  $n = a + ck$
- The total number of copies is:  
$$(a) + (a+c) + (a+2c) + \dots + (a+(k-1)c) =$$
$$ak + c(1+2+\dots+(k-1)) = ak + ck(k-1)/2 = \theta(k^2) = \theta(n^2)$$
- We infer  $\Omega(n^2)$  from  $\theta(n^2)$

## 2. All “push” operations take $O(n)$ (each “push” takes $O(1)$ )

# Next lecture ...

- Trees (chapter 7)