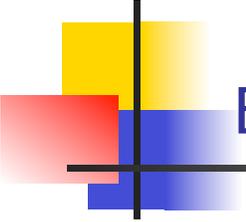


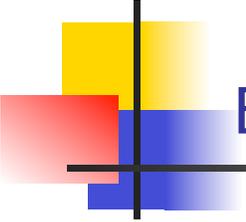
Equivalence Class Testing

Chapter 6



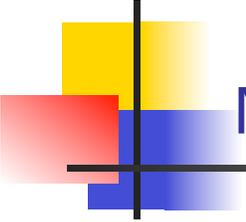
Boundary value problems

- **What problems does boundary value testing have?**



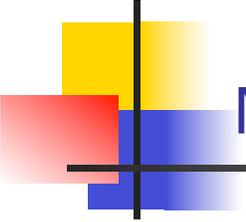
Boundary value problems – 2

- Boundary Value Testing derives test cases with
 - Serious gaps
 - Massive redundancy



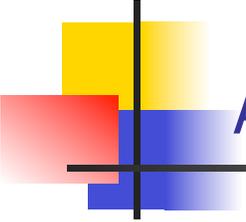
Motivation for equivalence class testing

- **What are the motivations for equivalence class testing?**



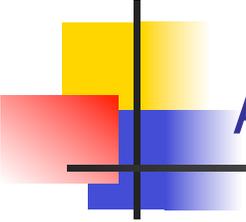
Motivation for equivalence class testing – 2

- Avoid redundancy
 - Have fewer test cases
- Complete testing
 - Remove gaps



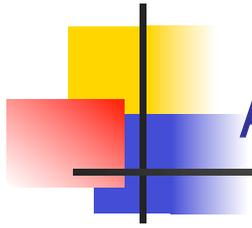
Addressing the motivation

- **How do equivalence classes meet the motivations of complete testing and avoiding redundancy?**



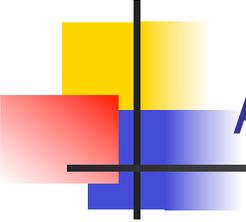
Addressing the motivation– 2

- The variable domain is partitioned into disjoint sub-sets



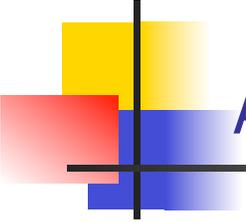
Assumptions

- **What assumptions are made?**



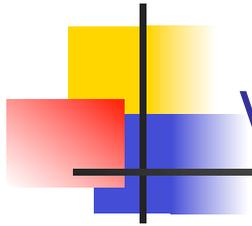
Assumptions – 2

- Program is a function from input to output
- Input and/or output variables have well defined intervals
 - For a two-variable function $F(x_1, x_2)$
 $a \leq x_1 \leq d$, with intervals $[a, b)$, $[b, c)$, $[c, d]$
 $e \leq x_2 \leq g$, with intervals $[e, f)$, $[f, g]$



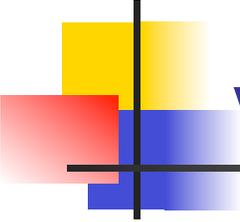
Assumptions – 3

- Completeness
 - The entire set is represented by the union of the sub-sets
- Redundancy
 - The disjointness of the sets assures a form of non-redundancy
- Choose one test case from each sub-set



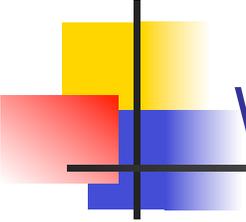
Variations

- **What variations are used for equivalence class testing?**



Variations – 2

- Use the same two orthogonal dimensions as in boundary value analysis
 - Robustness
 - Robust-normal distinguishes valid data from invalid data
 - Single/Multiple Fault Assumption
 - Weak-strong distinguishes single from multiple fault
- Combinations give four variations.



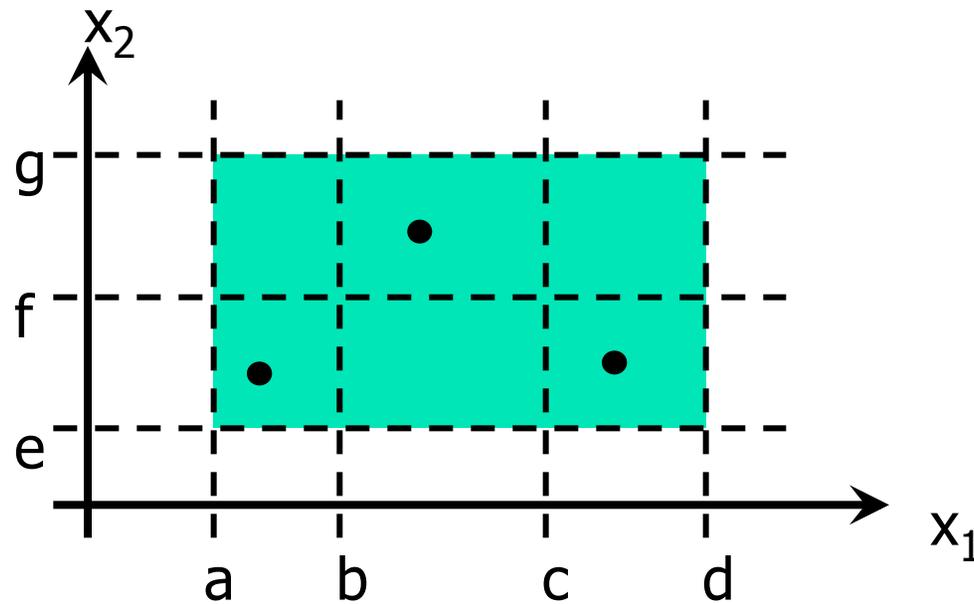
Weak-Normal ECT

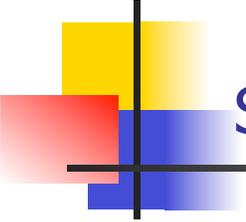
- **What is the number of test cases for weak-normal testing?**

Weak-Normal ECT – 2

Number of test cases =

$\max / \left[\left[v : 1 \dots \#variables \bullet \text{number_equivalence_classes}(\text{variable}_v) \right] \right]$





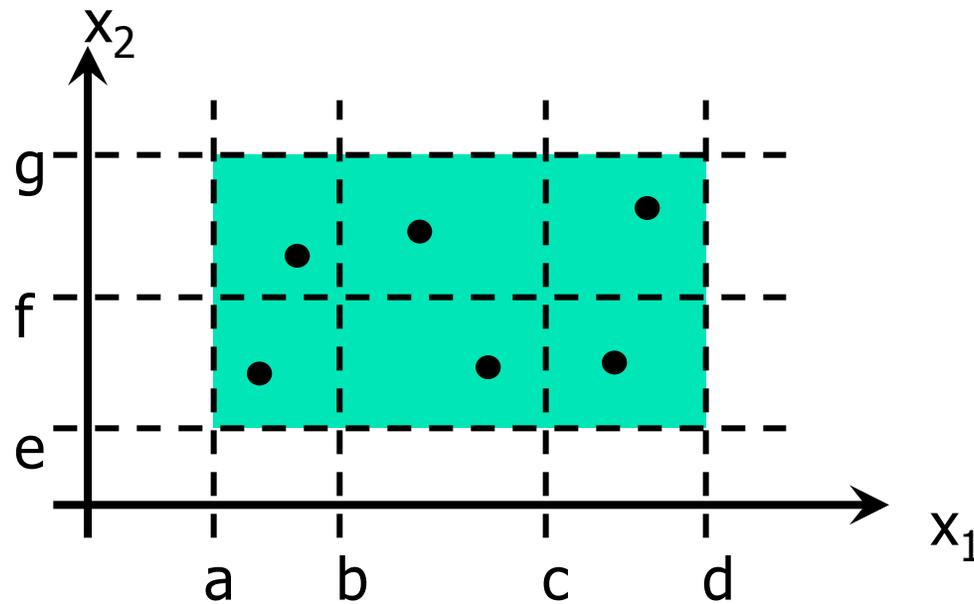
Strong-Normal ECT

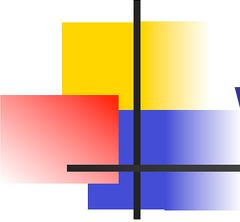
- **What is the number of test cases for strong-normal testing?**

Strong-Normal ECT – 2

Number of test cases =

$\times / \llbracket v : 1 \dots \#variables \bullet \text{number_equivalence_classes}(\text{variable}_v) \rrbracket$





Weak-Robust ECT

- **What is the number of test cases for weak-robust testing?**

Weak-Robust ECT – 2

Number of test cases =

$$\begin{aligned} & \max / \left[\left[v : 1 \dots \#variables \cdot \text{number_equivalence_classes}(\text{variable}_v) \right] \right] \\ & + \\ & + / \left[\left[v : 1 \dots \#variables \cdot \text{number_invalid_bounds}(\text{variable}_v) \right] \right] \end{aligned}$$

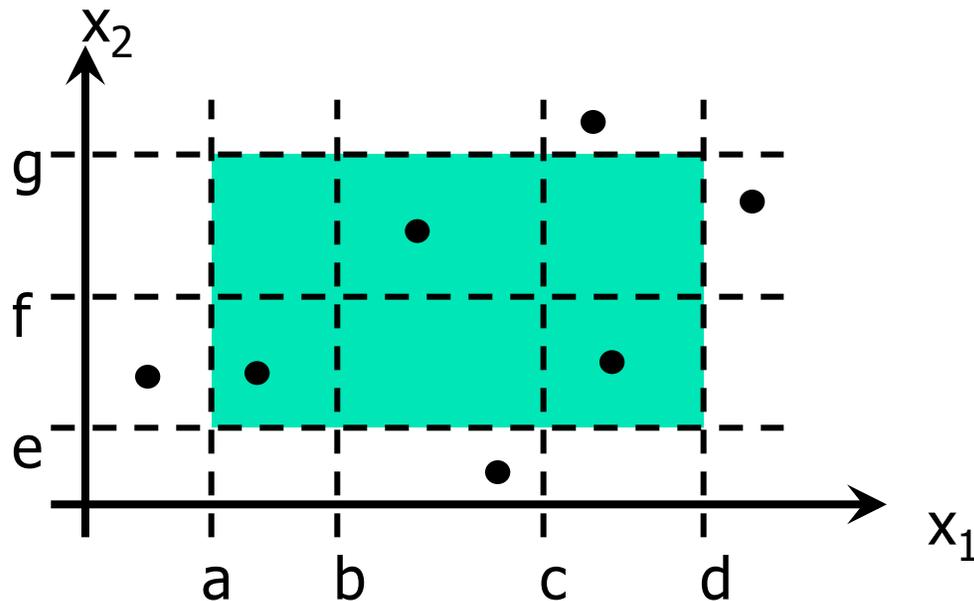
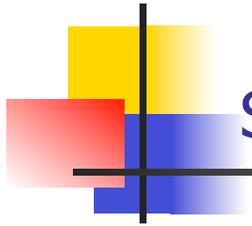


Figure 6.3 in the textbook is incorrect



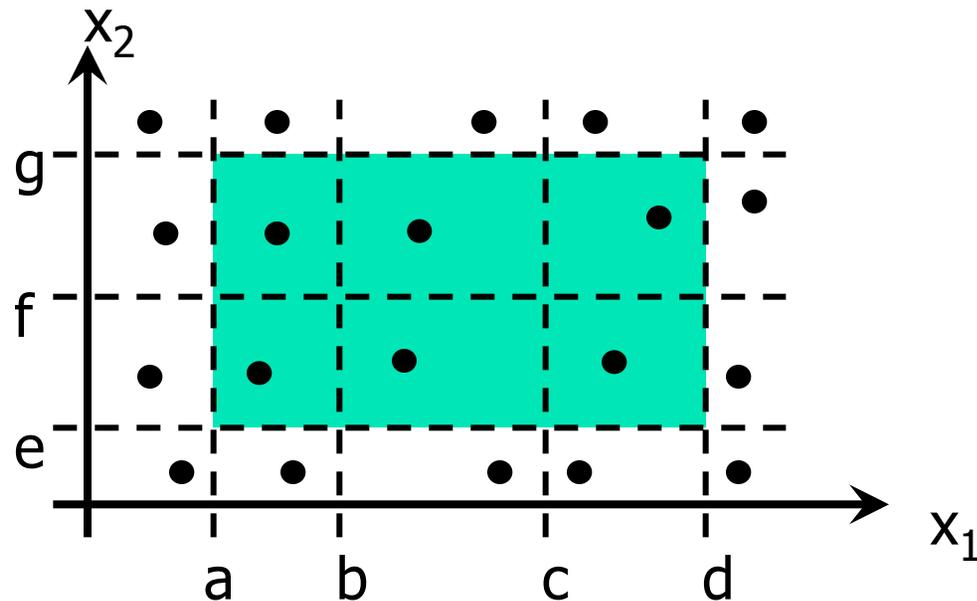
Strong-Robust ECT

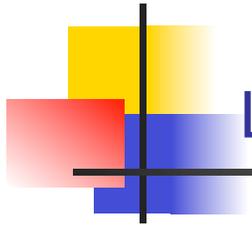
- **What is the number of test cases for strong-robust testing?**

Strong-Robust ECT – 2

Number of test cases =

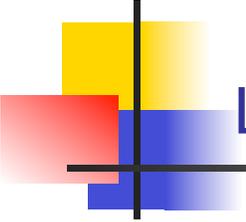
$\times / \left[\left[v : 1 \dots \# \text{variables} \bullet \text{number_equivalence_classes}(\text{variable}_v) \right. \right.$
 $\left. \left. + \text{number_invalid_bounds}(\text{variable}_v) \right] \right]$





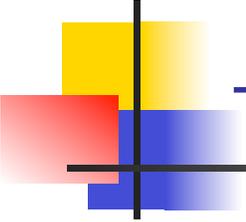
Limitations of ECT

- **What are the limitations of equivalence class testing?**



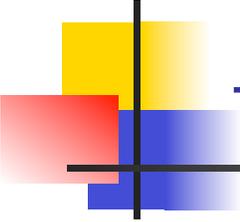
Limitations of ECT – 2

- The same as those for boundary value testing
 - Does not work well for Boolean variables
 - Does not work well for logical variables
 - When variables are not independent – i.e. are dependent
 - Not that useful for strongly-typed languages
- For robust variations same as for boundary value testing
 - Difficult or impossible to determine expected values for invalid variable values



Triangle Output Equivalence Classes

- Four possible outputs
 - Not a Triangle
 - Isosceles
 - Equilateral
 - Scalene



Triangle Output Equivalence Classes – 2

- Output (range) equivalence classes

$O1 = \{a, b, c : 0 .. 200 \mid \text{equilateral_triangle} (\langle a,b,c \rangle) \}$

$O2 = \{a, b, c : 0 .. 200 \mid \text{isocetes_triangle} (\langle a,b,c \rangle) \}$

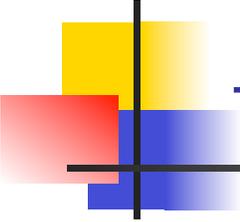
$O3 = \{a, b, c : 0 .. 200 \mid \text{scalene_triangle} (\langle a,b,c \rangle) \}$

$O4 = \{a, b, c : 0 .. 200 \mid \text{not_a_triangle} (\langle a,b,c \rangle) \}$

What are the number of test cases for

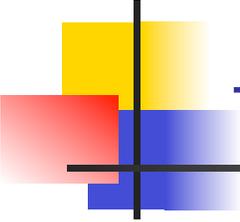
- **weak-normal?**
- **strong-normal?**
- **weak-robust?**
- **strong-robust?**

Why don't the previous formulas work?



Triangle – Weak Normal Test Cases

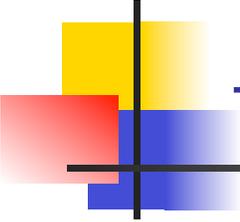
Test Case	a	b	c	Expected Output
WN1	5	5	5	Equilateral
WN2	2	2	3	Isosceles
WN3	3	4	5	Scalene
WN4	4	1	2	Not a Triangle



Triangle – Weak Robust Test Cases

Weak-normal cases + following error cases

Test Case	a	b	c	Expected Output
WR1	-1	5	5	a not in range
WR2	5	-1	5	b not in range
WR3	5	5	-1	c not in range
WR4	201	5	5	a not in range
WR5	5	201	5	b not in range
WR6	5	5	201	c not in range



Triangle – input equivalence classes

$$D1 = \{ a,b,c : 1..200 \mid a = b = c \bullet \langle a,b,c \rangle \}$$

$$D2 = \{ a,b,c : 1..200 \mid a = b, a \neq c \bullet \langle a,b,c \rangle \}$$

$$D3 = \{ a,b,c : 1..200 \mid a = c, a \neq b \bullet \langle a,b,c \rangle \}$$

$$D4 = \{ a,b,c : 1..200 \mid b = c, a \neq b \bullet \langle a,b,c \rangle \}$$

$$D5 = \{ a,b,c : 1..200 \mid a \neq b, a \neq c, b \neq c \bullet \langle a,b,c \rangle \}$$

$$D6 = \{ a,b,c : 1..200 \mid a \geq b+c \bullet \langle a,b,c \rangle \}$$

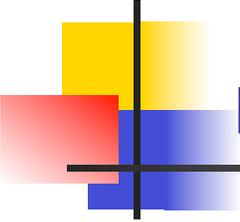
$$D7 = \{ a,b,c : 1..200 \mid b \geq a+c \bullet \langle a,b,c \rangle \}$$

$$D8 = \{ a,b,c : 1..200 \mid c \geq a+b \bullet \langle a,b,c \rangle \}$$

What are the number of test cases for

- **weak-normal?**
- **strong-normal?**
- **weak-robust?**
- **strong-robust?**

Is this a good set of equivalence classes to use or is there a problem?



NextDate – naive equivalence classes

$M1 = \{ \text{month} : 1 .. 12 \}$

$D1 = \{ \text{day} : 1 .. 31 \}$

$Y1 = \{ \text{year} : 1812 .. 2012 \}$

Invalid data

$M2 = \{ \text{month} : \text{Integer} \mid \text{month} < 1 \}$

$M3 = \{ \text{month} : \text{Integer} \mid \text{month} > 12 \}$

$D2 = \{ \text{day} : \text{Integer} \mid \text{day} < 1 \}$

$D3 = \{ \text{day} : \text{Integer} \mid \text{day} > 31 \}$

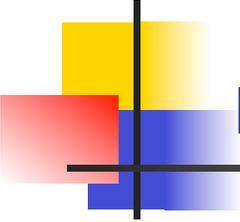
$Y2 = \{ \text{year} : \text{Integer} \mid \text{year} < 1812 \}$

$Y3 = \{ \text{year} : \text{Integer} \mid \text{year} > 2012 \}$

What are the number of test cases for

- **weak-normal?**
- **strong-normal?**
- **weak-robust?**
- **strong-robust?**

What is the problem with using these equivalence classes?



NextDate – improved equivalence classes

M1 = {month : 1 .. 12 | days(month) = 30 }

M2 = {month : 1 .. 12 | days(month) = 31 }

M3 = {month : {2} }

D1 = {day : 1 .. 28}

D2 = {day : {29} }

D3 = {day : {30} }

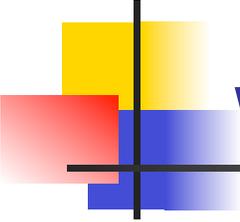
D4 = {day : {31} }

Y1 = {year : {2000} }

Y2 = {year : 1812 .. 2012 | leap_year (year) \wedge year \neq 2000 }

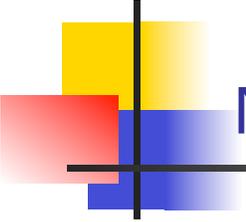
Y3 = {year : 1812 .. 2012 | common_year (year) }

**What is good and bad
with using these
equivalence classes?**



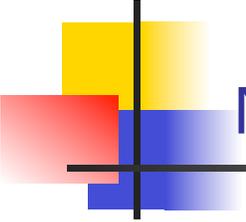
Weak Normal Test Cases

Test Case	Month	Day	Year	Expected Output
WN1	6	14	1900	6/15/1900
WN2	7	29	1996	7/30/1996
WN3	2	30	2002	Invalid input date
WN4	6	31	1900	Invalid input date



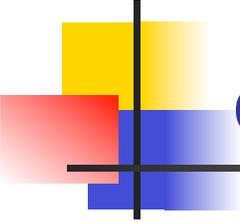
NextDate strong test cases

- **What are the number of test cases for strong-normal testing?**
- **What are the number of test cases for strong-robust testing?**



NextDate strong test cases – 2

- There are 36 strong-normal test cases (3 x 4 x 3)
- Some redundancy creeps in
 - Testing February 30 and 31 for three different types of years seems unlikely to reveal errors
- There are 150 strong-robust test cases (5 x 6 x 5)



Commission problem – input classes

L1 = {locks : 1 .. 70 }

L2 = {locks : { -1 } }

S1 = {stocks : 1 .. 80 }

B1 = {barrels : 1 .. 90}

Invalid data

L3 = {locks : Integer | locks \leq 0 \wedge locks \neq -1}

L4 = {locks : Integer | locks > 70 }

S2 = {stocks : Integer | stocks < 1 }

S3 = {stocks : Integer | stocks > 80 }

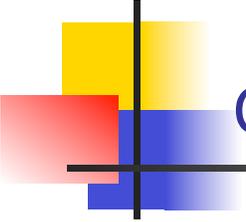
B2 = {barrels : Integer | barrels < 1 }

B3 = {barrels : Integer | barrels > 90 }

What are the number of test cases for

- **weak-normal?**
- **strong-normal?**
- **weak-robust?**
- **strong-robust?**

What is good and not good about using these classes?



Commission problem – output classes

Sales = $45 \times \text{locks} + 30 \times \text{stocks} + 25 \times \text{barrels}$

S1 = {sales : 0 .. 1000 }

S2 = {sales : 1001 .. 1800 }

S3 = {sales : Integer | sales > 1800 }

Invalid data

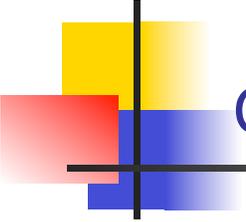
S4 = {sales : Integer | sales < 0}

What are the number of test cases for

- **weak-normal?**
- **strong-normal?**
- **weak-robust?**
- **strong-robust?**

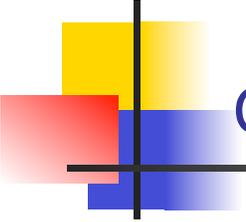
What is good and not good about using these classes?

Figure 5.6, page 84 shows the classes pictorially



Guidelines and observations

- Equivalence Class Testing is appropriate when input data is defined in terms of intervals and sets of discrete values.
- Equivalence Class Testing is strengthened when combined with Boundary Value Testing
- Strong equivalence makes the presumption that variables are independent.
 - If that is not the case, redundant test cases may be generated



Guidelines and observations – 2

- Complex functions, such as the NextDate program, are well-suited for Equivalence Class Testing
- Several tries may be required before the “right” equivalence relation is discovered
 - If the equivalence classes are chosen wisely, the potential redundancy among test cases is greatly reduced.
 - The key point in equivalence class testing is the choice of the equivalence relation that determines the classes.