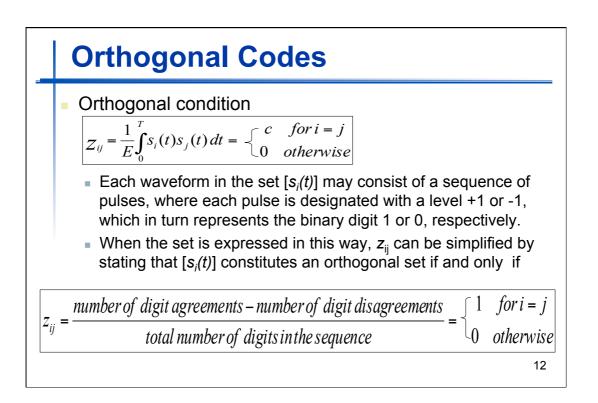
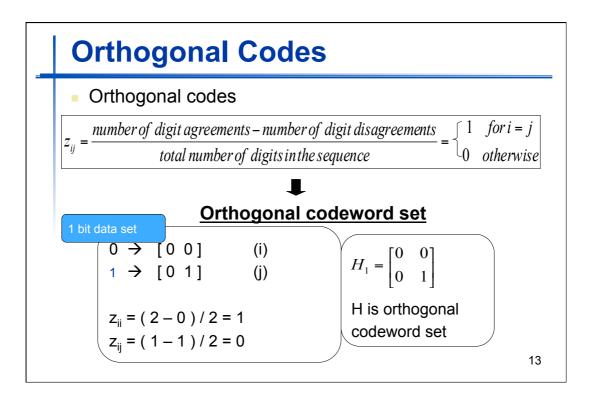
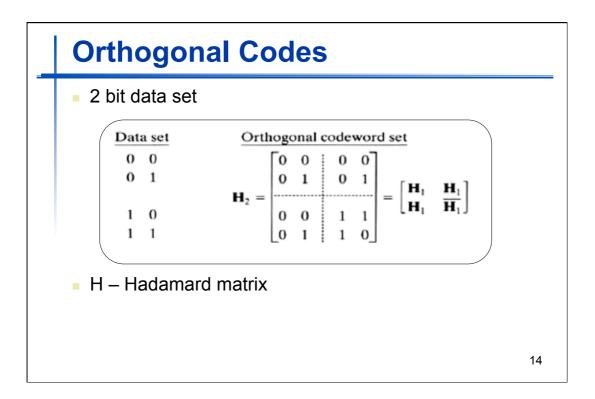


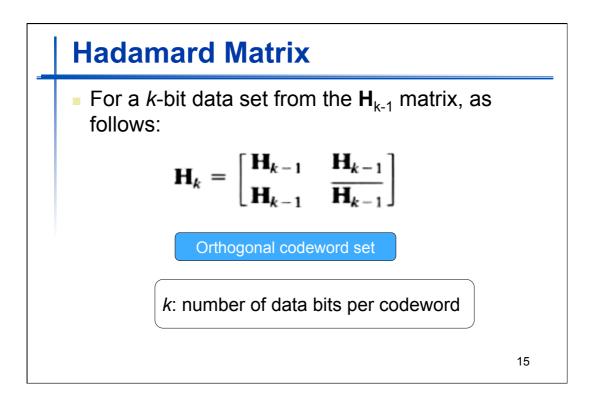
The Goal of Waveform Coding

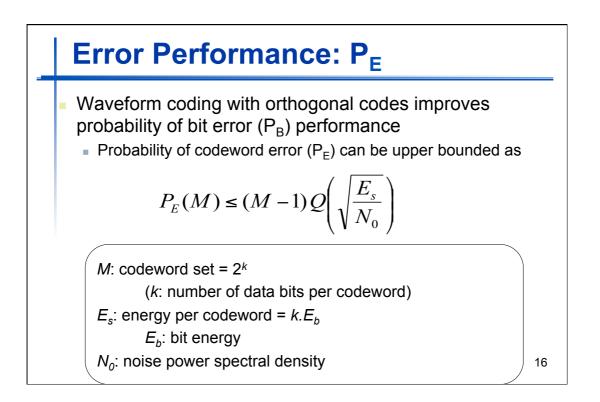
- Transform a waveform set (representing a message set) into an improved waveform set. The improved waveform set can then be used to provide improved probability of bit error (P_B) compared to the original set.
- The encoding procedure endeavors to make each of the waveforms in the coded signal set as unalike as possible; the goal is to render the cross-correlation coefficient z_{ij} (among all pairs of signals) as small as possible.
- The most popular of waveform codes are referred to as orthogonal and biorthogonal codes.

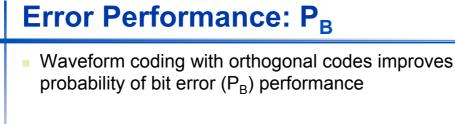












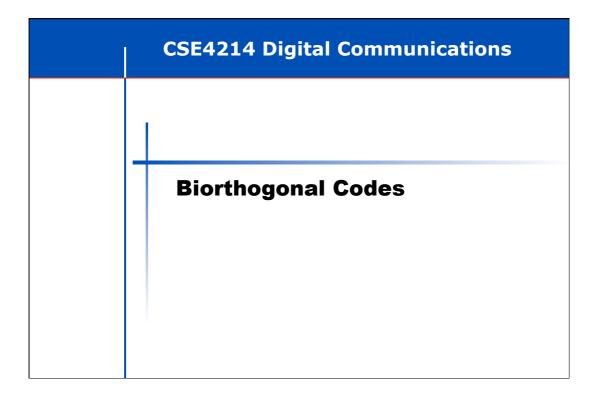
Knowing that

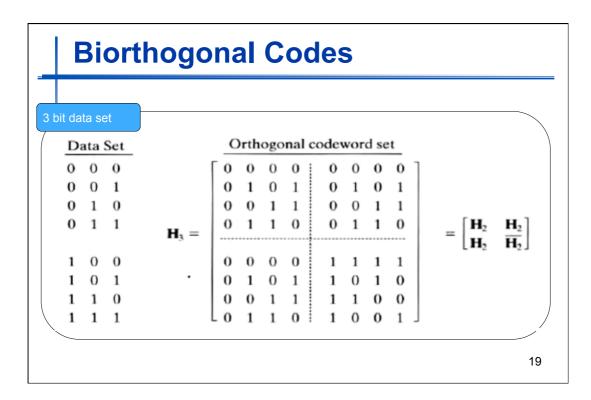
$$\frac{P_B(k)}{P_E(k)} = \frac{2^{k-1}}{2^k - 1} \quad or \quad \frac{P_B(M)}{P_E(M)} = \frac{M/2}{(M-1)}$$

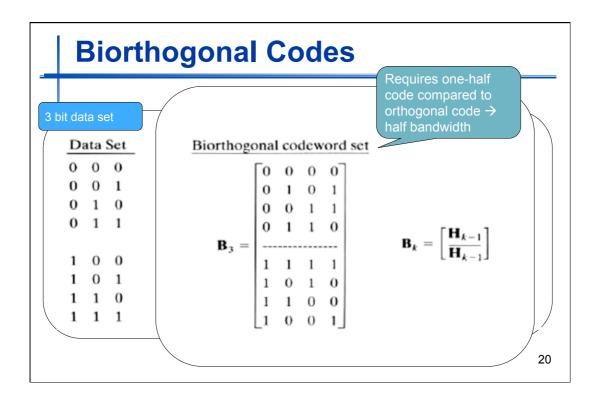
Probability of bit error (P_B) can be upper bounded as

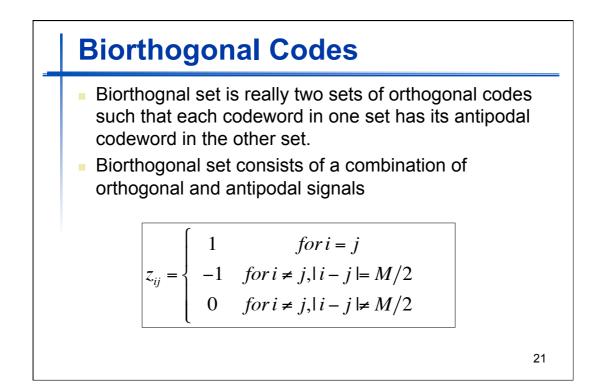
$$P_{B}(k) \leq (2^{k-1}) Q\left(\sqrt{\frac{kE_{b}}{N_{0}}}\right) \quad of$$
$$P_{B}(M) \leq \frac{M}{2} Q\left(\sqrt{\frac{E_{s}}{N_{0}}}\right)$$

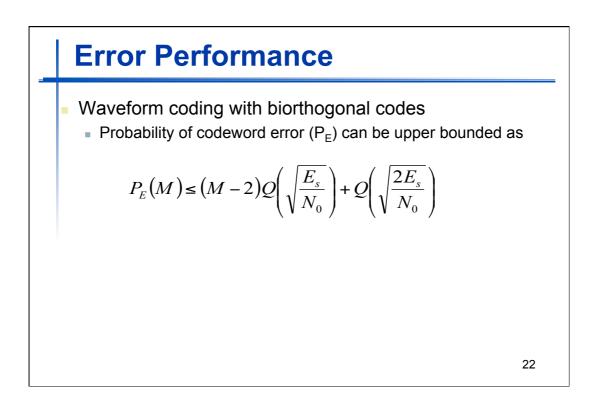
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Error Performance

- Waveform coding with biorthogonal codes
 - Probability of codeword error (P_E) can be upper bounded as

$$P_{E}(M) \leq (M-2)Q\left(\sqrt{\frac{E_{s}}{N_{0}}}\right) + Q\left(\sqrt{\frac{2E_{s}}{N_{0}}}\right)$$

• We can approximate P_B(M) by:

$$P_{B}(M) \leq \frac{1}{2} \left[(M-2)Q\left(\sqrt{\frac{E_{s}}{N_{0}}}\right) + Q\left(\sqrt{\frac{2E_{s}}{N_{0}}}\right) \right]$$

 Compared to orthogonal code, biorthogonal code has improved P_B performance and requires only half the bandwidth.

