



# Path Testing + Coverage

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## Chapter 8



# Structural Testing

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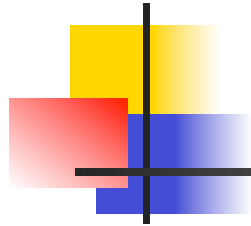
- Also known as glass/white/open box testing
- A software testing technique whereby explicit knowledge of the internal workings of the item being tested are used to select the test data
- Functional Testing uses program specification
- Structural Testing is based on specific knowledge of the source code to define the test cases and to examine outputs.



# Structural Testing

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- Structural testing methods are very amenable to:
  - Rigorous definitions
    - Control flow, data flow, coverage criteria
  - Mathematical analysis
    - Graphs, path analysis
  - Precise measurement
    - Metrics, coverage analysis

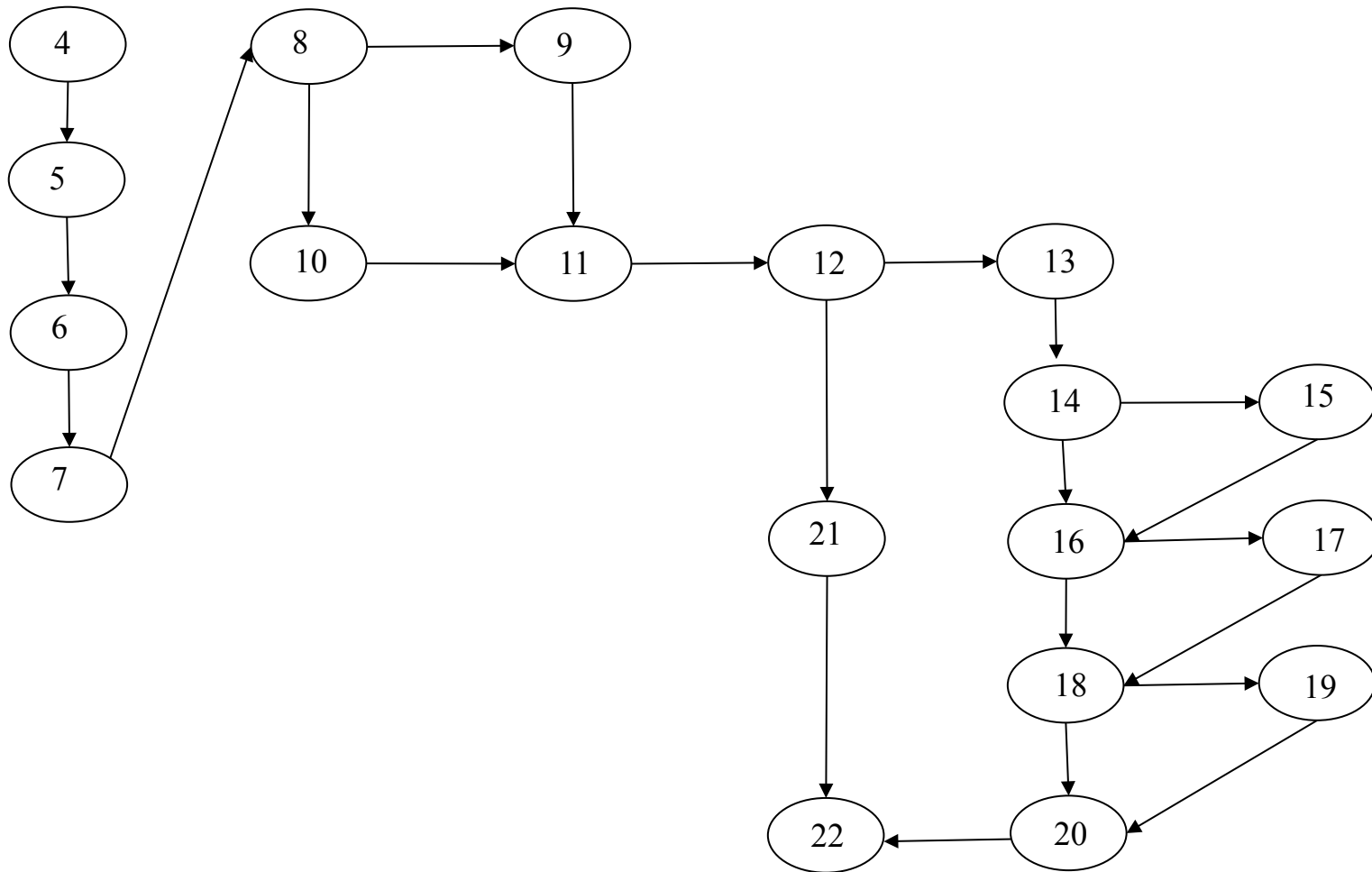


# Program Graph - Definition

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- Given a program written in an imperative programming language, its **program graph** is a directed graph in which nodes are statement fragments, and edges represent flow of control
- A complete statement is also considered a statement fragment

# Program Graph - Example





# DD-Path

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- A decision-to-decision path (DD-Path) is a chain in a program graph such that:
  - Case1: it consists of a single node with  $\text{indeg}=0$
  - Case2: it consists of a single node with  $\text{outdeg}=0$
  - Case3: it consists of a single node with  $\text{indeg} \geq 2$  or  $\text{outdeg} \geq 2$
  - Case4: it consists of a single node with  $\text{indeg} = 1$ , and  $\text{outdeg} = 1$
  - Case5: it is a maximal chain of length  $\geq 1$
- DD-Paths are also known as **segments**



# DD-Path Graph

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- Given a program written in an imperative language, its **DD-Path graph** is a directed graph, in which nodes are DD-Paths of its program graph, and edges represent control flow between successor DD-Paths.
- Also known as **Control Flow Graph**



# Control Flow Graph Derivation

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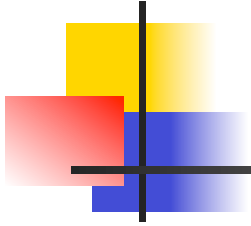
- Straightforward process
- Some judgement is required
- The last statement in a segment must be a predicate, a loop control, a break, or a method exit
- Let's try an example...



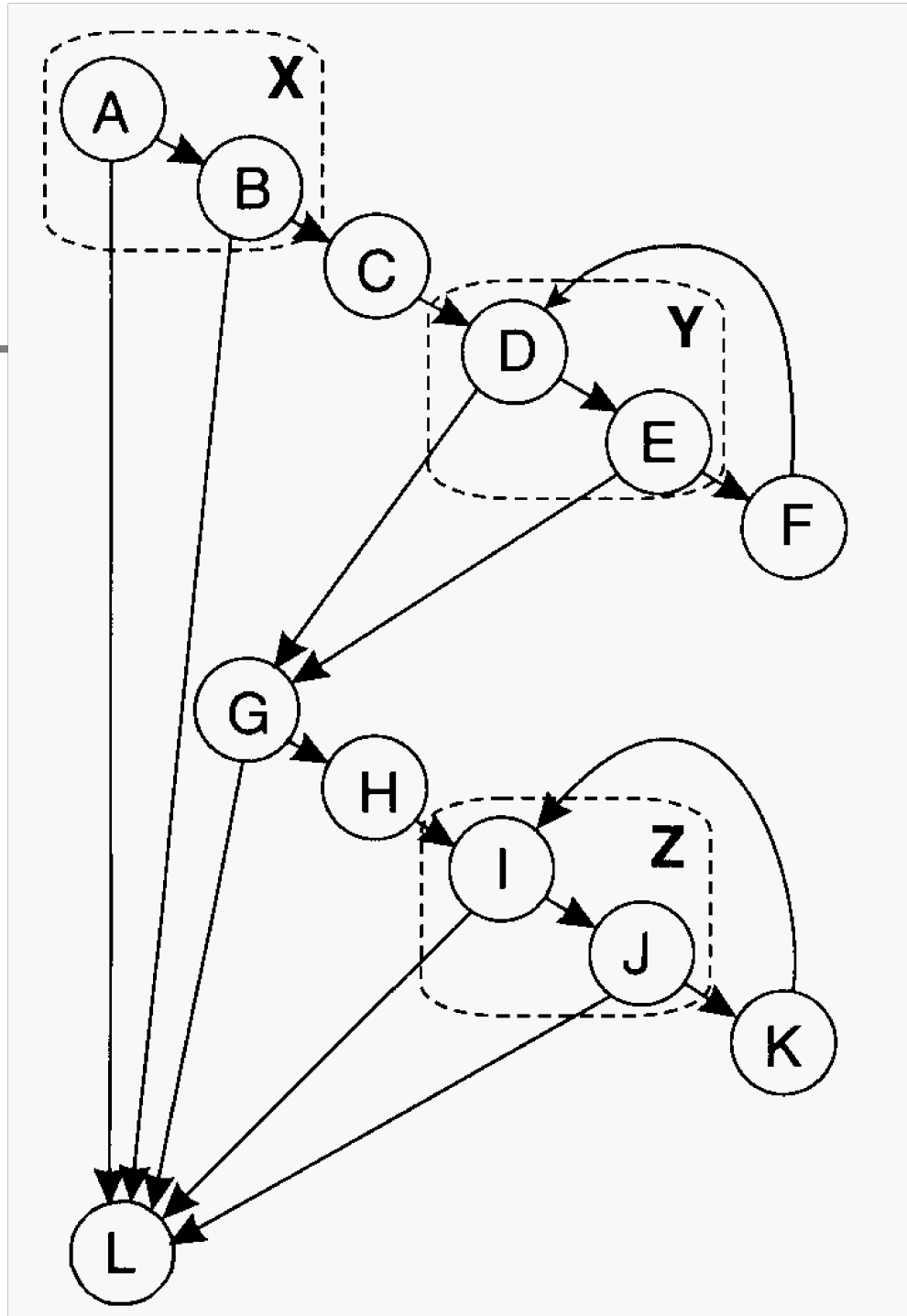
```

public int displayLastMsg(int nToPrint) {
    np = 0;
    if ((msgCounter > 0) && (nToPrint > 0)) {
        for (int j = lastMsg; ((j != 0) && (np < nToPrint)); --j) {
            System.out.println(messageBuffer[j]);
            ++np;
        }
        if (np < nToPrint) {
            for (int j = SIZE; ((j != 0) && (np < nToPrint)); --j) {
                System.out.println(messageBuffer[j]);
                ++np;
            }
        }
    }
    return np;
}

```



# Control flow graph for previous slide





# Control flow graphs

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- Depict which program segments may be followed by others
- A segment is a node in the CFG
- A conditional transfer of control is a **branch** represented by an edge
- An **entry node** (no inbound edges) represents the entry point to a method
- An **exit node** (no outbound edges) represents an exit point of a method



# Control flow graphs

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- An **entry-exit path** is a path from the entry node to the exit node
- **Path expressions** represent paths as sequences of nodes
- Loops are represented as segments within parentheses followed by an asterisk
- There are 22 different path expressions in our example



# Example path expressions

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AL

ABL

ABCDGL

ABCDEGL

ABC(DEF)\*DGL

ABC(DEF)\*DEGL

ABCDGHIL

ABCDGHIJL

ABCDGH(IJK)\*IL

ABC(DEF)\*DEGH(IJK)\*IJL



# Code coverage models

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- Statement Coverage
- Segment Coverage
- Branch Coverage
- Multiple-Condition Coverage



# Statement coverage

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- Achieved when all statements in a method have been executed at least once
- A test case that will follow the path expression below will achieve statement coverage in our example

ABC(DEF)\*DGH(IJK)\*IL

- One test case is enough to achieve statement coverage!



# Segment coverage

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- **Segment coverage** counts segments rather than statements
- May produce drastically different numbers
  - Assume two segments P and Q
  - P has one statement, Q has nine
  - Exercising only one of the segments will give 10% or 90% statement coverage
  - Segment coverage will be 50% in both cases





# Statement coverage problems

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- Predicate may be tested for only one value (misses many bugs)
- Loop bodies may only be iterated once
- Statement coverage can be achieved without branch coverage. Important cases may be missed

```
String s = null;  
if (x != y) s = "Hi";  
String s2 = s.substring(1);
```



# Branch coverage

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- Achieved when every path from a node is executed at least once
- At least one true and one false evaluation for each predicate
- Can be achieved with  $D+1$  paths in a control flow graph with  $D$  2-way branching nodes and no loops
  - Even less if there are loops



# Branch coverage problems

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- Short-circuit evaluation means that many predicates might not be evaluated
- A compound predicate is treated as a single statement. If  $n$  clauses,  $2^n$  combinations, but only 2 are tested
- Only a subset of all entry-exit paths is tested

```
if (a == b) x++;  
if (c == d) x--;
```



# Multiple-condition coverage

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- All true-false combinations of simple conditions in compound predicates are considered at least once
- A truth table may be necessary
- Not necessarily achievable due to lazy evaluation or mutually exclusive conditions

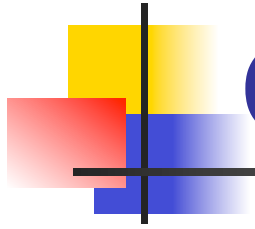
```
if ( (x > 0) && (x < 5) ) ...
```



# Dealing with Loops

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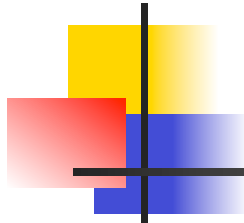
- Loops are highly fault-prone, so they need to be tested carefully
- Simple view: Every loop involves a decision to traverse the loop or not
- A bit better: Boundary value analysis on the index variable
- Nested loops have to be tested separately starting with the innermost



# Creating test cases

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- In order to increase the coverage of a test suite, one needs to generate test cases that exercise certain statements or follow a specific path
- This is not always easy to do...



# CFG question

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- **What is the control flow graph for the following?**

**if  $a < b$  then  $c = a + b ; d = a * b$   
    **else  $c = a * b ; d = a + b$****

**if  $c < d$  then  $x = a + c ; y = b + d$   
    **else  $x = a * c ; y = b * d$****

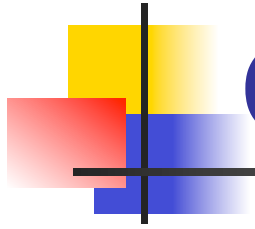


# Creating a test case

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- **What is the key question that needs to be answered to be able to create a test for a path?**





# Creating a test case

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- **What is the key question that needs to be answered to be able to create a test for a path?**
  - How to make the path execute, if possible.
    - Generate input data that satisfies all the conditions on the path.



# Creating a test case

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- **What are the key items you need to generate a test case for a path?**



# Creating a test case

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- **What are the key items you need to generate a test case for a path?**
  - Input vector
  - Predicate
  - Path predicate
  - Predicate interpretation
  - Path predicate expression
  - Create test input from path predicate expression



# Input Vector

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- **What is an input vector?**



# Input Vector – 2

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- **What is an input vector?**
  - A collection of all data entities read by the routine whose values must be fixed prior to entering the routine.



# Input Vector – 3

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- **What are the members of an input vector?**



# Input Vector – 4

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- **What are the members of an input vector?**
  - Input arguments to the routine
  - Global variables and constants
  - Files
  - Network connections
  - Timers



# Predicate

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- **What is a predicate?**



# Predicate – 2

## ■ What is a predicate?

- A logical function evaluated at a decision point.

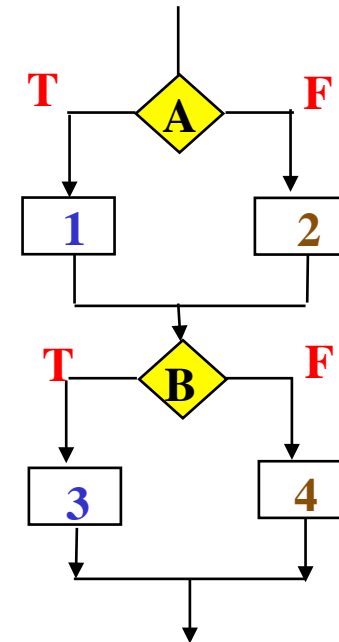
- In the following each of  $a < b$  and  $c < d$  are predicates

**if  $a < b$  then  $c = a + b$  ;  $d = a * b$**

**else  $c = a * b$  ;  $d = a + b$**

**if  $c < d$  then  $x = a + c$  ;  $y = b + d$**

**else  $x = a * c$  ;  $y = b * d$**





# Path predicate

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- **What is a path predicate?**

## Path predicate – 2

- The set of predicates associated with a path.

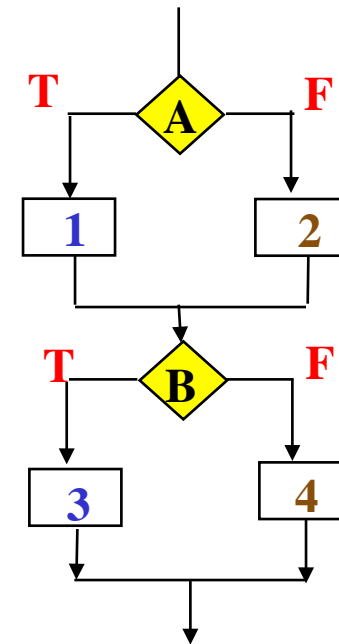
- $a < b = \text{true} \wedge c < d = \text{false}$   
is a path predicate

**if  $a < b$  then  $c = a + b$  ;  $d = a * b$**

**else  $c = a * b$  ;  $d = a + b$**

**if  $c < d$  then  $x = a + c$  ;  $y = b + d$**

**else  $x = a * c$  ;  $y = b * d$**





# Path Predicate Expression

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- **What is a path predicate expression?**



# Path Predicate Expression – 2

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- **What is a path predicate expression?**
  - An interpreted path predicate



# Predicate Interpretation

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- **What is a path predicate interpretation?**



# Predicate Interpretation – 2

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- **What is a path predicate interpretation?**
  - A path predicate may contain local variables.
  - Local variables cannot be selected independently of the input variables
  - Local variables are eliminated with **symbolic execution**



# Predicate Interpretation – 3

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- **What is symbolic execution?**
  - Symbolically substituting operations along a path in order to express the predicate solely in terms of the input vector and a constant vector.
  - A predicate may have different interpretations depending on how control reaches the predicate.

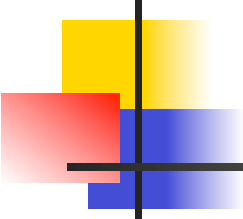




# Attributes of a Path Predicate Expression

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- **What are the attributes of a path predicate expression?**



# Attributes of a Path Predicate Expression – 2

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- **What are the attributes of a path predicate expression?**
  - No local variables
  - A set of constraints in terms of the input vector, and, maybe, constants
  - Path forcing inputs are generated by solving the constraints
  - If a path predicate expression has no solution, the path is infeasible



# Path Predicate Generating Input Values

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**if  $a < b$  then  $c = a + b$  ;  $d = a * b$   
    **else  $c = a * b$  ;  $d = a + b$**   
**if  $c < d$  then  $x = a + c$  ;  $y = b + d$   
    **else  $x = a * c$  ;  $y = b * d$******

---

- Path predicate       **$a < b = \text{true} \wedge c < d = \text{false}$**
- Substitute for c and d       **$c = a + b$      $d = a * b$**

**$a < b = \text{true} \wedge a + b < a * b = \text{false}$**

**$\rightarrow a < b \wedge a + b \geq a * b$**



# Path Predicate Generating Input Values – 2

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$$a < b \wedge a + b \geq a * b$$

- Solve for a and b **a = 0**  $\wedge$  **b = 1**
  - Solutions are not unique
  
- A solution exists
  - We have a feasible path
  
- No solution to the constraints
  - Have an infeasible path



# Organizing path predicates

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- **How can we organize the set of path predicates?**



# Organizing path predicates – 2

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- **How can we organize the set of path predicates?**
  - Use a decision table
    - **How would a decision table be used?**



# Decision table for the example

	<b>A1B3</b>	<b>A1B4</b>	<b>A2B3</b>	<b>A2B4</b>
<b>A &lt; B</b>	<b>T</b>	<b>T</b>	<b>F</b>	<b>F</b>
<b>C &lt; D</b>	<b>T</b>	<b>F</b>	<b>T</b>	<b>F</b>
<b>A value</b>	<b>2</b>	<b>0</b>	<b>1</b>	<b>5</b>
<b>B value</b>	<b>5</b>	<b>1</b>	<b>0</b>	<b>2</b>

Paths **A1B3** and **A2B4** give statement coverage  
or Paths **A1B4** and **A2B3** give statement coverage

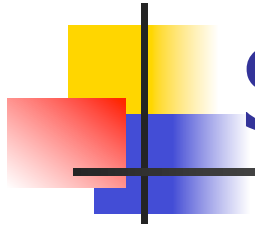


# Selecting paths

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- A program unit may contain a large number of paths.
  - Path selection becomes a problem
  - Some selected paths may be infeasible
- **What strategy would you use to select paths?**





# Selecting paths – 2

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- **What strategy would you use to select paths?**
  - Select as many short paths as possible
    - Tradeoffs?
  - Choose longer paths
    - Tradeoffs?



# Selecting paths – 3

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- **What about infeasible paths?**
  - What would you do about them?



# Selecting paths – 4

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- **What about infeasible paths?**
  - What would you do about them?
  - Make an effort to write program text with fewer or no infeasible paths.