ENG2200 Electric Circuits

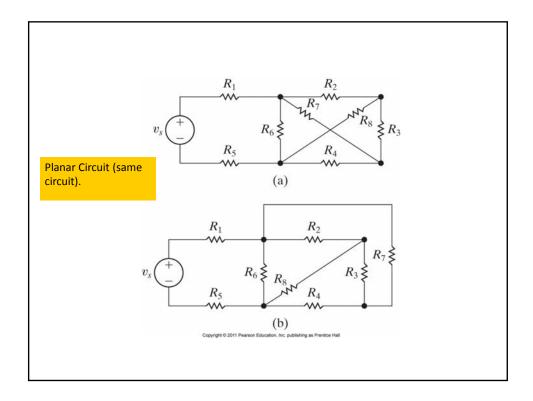
Chapter 4
Techniques for Circuit Analysis

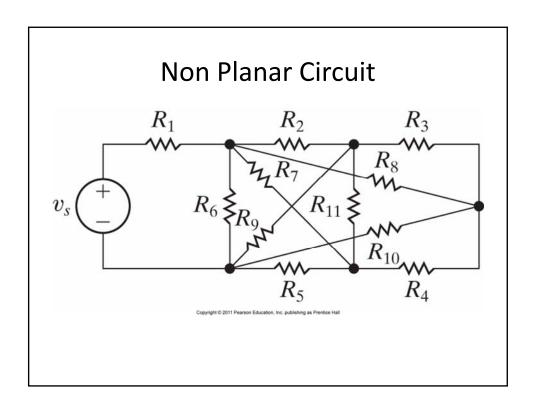
Objectives

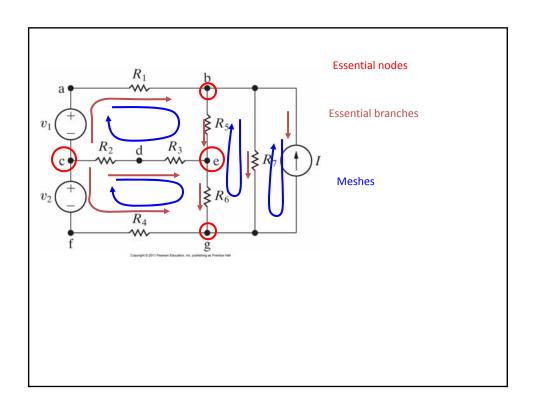
- Understand and being able to use node-voltage and mesh-current methods to solve a circuit.
- Understand source transformation and being able to use it to solve a circuit.
- Understand the concept of Thevenin and Norton equivalent circuits and being able to construct them for any circuit.
- Know the condition for maximum power transfer to a resistive load, and being able to calculate the value of the load resistor that achieves that.

Terminology

- Node: A point that connects two or more circuit elements.
- Essential node: A node where 3 or more circuit elements join.
- Path: A trace of adjoining basic elements with no element included twice.
- Branch: A path that connects two nodes.
- Essential path: A path which connects two essential nodes without passing through an essential node.
- Loop: A path whose last node is the same as the first
- Mesh: A loop that does not enclose any other loops
- Planar circuit: A circuit that could be drawn on a plane with no crossing branches.

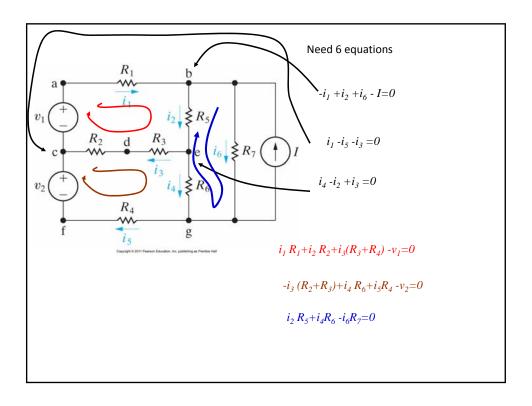






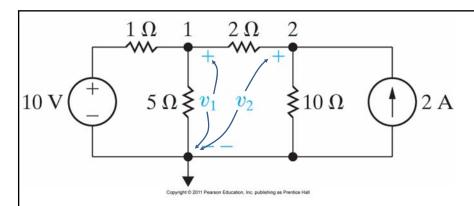
Simultaneous Equations

- In a circuit with b essential branches, and n essential nodes
- Get n-1 equations by applying KCL at n-1 nodes (why not n?)
- Still need *b-n+1* equations to solve for the currents in each essential branch.
- Use KVL on loops or meshes to get the remaining *b-n+1* equations
- Solve them.



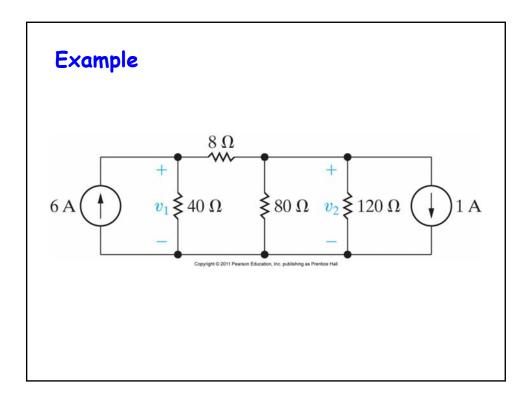
Node-Voltage Method

- Draw the circuit in a neat way
- If the circuit has n essential nodes, we need n-1 equations.
- Select one of the n nodes as a reference node (usually the one with the most branches).
- Define the node voltages for the n-1 nodes (voltage rise from reference to the node).
- Write KCL for the n-1 nodes as a function of the node voltage.



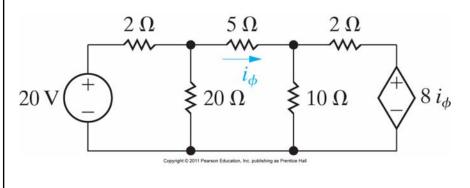
$$\frac{v_1 - 10}{1} + \frac{v_1}{5} + \frac{v_1 - v_2}{2} = 0$$

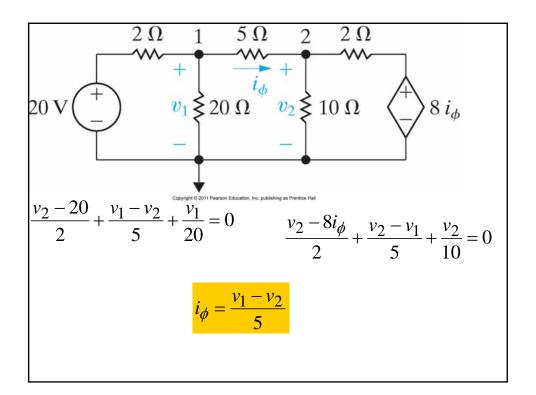
$$\frac{v_2 - v_1}{2} + \frac{v_2}{10} - 2 = 0$$

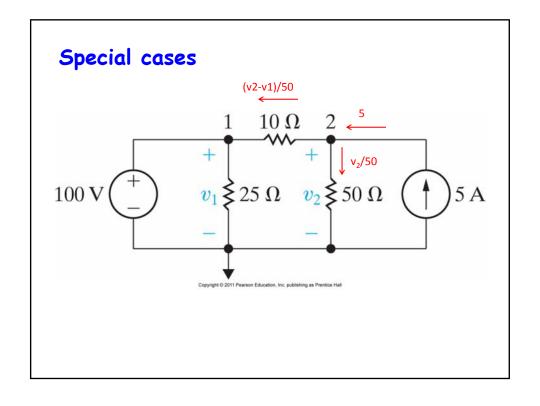


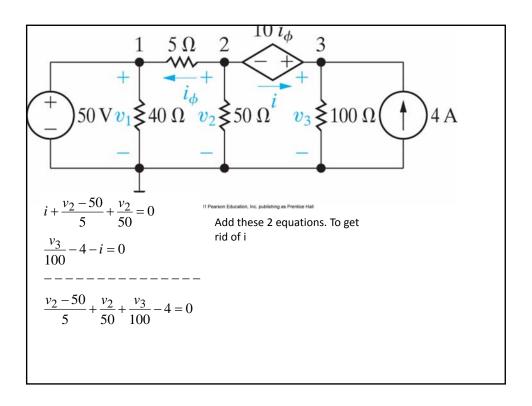
Node-Voltage and Dependent Sources.

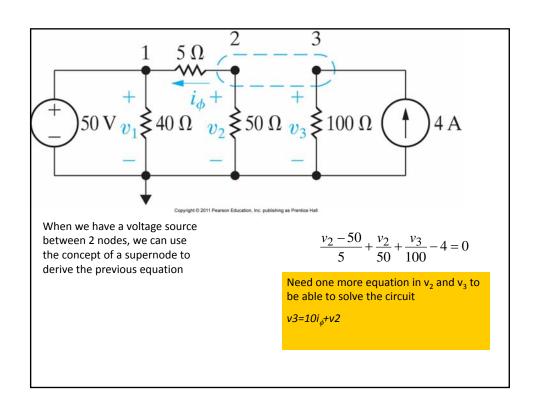
• Another constraint is added by the dependent source

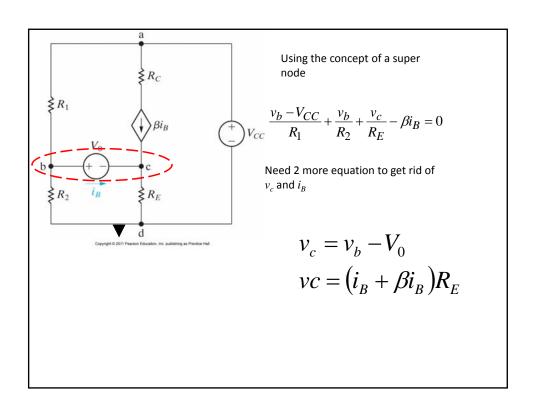


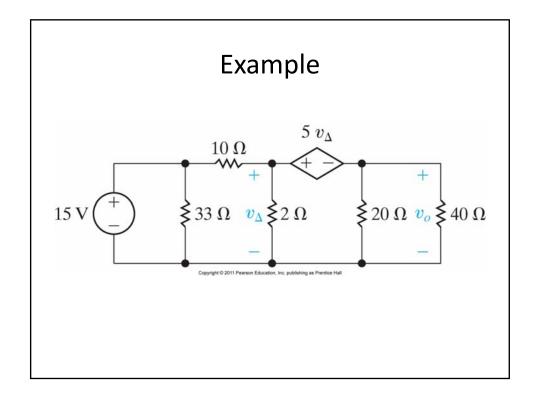


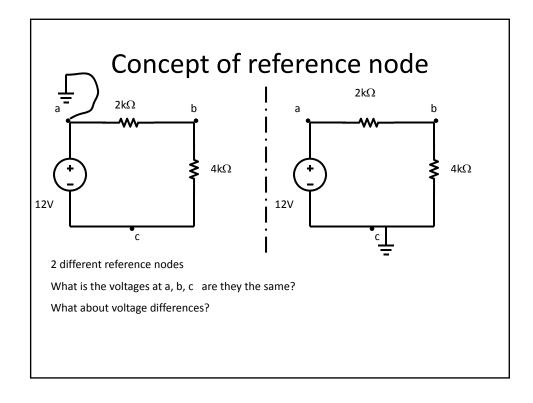






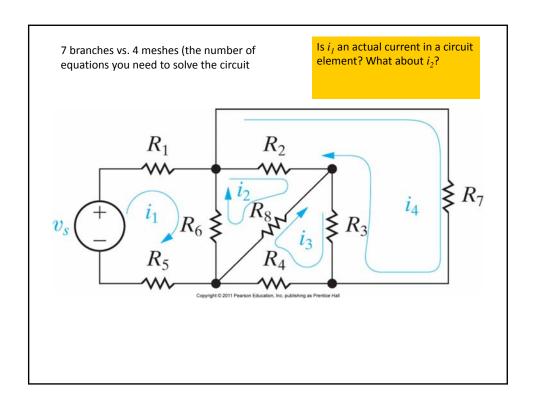


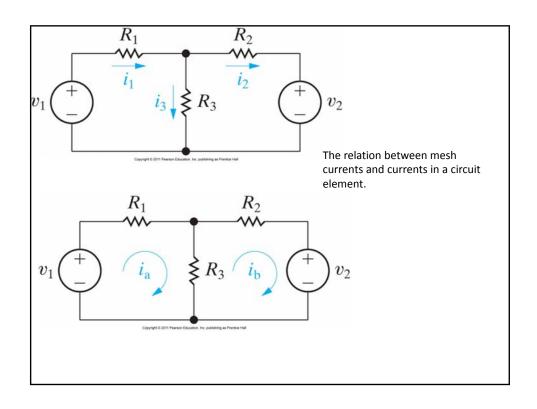


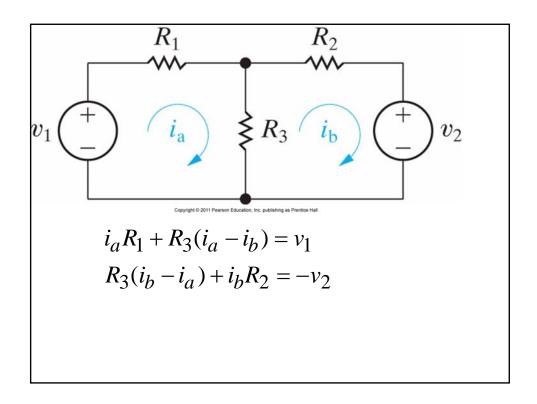


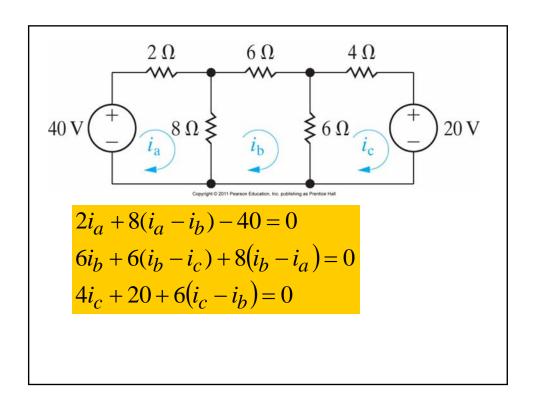
Mesh-Current Method

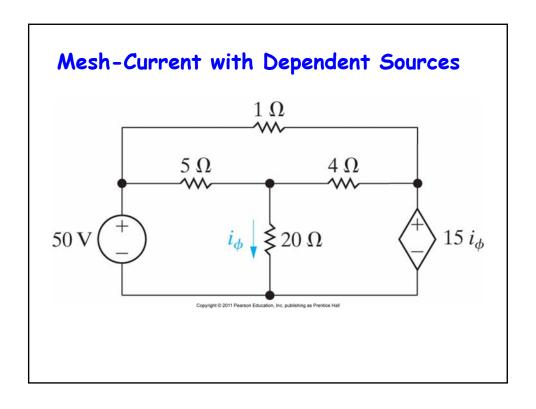
- For planar circuit
- A mesh current is a current that exists only in the perimeter in the mesh
- Mesh current may or may not be an actual current in a circuit element (i₁ and i₂)

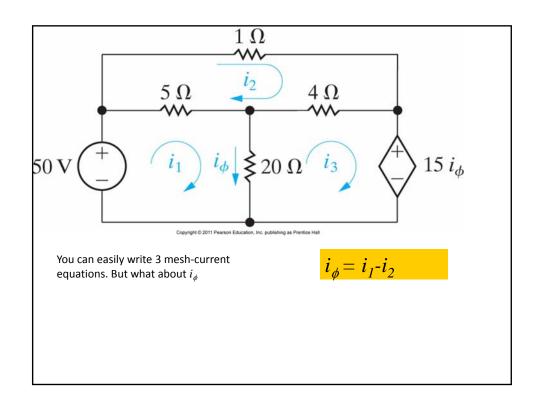


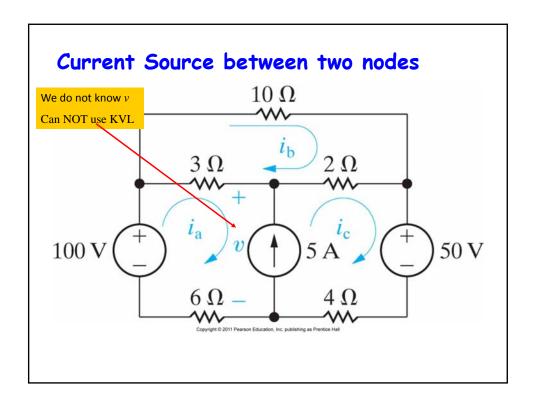


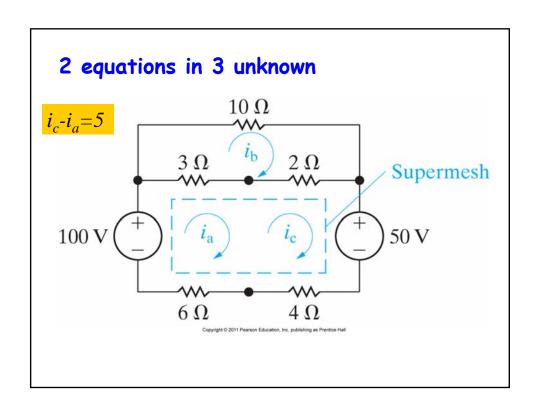


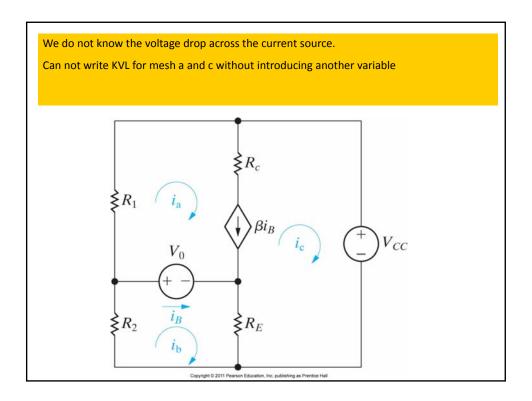


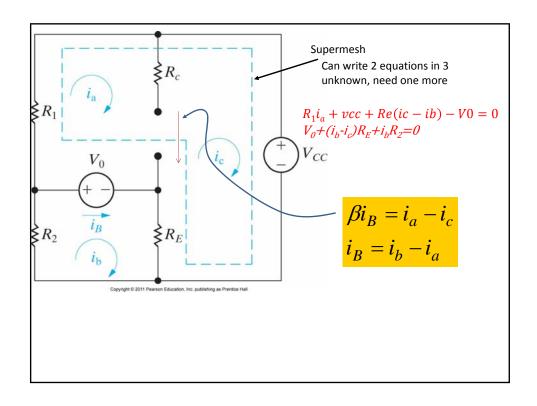






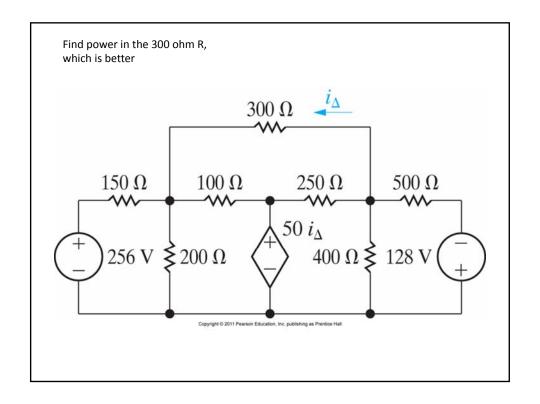


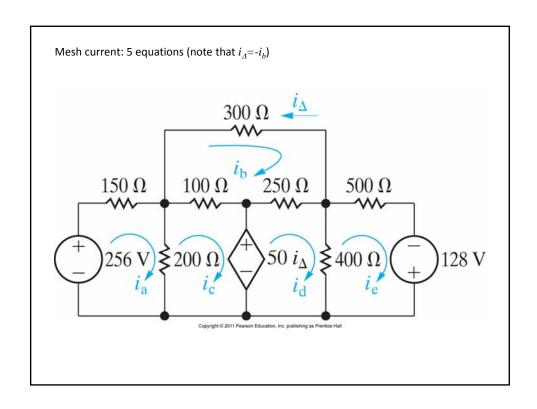


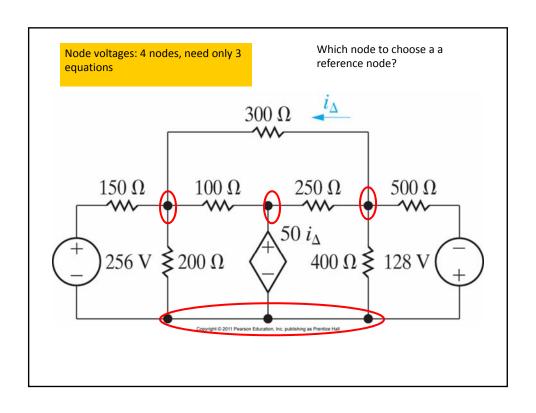


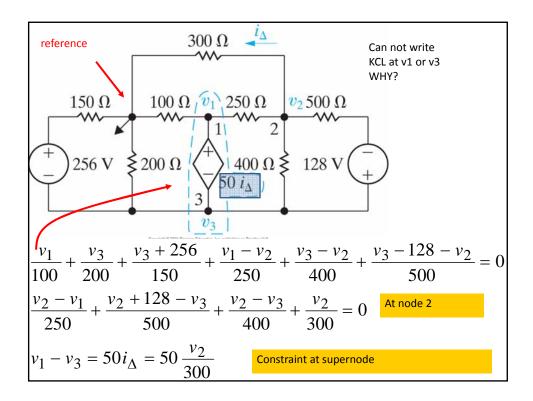
Node-Voltage vs. Mesh Current

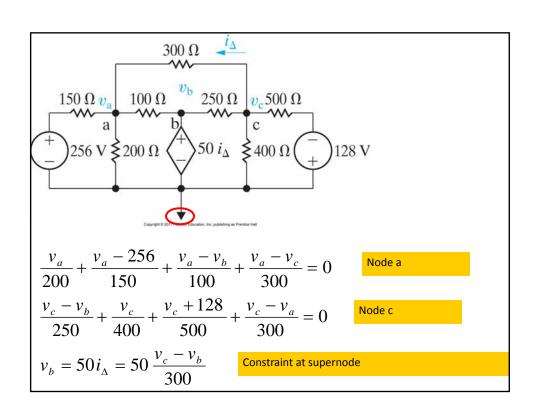
- Which is better (less equations)
- Depnds
 - Number of equations formed for each
 - Any supernode (node voltage)
 - Supermesh? (mesh-current)
 - Do we have to solve for the entire circuit?





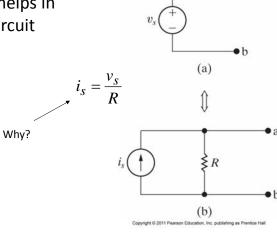


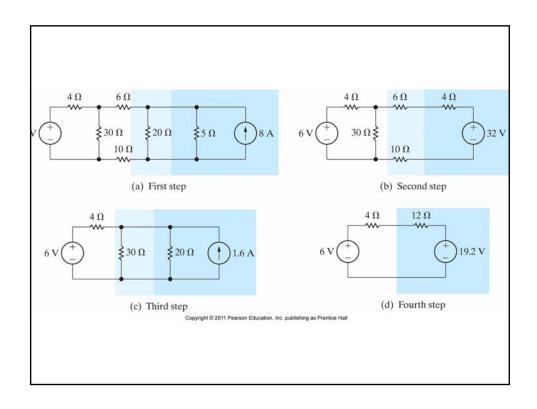


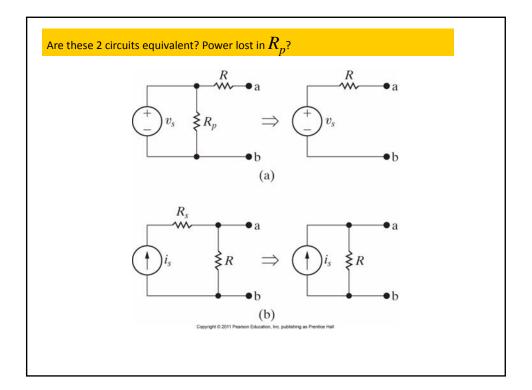


Source Transformation

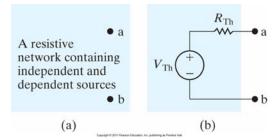
 Some times it helps in reducing the circuit complexity





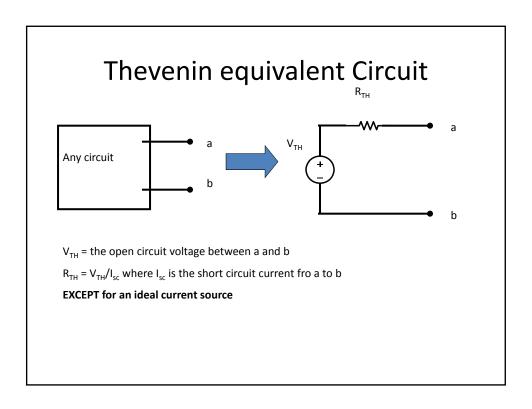


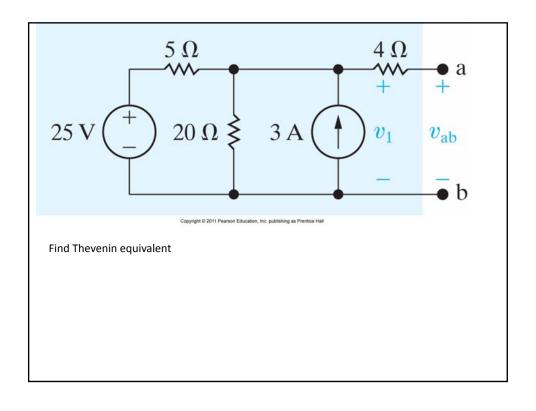
Thevenin Equivalent Circuit

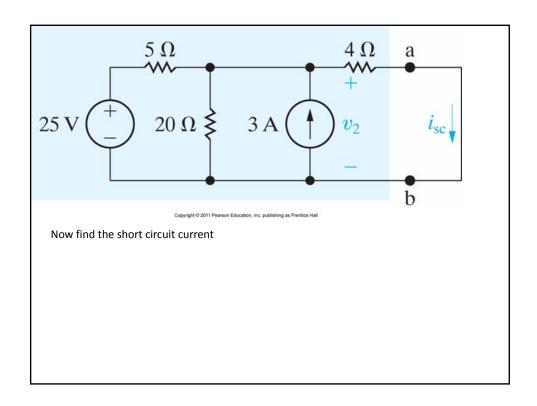


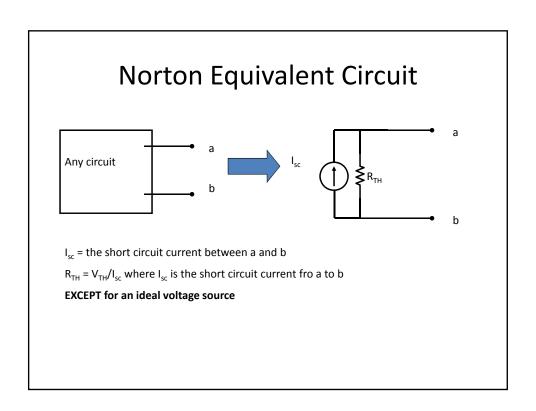
Especially useful when we are interested in the behavior of the circuit between two terminals.

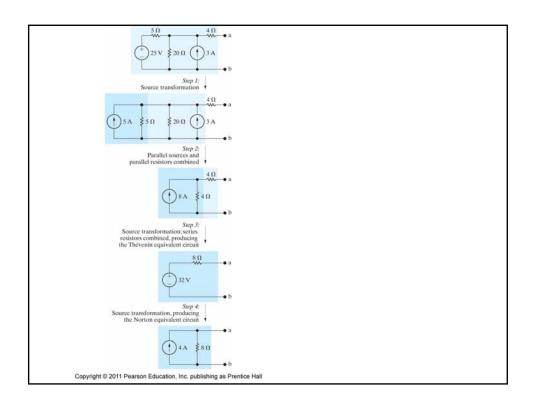
Any resistive network with dependent or independent sources could be represented as a dependent voltage source V_{TH} in series with a resistance R_{TH} .

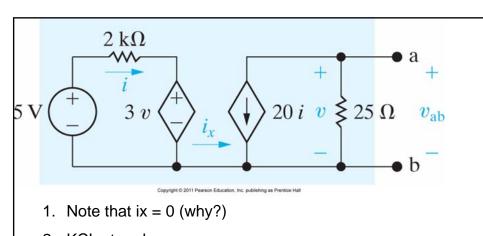




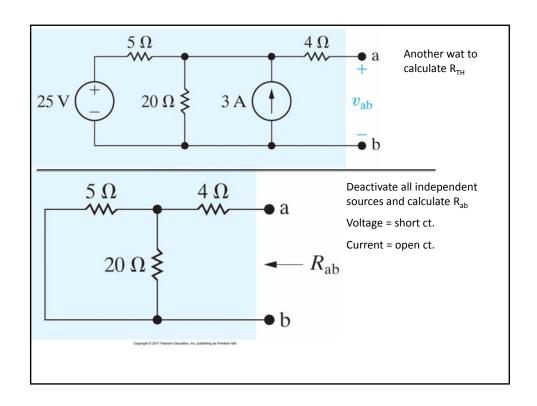


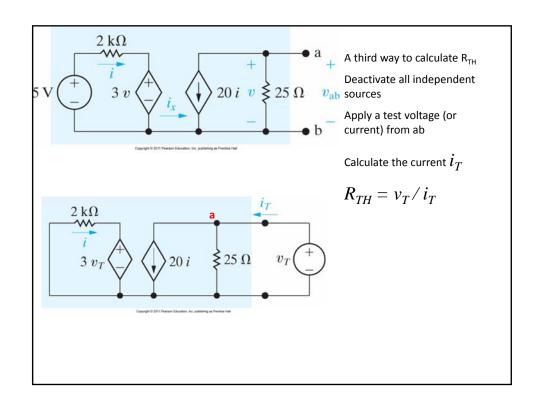


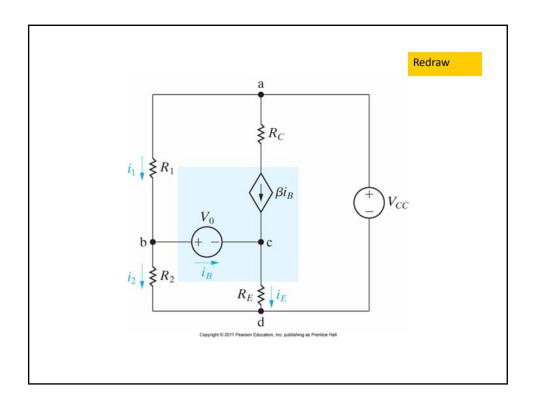


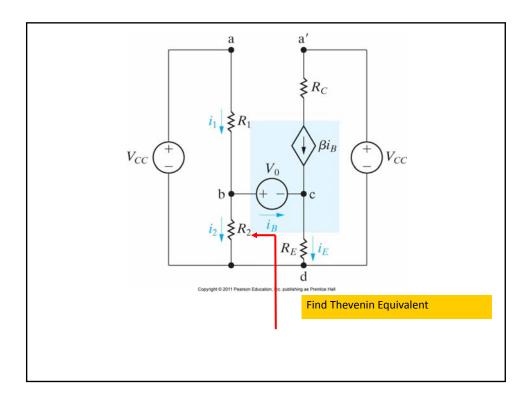


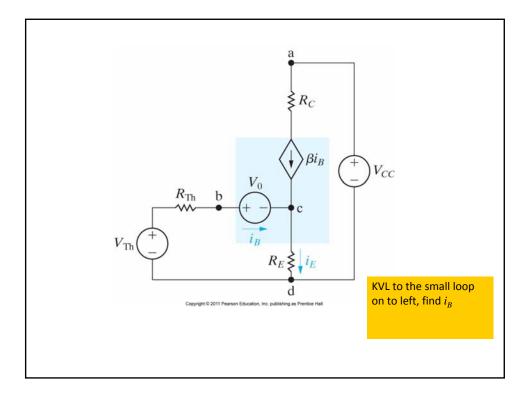
- 2. KCL at node a
- 3. KVL at the loop to the left $\,$ get $v_{ab}=V_{th}$
- 4. Short circuit a and b
- 5. I_{sc} =-20 i, find i from KVL o the left











Maximum Power Transfer

- Assume a voltage source, V with internal resistance R₀ is driving a load R_L
- What is the maximum power R_L can get?
- Calculate $p(R_{\nu}, R_0)$ and differentiate =0
- What if it is not a simple source with an internal resistance?
- Thevenin equivalent

Superposition

 When a linear system is excited by more than one independent source, the total response is the sum of the individual responses where each response is the result of one of the independent sources acting alone.

