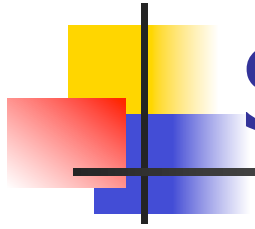




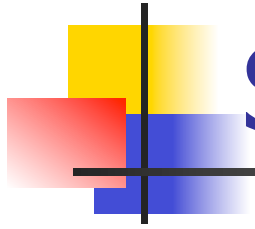
Path Testing + Coverage

Chapter 8



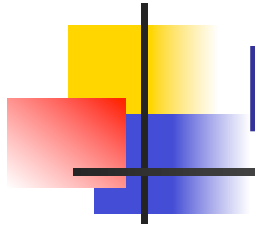
Structural Testing

- Also known as glass/white/open box testing
- A software testing technique whereby explicit knowledge of the internal workings of the item being tested are used to select the test data
- Functional Testing uses program specification
- Structural Testing is based on specific knowledge of the source code to define the test cases and to examine outputs.



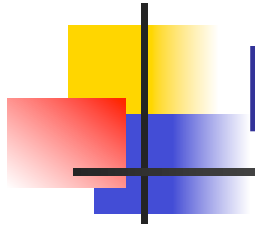
Structural Testing

- Structural testing methods are very amenable to:
 - Rigorous definitions
 - Control flow, data flow, coverage criteria
 - Mathematical analysis
 - Graphs, path analysis
 - Precise measurement
 - Metrics, coverage analysis

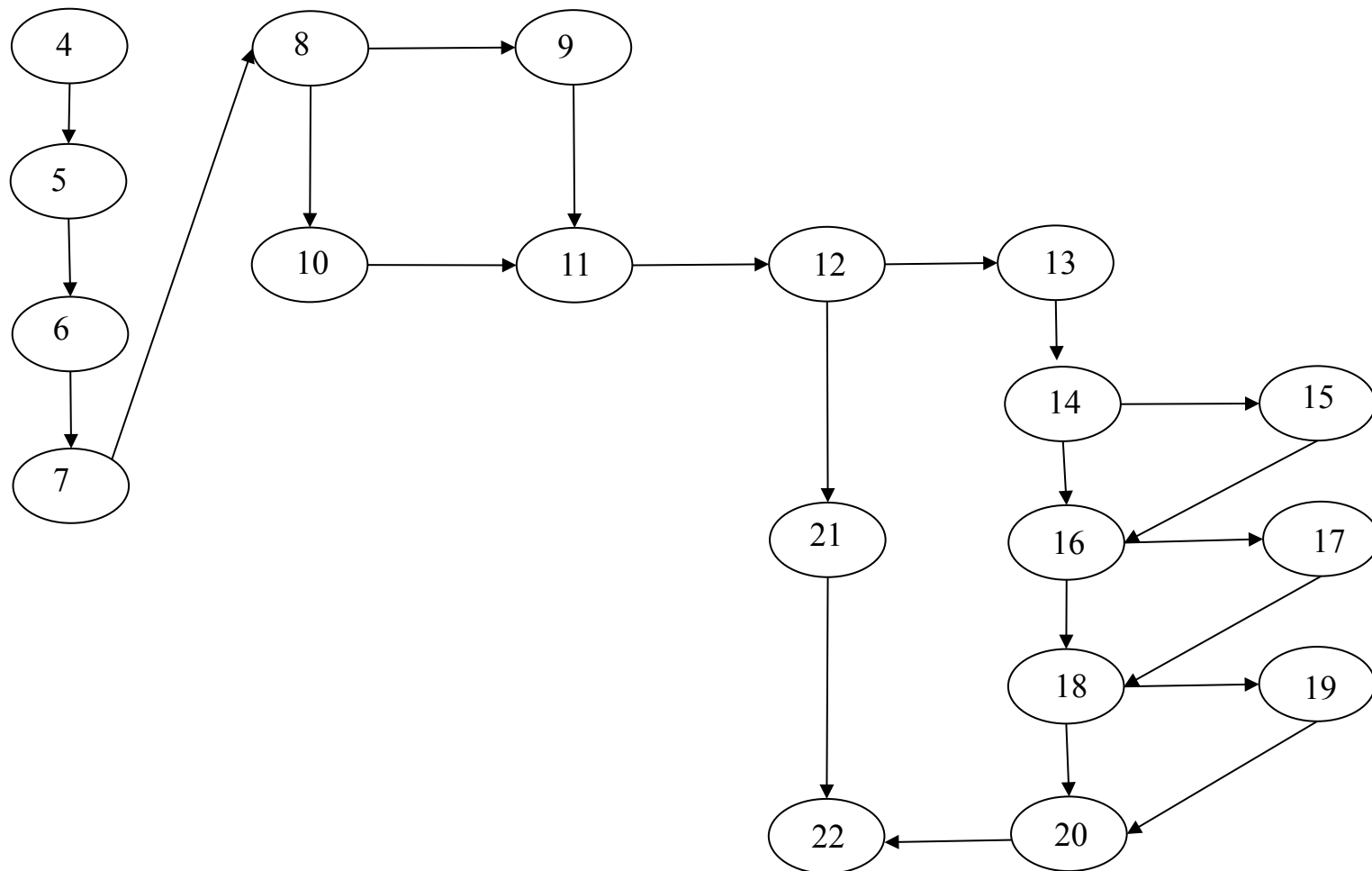


Program Graph - Definition

- Given a program written in an imperative programming language, its **program graph** is a directed graph in which nodes are statement fragments, and edges represent flow of control
- A complete statement is also considered a statement fragment



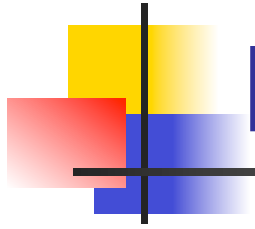
Program Graph - Example





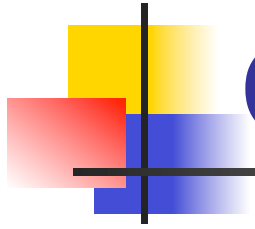
DD-Path

- A decision-to-decision path (DD-Path) is a chain in a program graph such that:
 - Case1: it consists of a single node with $\text{indeg}=0$
 - Case2: it consists of a single node with $\text{outdeg}=0$
 - Case3: it consists of a single node with $\text{indeg} \geq 2$ or $\text{outdeg} \geq 2$
 - Case4: it consists of a single node with $\text{indeg} = 1$, and $\text{outdeg} = 1$
 - Case5: it is a maximal chain of length ≥ 1
- DD-Paths are also known as **segments**



DD-Path Graph

- Given a program written in an imperative language, its **DD-Path graph** is a directed graph, in which nodes are DD-Paths of its program graph, and edges represent control flow between successor DD-Paths.
- Also known as **Control Flow Graph**



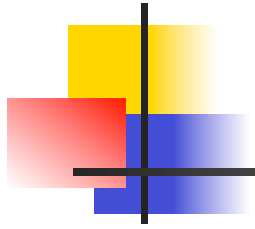
Control Flow Graph Derivation

- Straightforward process
- Some judgement is required
- The last statement in a segment must be a predicate, a loop control, a break, or a method exit
- Let's try an example...

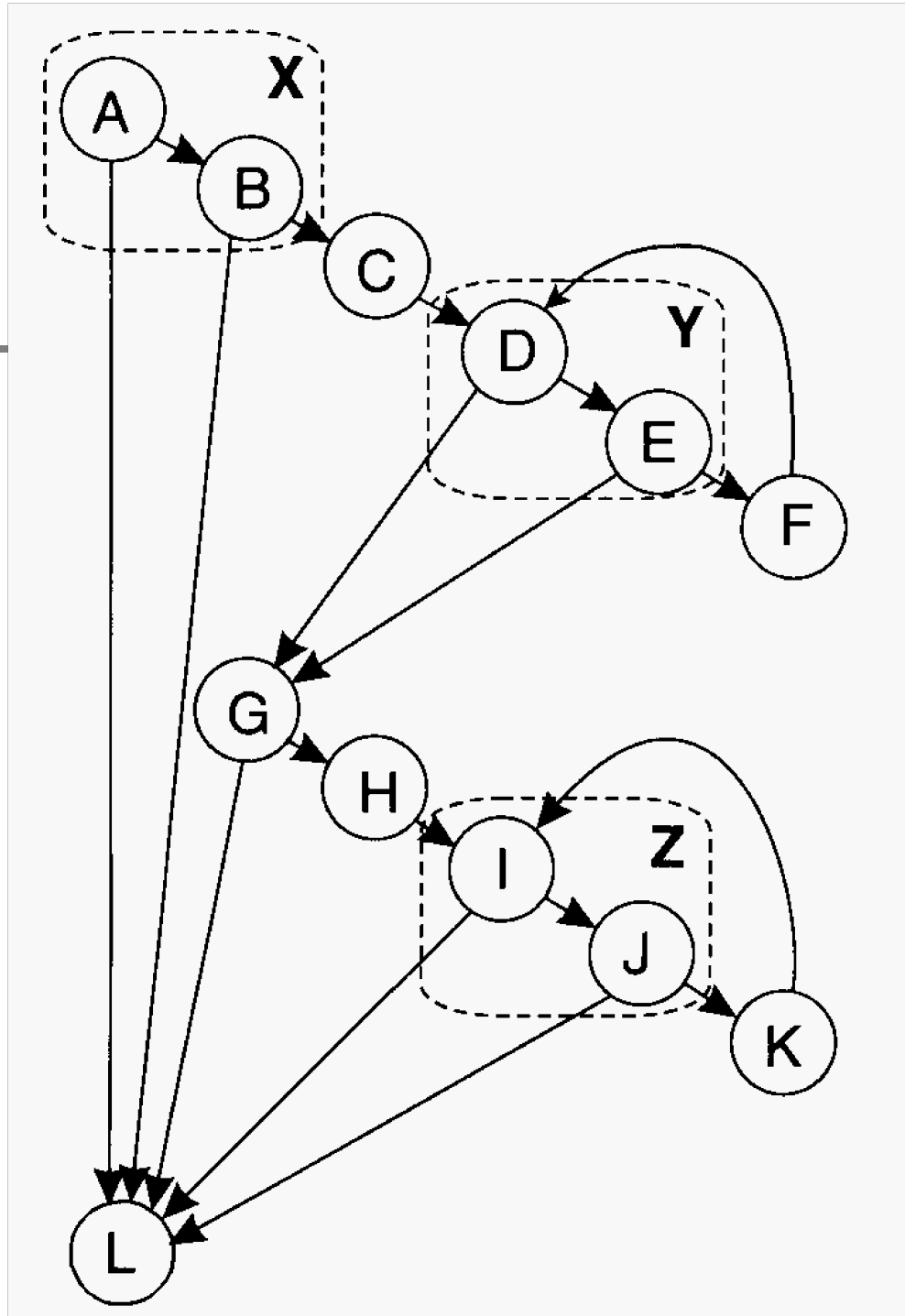

```

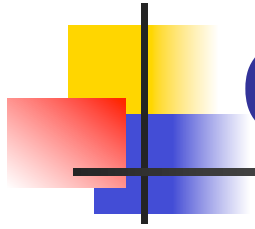
public int displayLastMsg(int nToPrint) {
    np = 0;
    if ((msgCounter > 0) && (nToPrint > 0)) {
        for (int j = lastMsg; ((j != 0) && (np < nToPrint)); --j) {
            System.out.println(messageBuffer[j]);
            ++np;
        }
        if (np < nToPrint) {
            for (int j = SIZE; ((j != 0) && (np < nToPrint)); --j) {
                System.out.println(messageBuffer[j]);
                ++np;
            }
        }
    }
    return np;
}

```



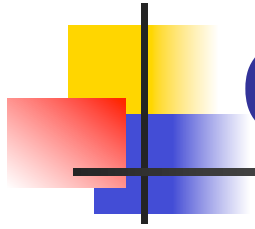
Control flow graph for previous slide





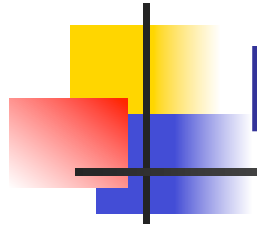
Control flow graphs

- Depict which program segments may be followed by others
- A segment is a node in the CFG
- A conditional transfer of control is a **branch** represented by an edge
- An **entry node** (no inbound edges) represents the entry point to a method
- An **exit node** (no outbound edges) represents an exit point of a method



Control flow graphs

- An **entry-exit path** is a path from the entry node to the exit node
- **Path expressions** represent paths as sequences of nodes
- Loops are represented as segments within parentheses followed by an asterisk
 - Example: ABC(DEF)*DGL
- How many path expressions in this example?



Example path expressions

AL

ABL

ABCDGL

ABCDEGL

ABC(DEF)*DGL

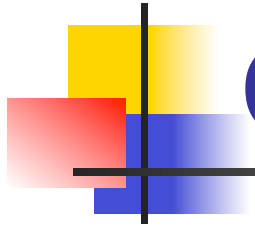
ABC(DEF)*DEGL

ABCDGHIL

ABCDGHIJL

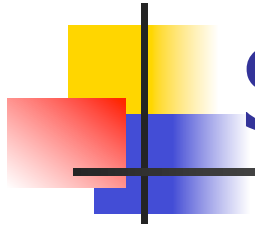
ABCDGH(IJK)*IL

ABC(DEF)*DEGH(IJK)*IJL



Code coverage models

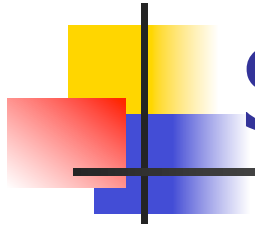
- Statement Coverage
- Segment Coverage
- Branch Coverage
- Multiple-Condition Coverage



Statement coverage

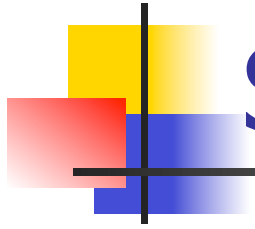
- Achieved when all statements in a method have been executed at least once
- How many test cases do we need to achieve statement coverage in our example?
- A test case that will follow the path expression below will achieve statement coverage

ABC(DEF)*DGH(IJK)*IL



Segment coverage

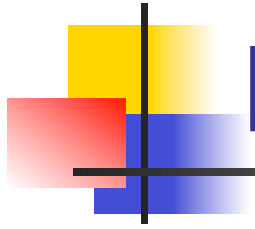
- **Segment coverage** counts segments rather than statements
- May produce drastically different numbers
 - Assume two segments P and Q
 - P has one statement, Q has nine
 - Exercising only one of the segments will give 10% or 90% statement coverage
 - Segment coverage will be 50% in both cases



Statement coverage problems

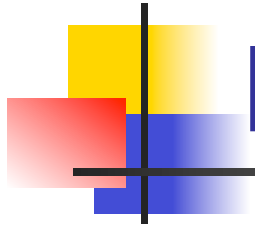
- Predicate may be tested for only one value (misses many bugs)
- Loop bodies may only be iterated once
- Statement coverage can be achieved without branch coverage. Important cases may be missed

```
String s = null;  
if (x != y) s = "Hi";  
String s2 = s.substring(1);
```



Branch coverage

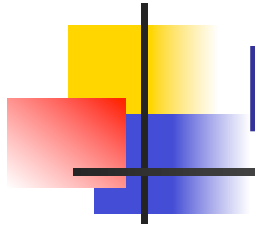
- Achieved when every branch from a node is executed at least once
- At least one true and one false evaluation for each predicate
- Can be achieved with $D+1$ paths in a control flow graph with D 2-way branching nodes and no loops
 - Even less if there are loops



Branch coverage problems

- Short-circuit evaluation means that many predicates might not be evaluated
- A compound predicate is treated as a single statement. If n clauses, 2^n combinations, but only 2 are tested
- Only a subset of all entry-exit paths is tested

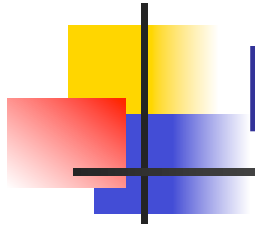
```
if (a == b) x++;  
if (c == d) x--;
```



Multiple-condition coverage

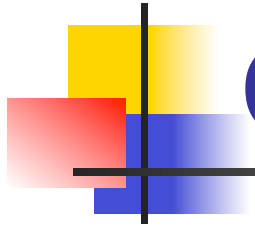
- All true-false combinations of simple conditions in compound predicates are considered at least once
- A truth table may be necessary
- Not necessarily achievable due to lazy evaluation or mutually exclusive conditions

```
if ( (x > 0) && (x < 5) ) ...
```



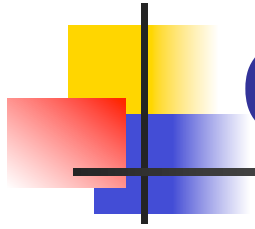
Dealing with Loops

- Loops are highly fault-prone, so they need to be tested carefully
- Simple view: Every loop involves a decision to traverse the loop or not
- A bit better: Boundary value analysis on the index variable
- Nested loops have to be tested separately starting with the innermost



Creating test cases

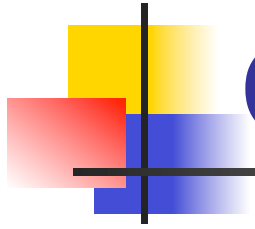
- In order to increase the coverage of a test suite, one needs to generate test cases that exercise certain statements or follow a specific path
- This is not always easy to do...



CFG question

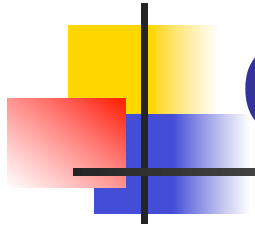
- What is the control flow graph for the following?

if $a < b$ then $c = a + b$; $d = a * b$
else $c = a * b$; $d = a + b$
if $c < d$ then $x = a + c$; $y = b + d$
else $x = a * c$; $y = b * d$



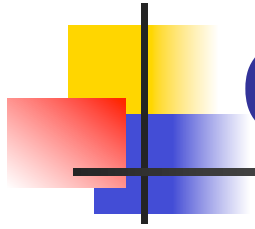
Creating a test case

- **What is the key question that needs to be answered to be able to create a test for a path?**



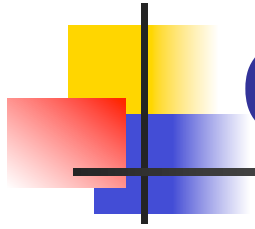
Creating a test case

- **What is the key question that needs to be answered to be able to create a test for a path?**
 - How to make the path execute, if possible.
 - Generate input data that satisfies all the conditions on the path.



Creating a test case

- **What are the key items you need to generate a test case for a path?**



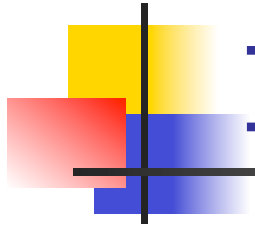
Creating a test case

- **What are the key items you need to generate a test case for a path?**
 - Input vector
 - Predicate
 - Path predicate
 - Predicate interpretation
 - Path predicate expression
 - Create test input from path predicate expression



Input Vector

- **What is an input vector?**



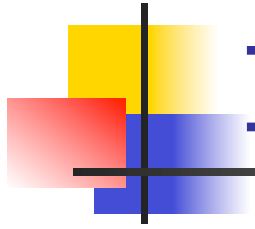
Input Vector – 2

- **What is an input vector?**
 - A collection of all data entities read by the routine whose values must be fixed prior to entering the routine.



Input Vector – 3

- **What are the members of an input vector?**



Input Vector – 4

- **What are the members of an input vector?**
 - Input arguments to the routine
 - Global variables and constants
 - Files
 - Network connections
 - Timers



Predicate

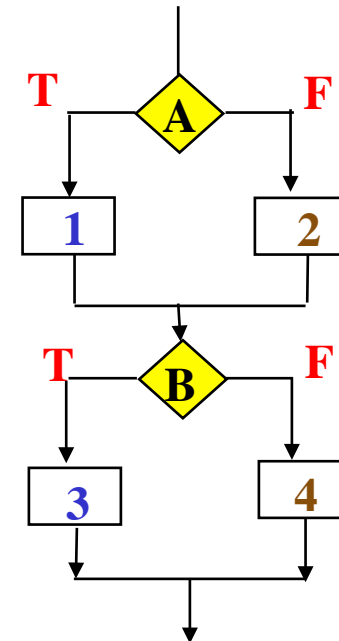
- **What is a predicate?**

Predicate – 2

■ What is a predicate?

- A logical function evaluated at a decision point.
 - In the following each of $a < b$ and $c < d$ are predicates

if $a < b$ then $c = a + b$; $d = a * b$
else $c = a * b$; $d = a + b$
if $c < d$ then $x = a + c$; $y = b + d$
else $x = a * c$; $y = b * d$





Path predicate

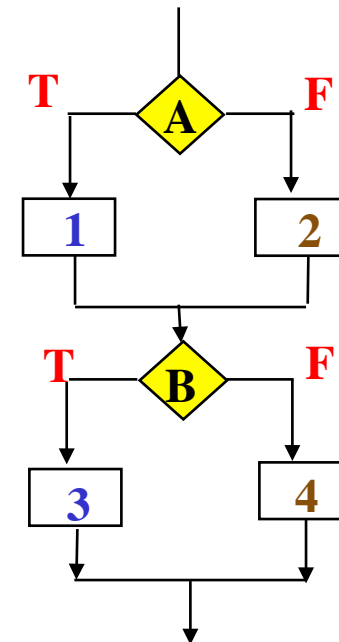
- **What is a path predicate?**

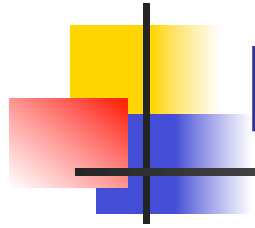
Path predicate – 2

- The set of predicates associated with a path.

■ $a < b = \text{true} \wedge c < d = \text{false}$
is a path predicate

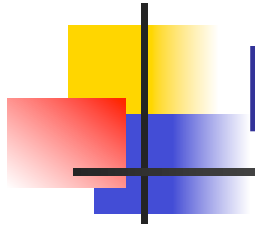
if $a < b$ then $c = a + b$; $d = a * b$
else $c = a * b$; $d = a + b$
if $c < d$ then $x = a + c$; $y = b + d$
else $x = a * c$; $y = b * d$





Path Predicate Expression

- **What is a path predicate expression?**



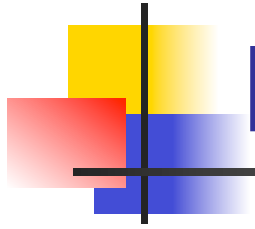
Path Predicate Expression – 2

- **What is a path predicate expression?**
 - An interpreted path predicate



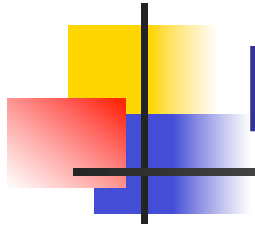
Predicate Interpretation

- **What is a path predicate interpretation?**



Predicate Interpretation – 2

- **What is a path predicate interpretation?**
 - A path predicate may contain local variables.
 - Local variables cannot be selected independently of the input variables
 - Local variables are eliminated with **symbolic execution**



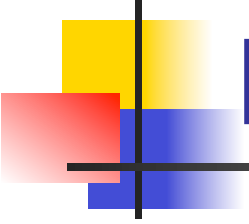
Predicate Interpretation – 3

- **What is symbolic execution?**
 - Symbolically substituting operations along a path in order to express the predicate solely in terms of the input vector and a constant vector.
 - A predicate may have different interpretations depending on how control reaches the predicate.



Attributes of a Path Predicate Expression

- **What are the attributes of a path predicate expression?**



Attributes of a Path Predicate Expression – 2

- **What are the attributes of a path predicate expression?**
 - No local variables
 - A set of constraints in terms of the input vector, and, maybe, constants
 - Path forcing inputs are generated by solving the constraints
 - If a path predicate expression has no solution, the path is infeasible



Path Predicate Generating Input Values

**if $a < b$ then $c = a + b$; $d = a * b$
 else $c = a * b$; $d = a + b$
**if $c < d$ then $x = a + c$; $y = b + d$
 else $x = a * c$; $y = b * d$****

- Path predicate **$a < b = \text{true} \wedge c < d = \text{false}$**
- Substitute for c and d **$c = a + b$ $d = a * b$**

$a < b = \text{true} \wedge a + b < a * b = \text{false}$

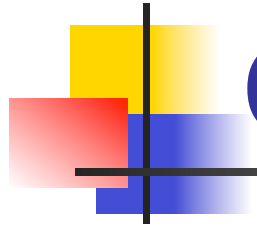
$\rightarrow a < b \wedge a + b \geq a * b$



Path Predicate Generating Input Values – 2

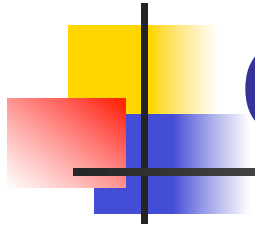
$$a < b \wedge a + b \geq a * b$$

- Solve for a and b $a = 0 \wedge b = 1$
 - Solutions are not unique
- A solution exists
 - We have a feasible path
- No solution to the constraints
 - Have an infeasible path



Organizing path predicates

- **How can we organize the set of path predicates?**



Organizing path predicates – 2

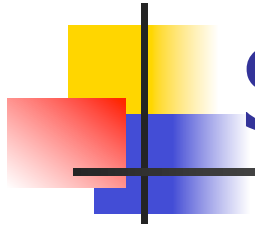
- **How can we organize the set of path predicates?**
 - Use a decision table
 - **How would a decision table be used?**



Decision table for the example

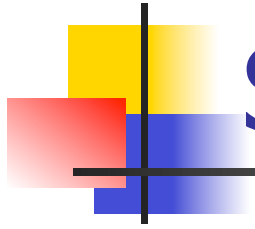
	A1B3	A1B4	A2B3	A2B4
A < B	T	T	F	F
C < D	T	F	T	F
A value	2	0	1	5
B value	5	1	0	2

Paths **A1B3** and **A2B4** give statement coverage
or Paths **A1B4** and **A2B3** give statement coverage



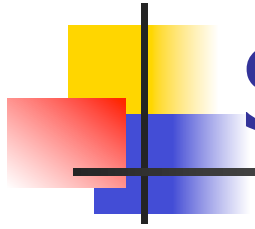
Selecting paths

- A program unit may contain a large number of paths.
 - Path selection becomes a problem
 - Some selected paths may be infeasible
- **What strategy would you use to select paths?**



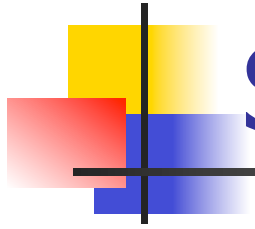
Selecting paths – 2

- **What strategy would you use to select paths?**
 - Select as many short paths as possible
 - Tradeoffs?
 - Choose longer paths
 - Tradeoffs?



Selecting paths – 3

- **What about infeasible paths?**
 - What would you do about them?



Selecting paths – 4

- **What about infeasible paths?**
 - What would you do about them?
 - Make an effort to write program text with fewer or no infeasible paths.