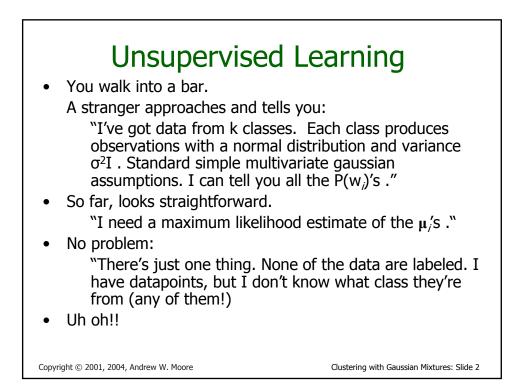
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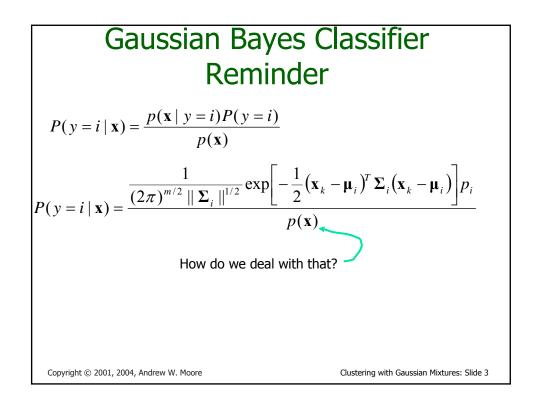
Clustering with Gaussian Mixtures

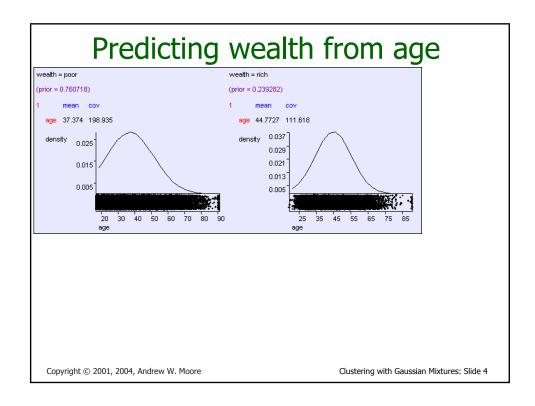
Andrew W. Moore Professor School of Computer Science Carnegie Mellon University www.cs.cmu.edu/~awm

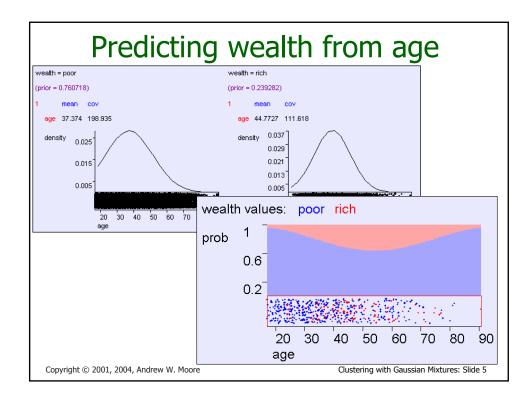
awm@cs.cmu.edu 412-268-7599

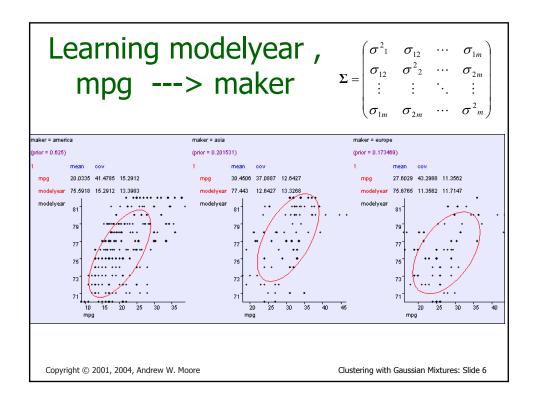
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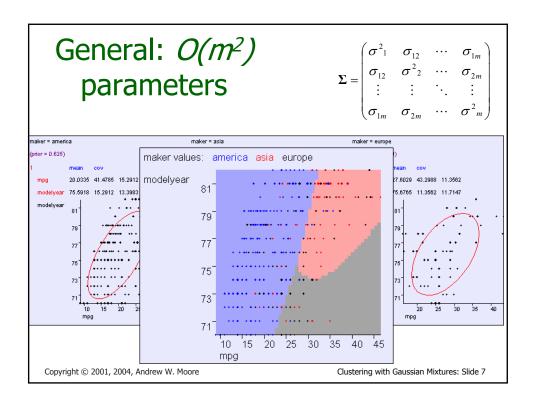


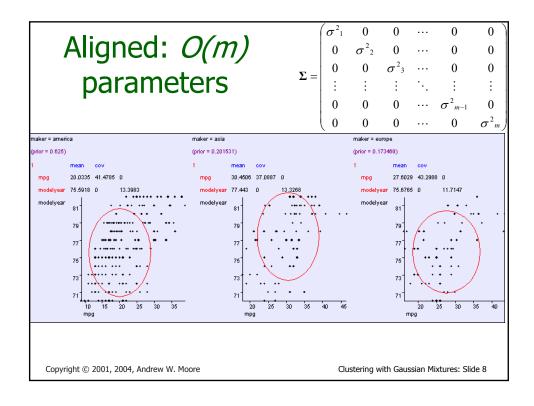


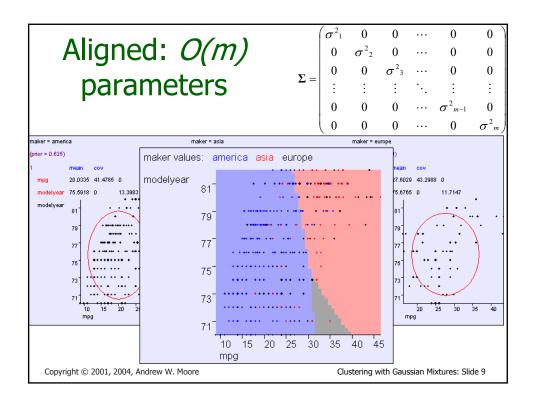


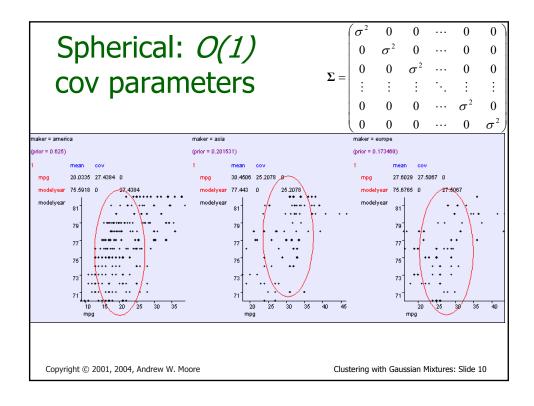


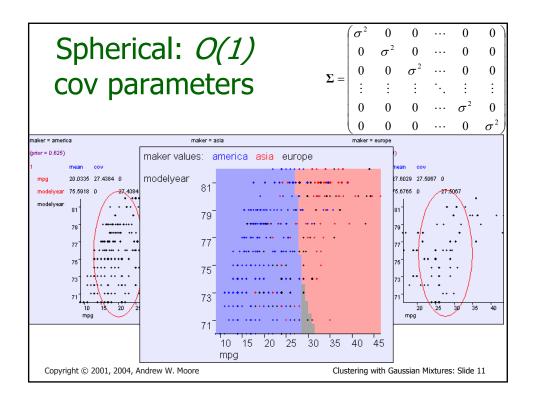


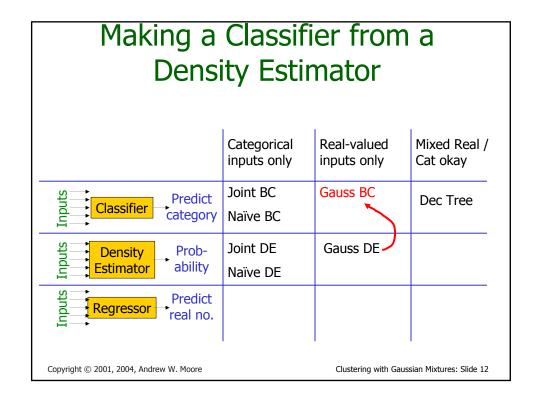


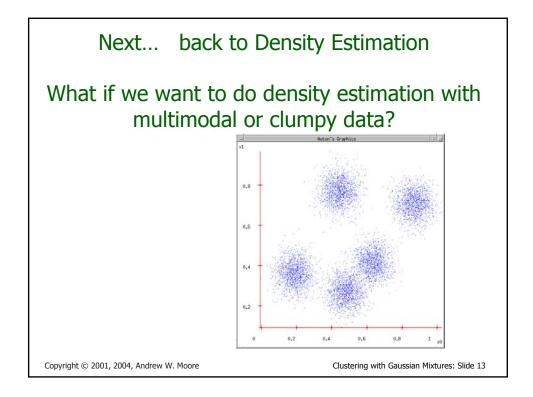


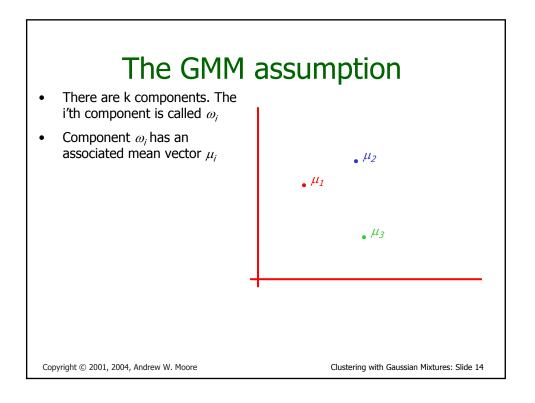


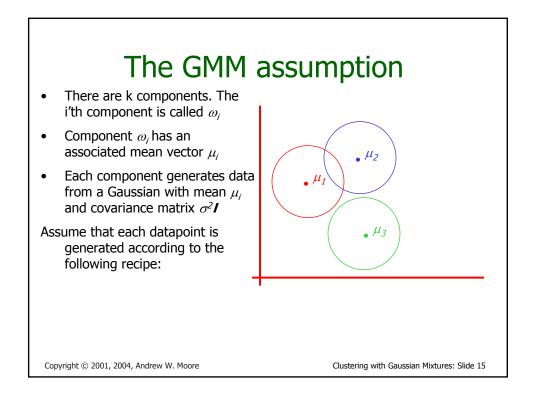


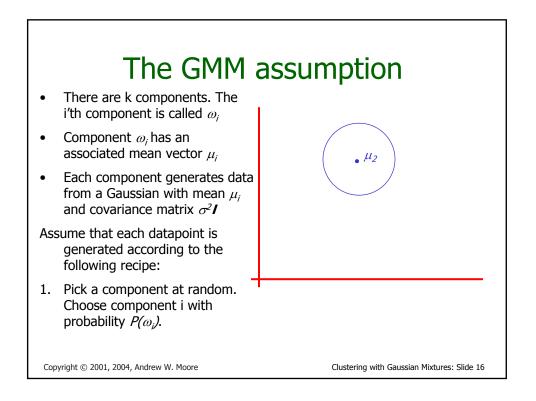


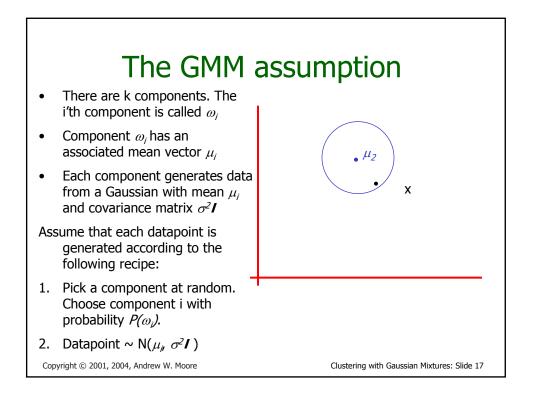


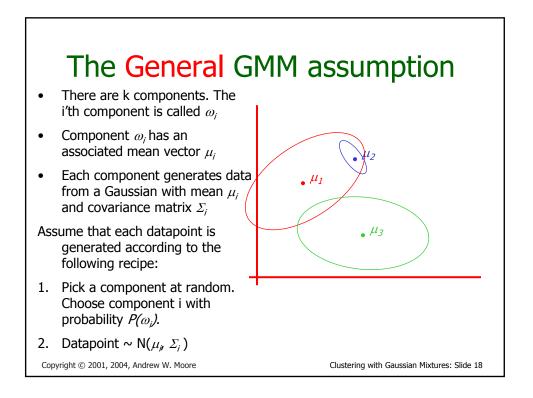


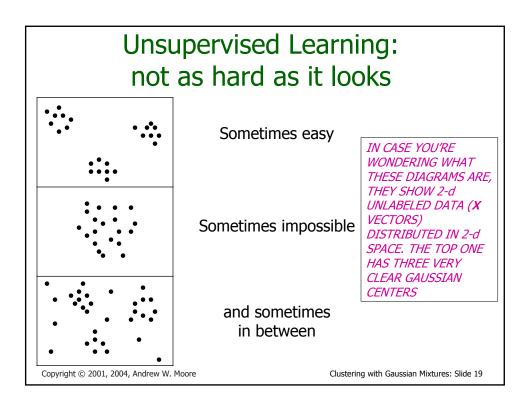


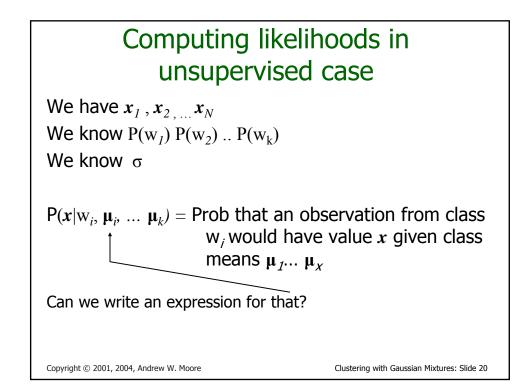












likelihoods in unsupervised case

We have $x_1 x_2 \dots x_n$ We have $P(w_1) \dots P(w_k)$. We have σ . We can define, for any x, $P(x|w_i, \mu_j, \mu_2 \dots \mu_k)$

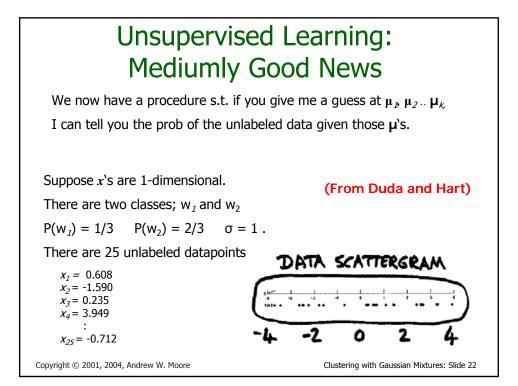
Can we define $P(x \mid \mu_{\mathcal{D}}, \mu_{\mathcal{D}}, \mu_k)$?

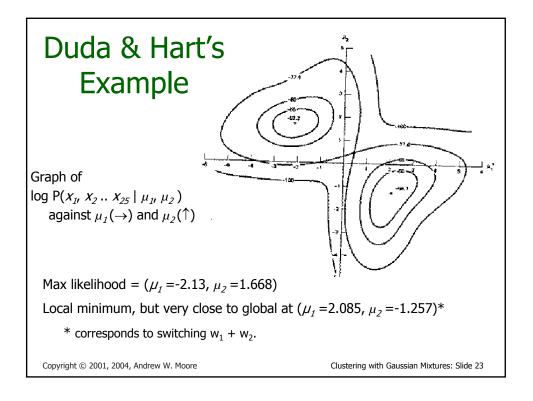
Can we define $P(x_1, x_1, \dots, x_n \mid \mu_{\mathcal{B}} \mid \mu_2 \dots \mid \mu_k)$?

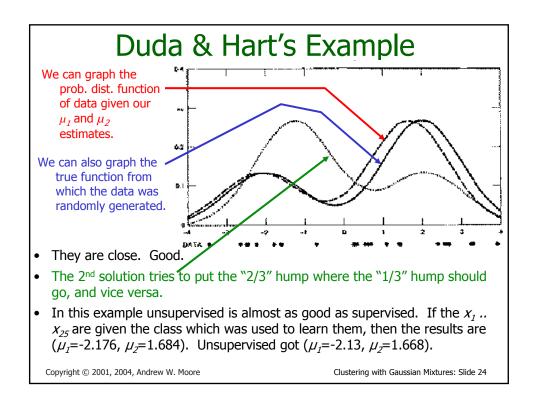
[YES, IF WE ASSUME THE X_1 'S WERE DRAWN INDEPENDENTLY]

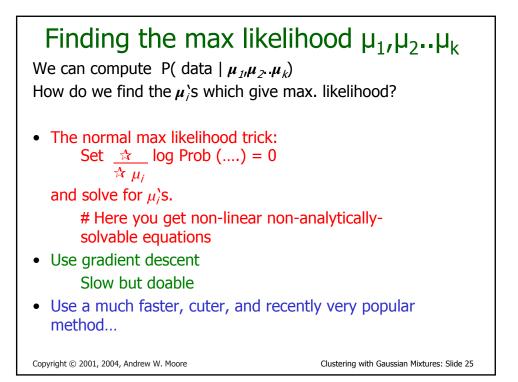
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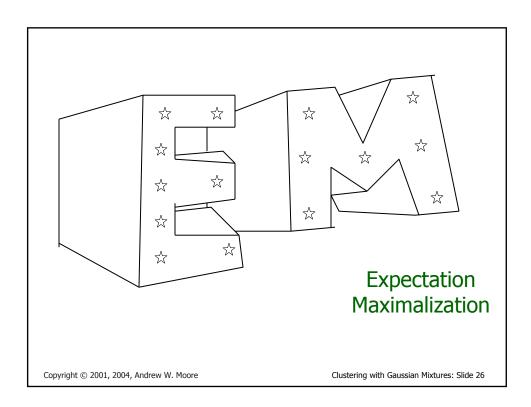
Clustering with Gaussian Mixtures: Slide 21

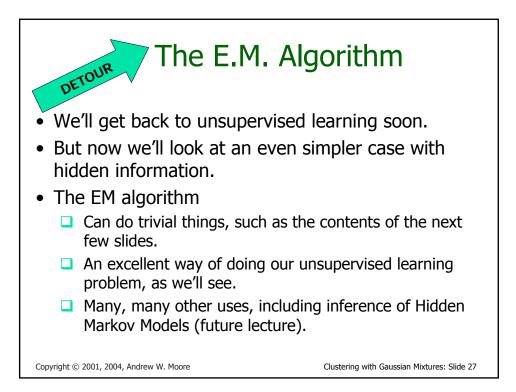


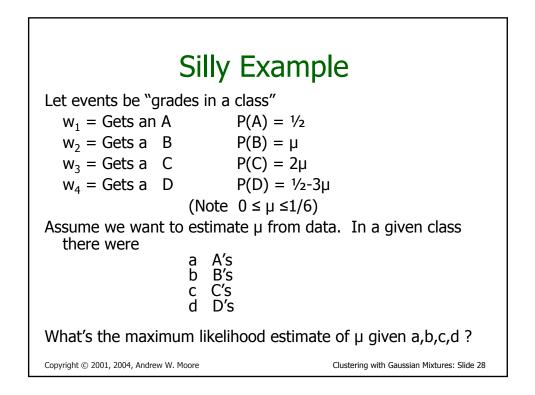


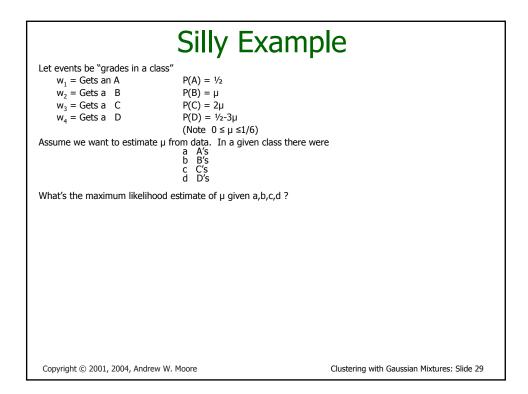


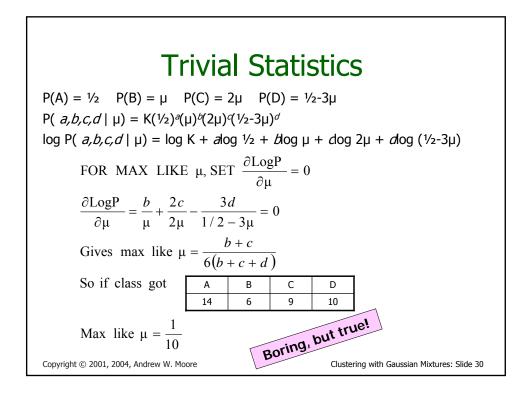


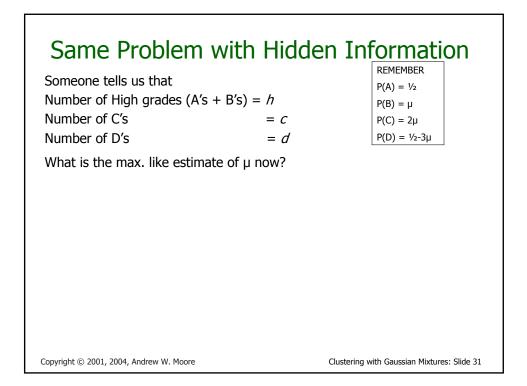


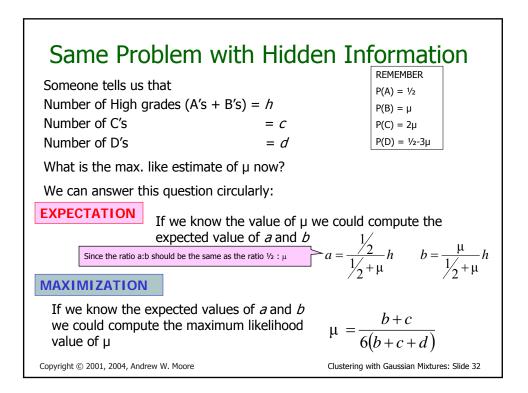


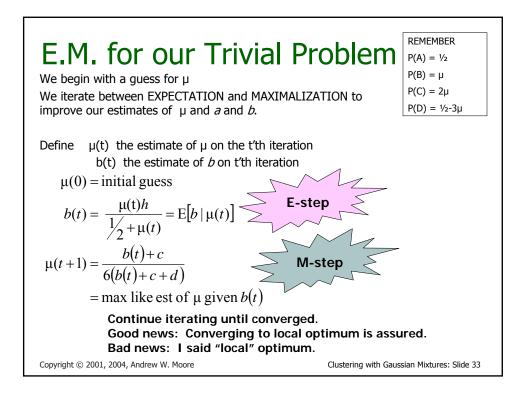




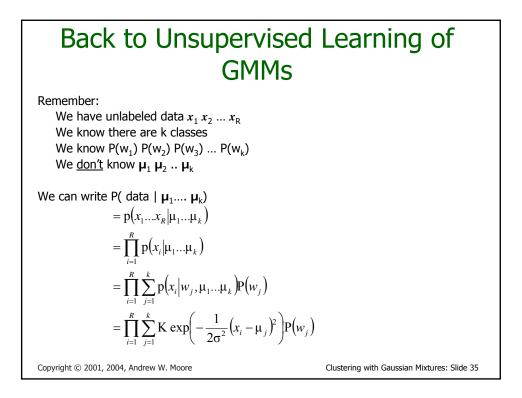


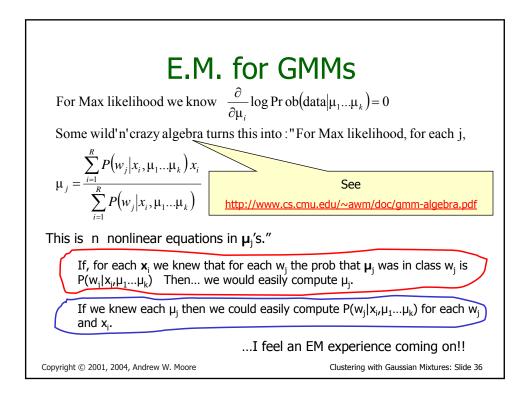


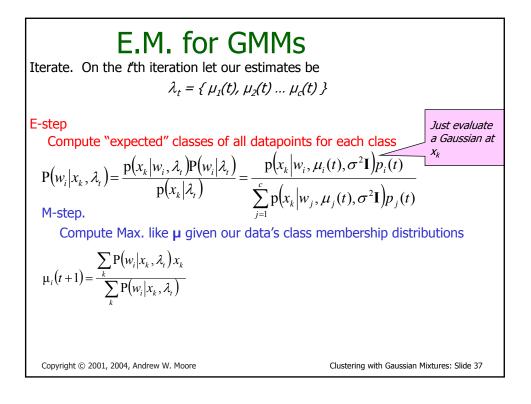


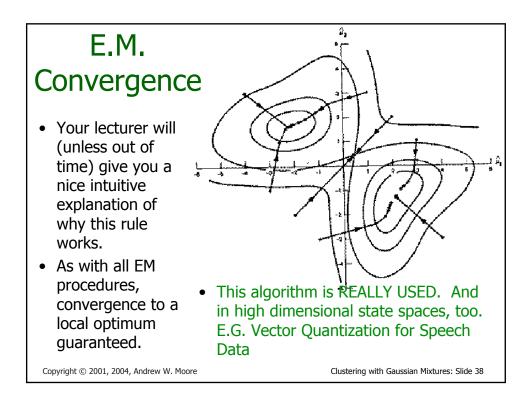


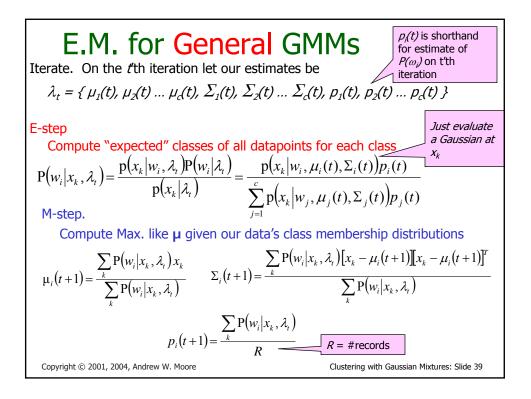
| E.M. Convergence | | | | |
|---|----|---|-------|--|
| Convergence proof based on fact that Prob(data µ) must increase or remain same between each iteration [NOT OBVIOUS] But it can never exceed 1 [OBVIOUS] So it must therefore converge [OBVIOUS] | | | | |
| In our example, | t | μ(t) | b(t) | |
| suppose we had | 0 | 0 | 0 | |
| h = 20 | 1 | 0.0833 | 2.857 | |
| $\begin{array}{c} c = 10 \\ d = 10 \end{array}$ | 2 | 0.0937 | 3.158 | |
| $\mu(0) = 0$ | 3 | 0.0947 | 3.185 | |
| | 4 | 0.0948 | 3.187 | |
| Convergence is generally <u>linear</u> : error decreases by a constant factor each time | 5 | 0.0948 | 3.187 | |
| step. | 6 | 0.0948 | 3.187 | |
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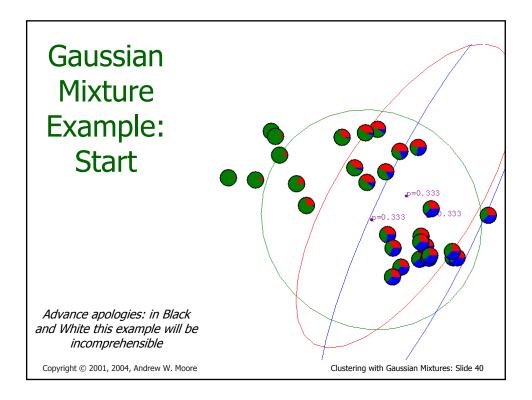


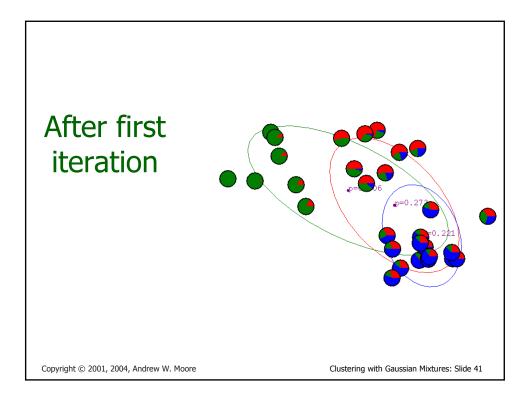


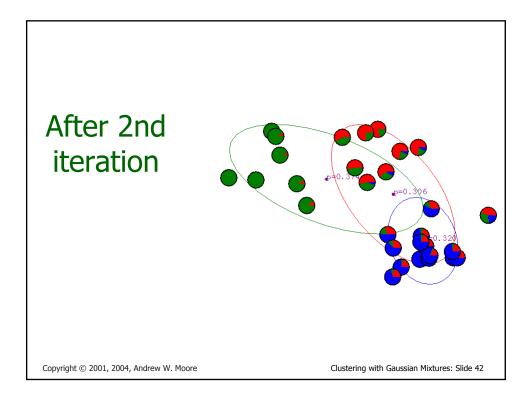


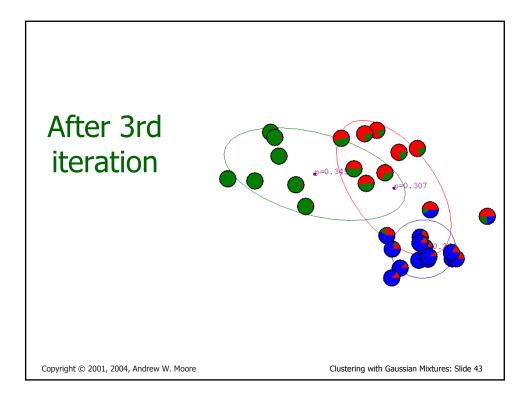


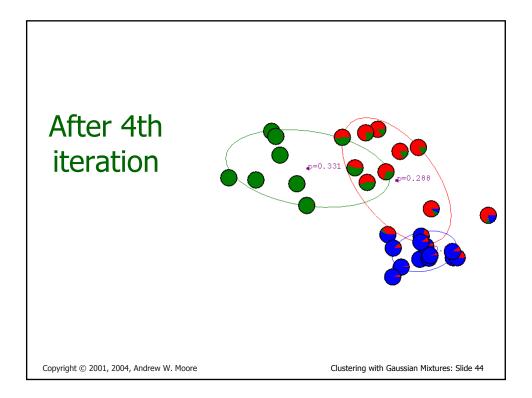


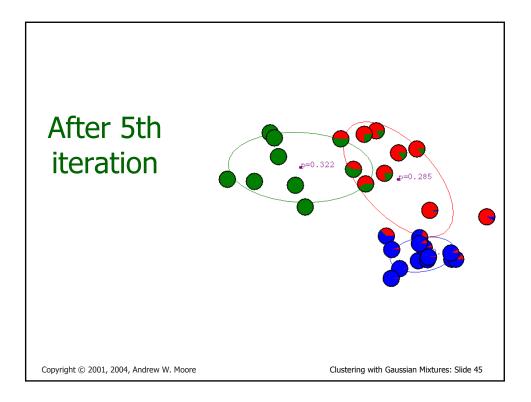


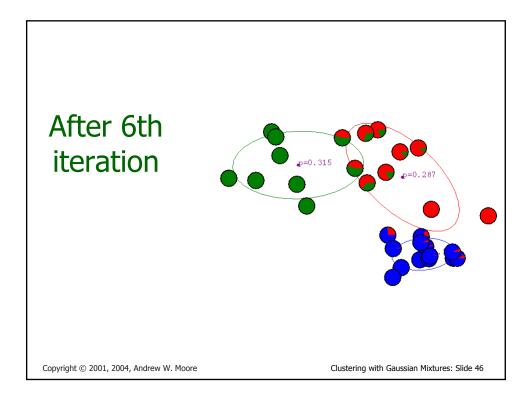


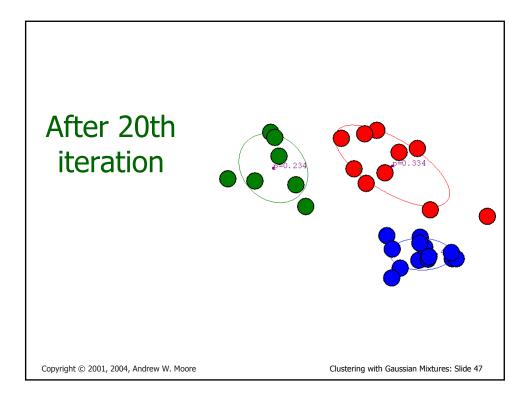


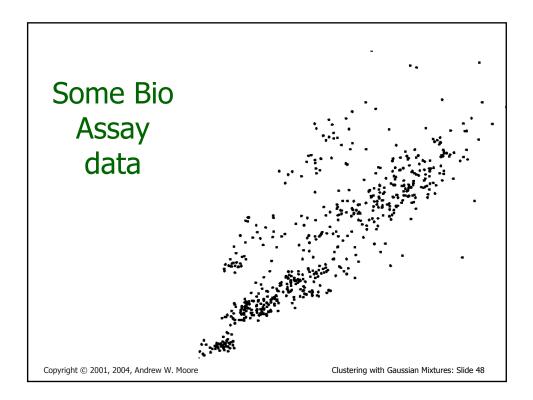


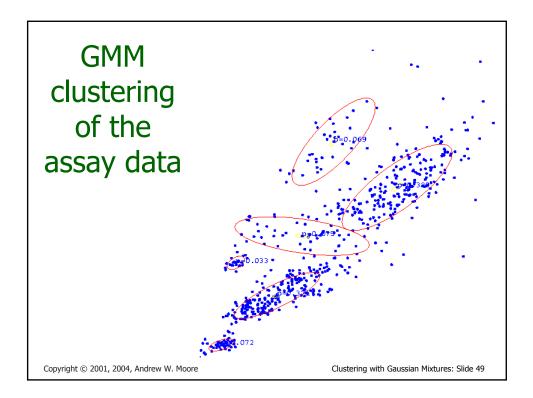


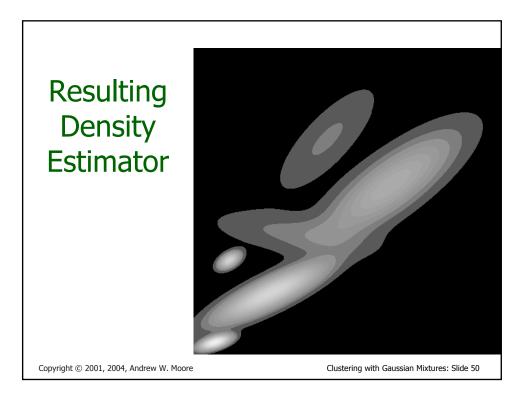


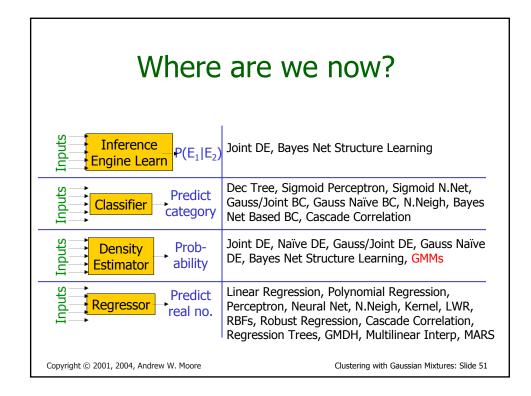


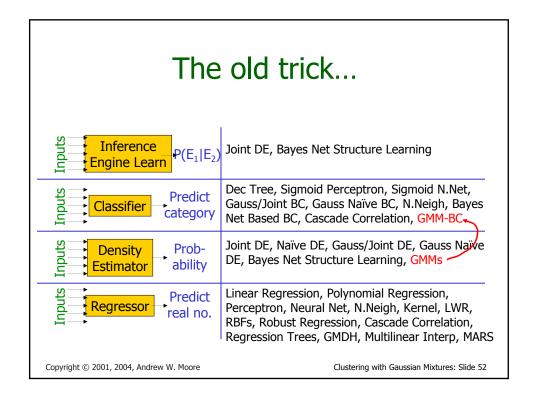


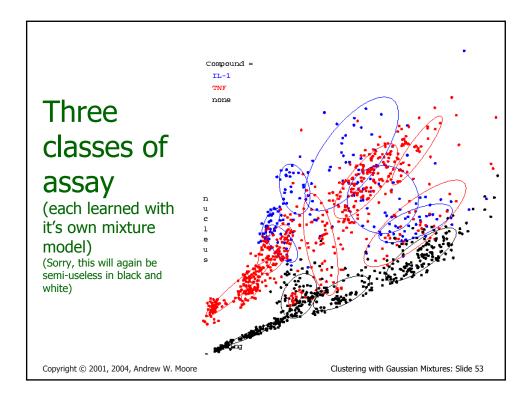


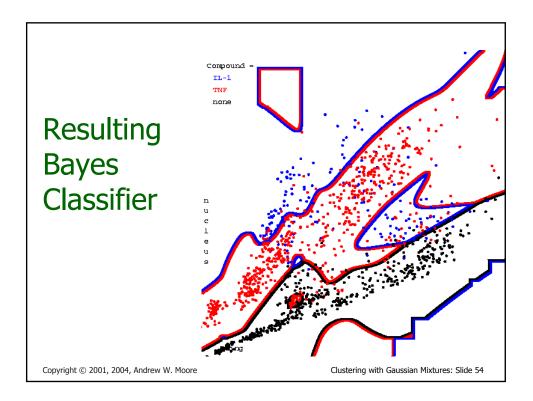


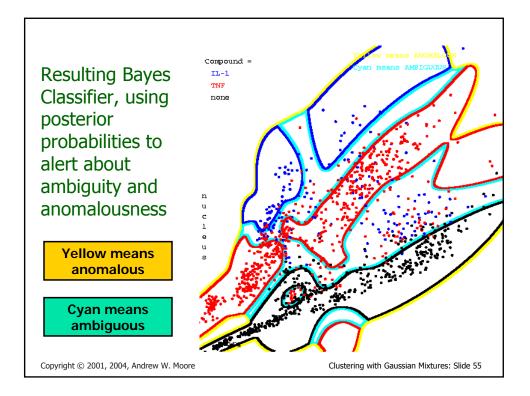


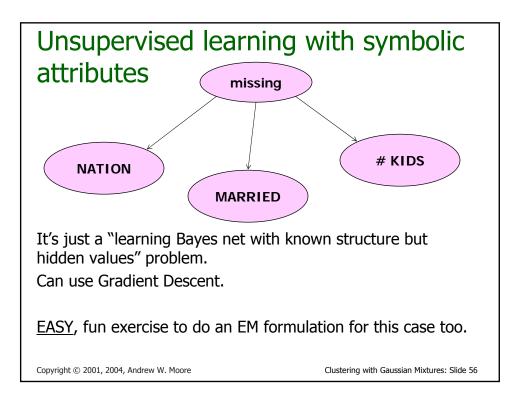


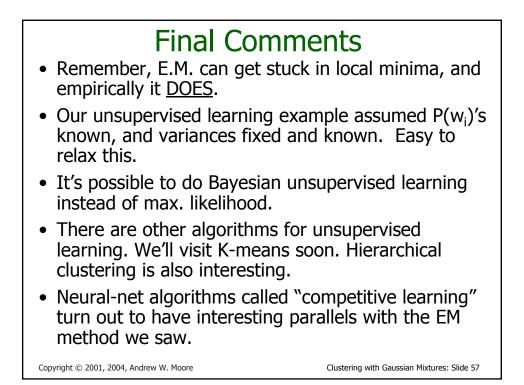


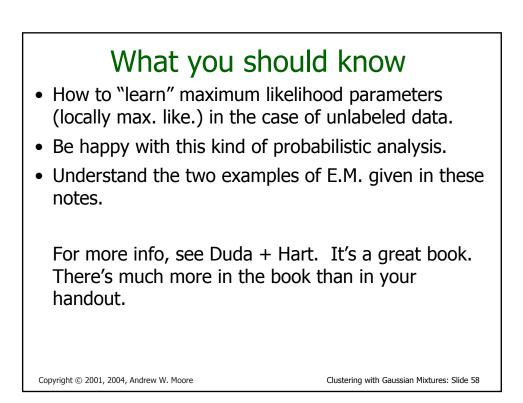












Other unsupervised learning methods

- K-means (see next lecture)
- Hierarchical clustering (e.g. Minimum spanning trees) (see next lecture)
- Principal Component Analysis
 simple, useful tool
- Non-linear PCA Neural Auto-Associators Locally weighted PCA Others...

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Clustering with Gaussian Mixtures: Slide 59