

# Concurrency

## EECS 4315

[www.cse.yorku.ca/course/4315/](http://www.cse.yorku.ca/course/4315/)

- Brian Goetz, Tim Peierls, Joshua Bloch, Joseph Bowbeer, David Holmes and Doug Lea. Java Concurrency in Practice. Addison-Wesley, 2006.
- Mary Campione, Kathy Walrath and Alison Huml. The Java Tutorial. Lesson: Threads: Doing Two or More Tasks At Once.
- James Gosling, Bill Joy, Guy L. Steele Jr. and Gilad Bracha. The Java Language Specification. Third edition

# Concurrency

Threads can exchange information by accessing and updating shared attributes.

## Question

One thread executes

```
v = 1;
```

```
v = v + 1;
```

and another thread executes

```
v = 0;
```

What is the final value of v?

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## Answer

0, 1 or 2.

## Question

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```

If the initial value of  $v$  is 0, then what is the final value of  $v$ ?

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```
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```

If the initial value of  $v$  is 0, then what is the final value of  $v$ ?

## Answer

1 or 2.

## Question

How can the final value of  $v$  be 1?

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The assignment  $v = v + 1$  is not **atomic**.



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0: `getstatic`

3: `iconst_1`

4: `iadd`

5: `putstatic`

## Question

One thread executes

```
v = 0;
```

and another thread executes

```
v = Long.MAX_VALUE;
```

How many different final values can v have?

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One thread executes

```
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and another thread executes

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How many different final values can v have?

## Answer

4.

## Question

How can  $v$  have 4 different final values?

## Question

How can `v` have 4 different final values?

## Answer

The assignments `v = 0` and `v = Long.MAX_VALUE` may not be **atomic**.

# Thread Creation

In Java, threads are created dynamically:

```
// create and initialize Thread object
Thread thread = new Thread();
// execute run method of Thread object concurrently
thread.start();
```

The class **Thread** is part of package **java.lang** (and, hence, does not need to be imported). Its API can be found at the URL <https://docs.oracle.com/javase/8/docs/api/java/lang/Thread.html>.

- `public Thread(String name)`  
Initializes a new Thread object with the specified name as its name.
- `public void start()`  
Causes this thread to begin execution; the Java Virtual Machine calls the run method of this thread.
- `public void run()`  
This method does nothing and returns.

## Question

Develop a Java class called `Printer` that is a `Thread` and prints its name 1000 times.



# Two Concurrent Printers

## Question

Develop an app that creates two `Printers` with names 1 and 2 and run them concurrently.

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## Question

What is the output of the app?

## Answer

A sequence of 1000 1's and 2's (arbitrarily interleaved). This example shows that concurrency gives rise to nondeterminism.

# Two Concurrent Printers

## Question

What happens if we replace start with run in the app?

# Two Concurrent Printers

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What happens if we replace start with run in the app?

## Answer

Let's try it.

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## Answer

Let's try it.

## Answer

The output is a sequence of 1000 1's followed by 1000 2's.

# Java only Supports Single Inheritance

The following is **not** allowed in Java.

```
public class Printer extends Applet, Thread
```

# Thread Creation

```
// create and initialize Runnable object
Runnable runnable = new ... ();
// create and initialize Thread object
Thread thread = new Thread(runnable);
// execute run method of Runnable object concurrently
thread.start ();
```

The interface `Runnable` is part of package `java.lang` (and, hence, does not need to be imported). Its API can be found at the URL <https://docs.oracle.com/javase/8/docs/api/java/lang/Runnable.html>.



# Runnable is an Interface

In Java, you cannot create instances of an interface.

```
public class Printer implements Runnable
{
    ...
}
```

The assignment

```
Runnable printer = new Printer();
```

is valid since the class **Printer** implements the interface **Runnable**.

## Question

Develop a Java class called `Printer` that implements `Runnable` and prints the thread's name 1000 times.

# How Many Different Executions?

## Question

One thread prints 1 one. Another thread prints 1 two. How many different executions are there?

# How Many Different Executions?

## Question

One thread prints 1 one. Another thread prints 1 two. How many different executions are there?

## Answer

2.

# How Many Different Executions?

## Question

One thread prints 2 ones. Another thread prints 2 twos. How many different executions are there?

# How Many Different Executions?

## Question

One thread prints 2 ones. Another thread prints 2 twos. How many different executions are there?

## Answer

6.

# How Many Different Executions?

## Question

One thread prints 3 ones. Another thread prints 3 twos. How many different executions are there?

# How Many Different Executions?

## Question

One thread prints 3 ones. Another thread prints 3 twos. How many different executions are there?

## Answer

20.



# How Many Different Executions?

## Question

One thread prints 1000 ones. Another thread prints 1000 twos.  
How many different executions are there?

# How Many Different Executions?

## Question

One thread prints 1000 ones. Another thread prints 1000 twos. How many different executions are there?

## Answer

204815162698948971433516250298082504439642488798139  
703382038263767174818620208375582893299418261020620  
146476631999802369241548179800452479201804754976926  
157856301289663432064714851152395251651227768588611  
539546256147907378668464154444533617613770073855673  
814589630071306510455959514479888746206368718514551  
828551173166276253663773084682932255389049743859481  
431755030783796444370810085163724827462791417016619  
883764840843541430817785947037746565188475514680749  
694674923803033101818723298009668567458560252549910  
118113525353465888794196665367490451130611009631190  
6270342502293155911108976733963991149120.

# How Many Different Executions?

## Question

One thread prints 1000 ones. Another thread prints 1000 twos. How many different executions are there?

## Answer

$$\binom{2000}{1000} = \frac{2000!}{1000!1000!}$$

# How Many Different Executions?

## Question

One thread executes  $n$  instructions. Another thread executes  $n$  instructions. How many different executions are there?

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## Answer

At most  $\binom{2n}{n}$ .

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## Question

Can there be fewer?

# How Many Different Executions?

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## Answer

At most  $\binom{2n}{n}$ .

## Question

Can there be fewer?

## Answer

Yes. For example, if each instruction is  $x = 1$  then there is only one execution.

# How Many Different Executions?

## Question

There are  $k$  threads. Each thread executes  $n$  instructions. How many different executions are there?



# How Many Different Executions?

Answer

$$\binom{kn}{n} \binom{(k-1)n}{n} \cdots \binom{2n}{n}$$

# How Many Different Executions?

Answer

$$\binom{kn}{n} \binom{(k-1)n}{n} \cdots \binom{2n}{n}$$
$$= \frac{(kn)!}{n!((k-1)n)!} \frac{((k-1)n)!}{n!((k-2)n)!} \cdots \frac{(2n)!}{n!n!}$$

# How Many Different Executions?

## Answer

$$\begin{aligned} & \binom{kn}{n} \binom{(k-1)n}{n} \cdots \binom{2n}{n} \\ &= \frac{(kn)!}{n!((k-1)n)!} \frac{((k-1)n)!}{n!((k-2)n)!} \cdots \frac{(2n)!}{n!n!} \\ &= \frac{(kn)!}{(n!)^k} \end{aligned}$$

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## Answer

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# How Many Different Executions?

## Answer

$$\begin{aligned} & \binom{kn}{n} \binom{(k-1)n}{n} \cdots \binom{2n}{n} \\ &= \frac{(kn)!}{n!((k-1)n)!} \frac{((k-1)n)!}{n!((k-2)n)!} \cdots \frac{(2n)!}{n!n!} \\ &= \frac{(kn)!}{(n!)^k} \\ &= \frac{kn((kn-1)\cdots(kn-n+1)) \cdots \frac{2n(2n-1)\cdots(n+1)}{n!}}{n!} \\ &\geq \left( \frac{2n(2n-1)\cdots(n+1)}{n!} \right)^k \end{aligned}$$

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$$\begin{aligned} & \binom{kn}{n} \binom{(k-1)n}{n} \cdots \binom{2n}{n} \\ &= \frac{(kn)!}{n!((k-1)n)!} \frac{((k-1)n)!}{n!((k-2)n)!} \cdots \frac{(2n)!}{n!n!} \\ &= \frac{(kn)!}{(n!)^k} \\ &= \frac{kn((kn-1)\cdots(kn-n+1)) \cdots \frac{2n(2n-1)\cdots(n+1)}{n!}}{n!} \\ &\geq \left( \frac{2n(2n-1)\cdots(n+1)}{n!} \right)^k \\ &= \left( \frac{2n(2n-1)\cdots(n+1)}{n(n-1)\cdots 1} \right)^k \end{aligned}$$

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## Answer

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# How Many Different Executions?

## Question

There are  $k$  threads. Each thread executes  $n$  instructions. How many different executions are there?

## Answer

In the worst case, more than  $n^k$ .

## Conclusion

The number of different executions may grow exponential in the number of threads.



```
public static void main(String[] args)
{
    Printer one = new Printer("1");
    Printer two = new Printer("2");
    one.start();
    two.start();
}
```

## Question

Draw the state-transition diagram.

# Executions

