

EECS 3221.3  
**Operating System Fundamentals**

**No.9**

## **Memory Management (2)**

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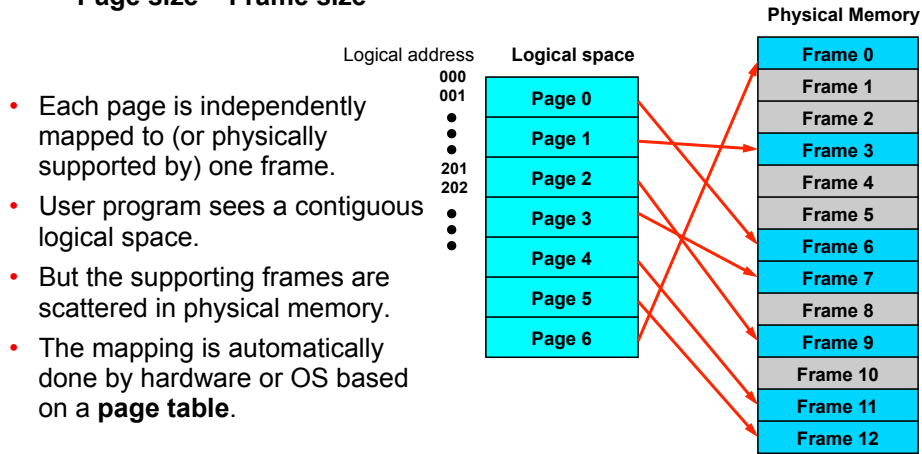
### **Memory Management Approaches**

- **Contiguous Memory Allocation**
- **Paging**
- **Segmentation**
- **Segmentation with paging**

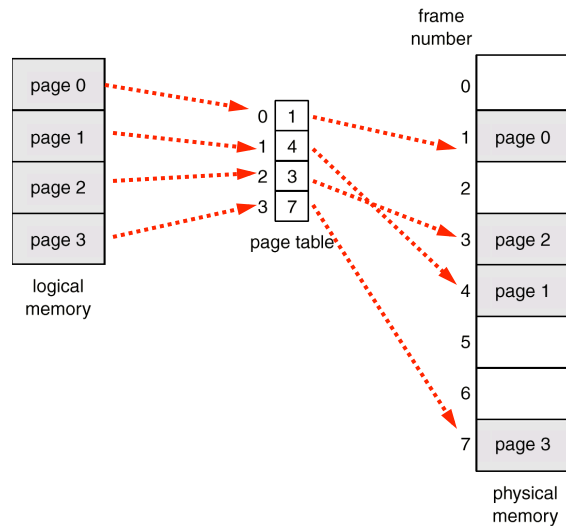
Contiguous Memory Allocation suffers serious external fragmentation

## Paging(1)

- Logical space is contiguous and consists of pages
- Physical space is broken into frames
- Page size = Frame size

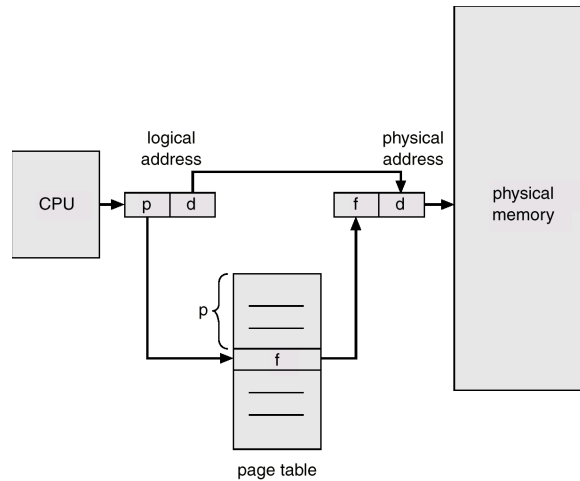


## Paging Example(1)



## Address Translation Architecture

- Convert logical address into page # and offset :  
Logical address ( $X$ ) = page number ( $p$ ) + page offset ( $d$ ).
- Assume page size  $k$ :  
 $p = X/k$  (quotient).  
 $d = X \% k$  (remainder).
- $p$  is used to index page table to find frame number or base physical address of this page.
- $d$  is the offset in the mapped frame.
- The physical address  $Y$ :  
 $Y = f * k + d$   
( $f$  is frame number).



## Translation of logical address (for binary address)

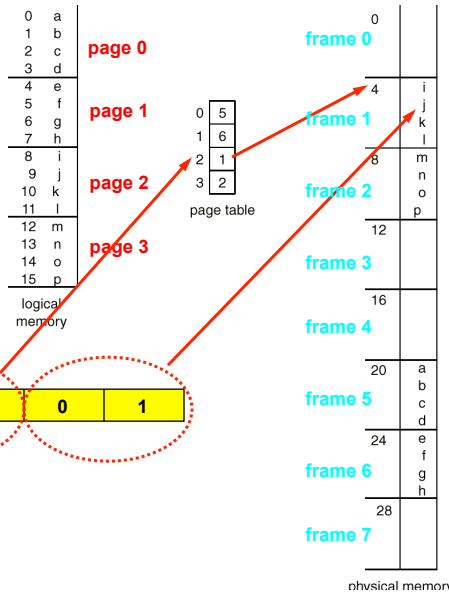
- Page size (frame size) is typical a power of 2. (4k – 16M).
- Logical address is a concatenated bit stream of page number and page offset.
- An example: 1) logical space is  $2^{m-n}$ : logical address is  $m$  bits.  
2) page size is  $2^n$ : page offset is  $n$  bits.  
3) a logical space needs at most  $2^{m-n}$  pages:  
page table contains at most  $2^{m-n}$  elements  
page number needs  $(m-n)$  bits to index page table



**Given a binary logical address, the last  $n$  bits is page offset and the first  $m-n$  bits is page number.**

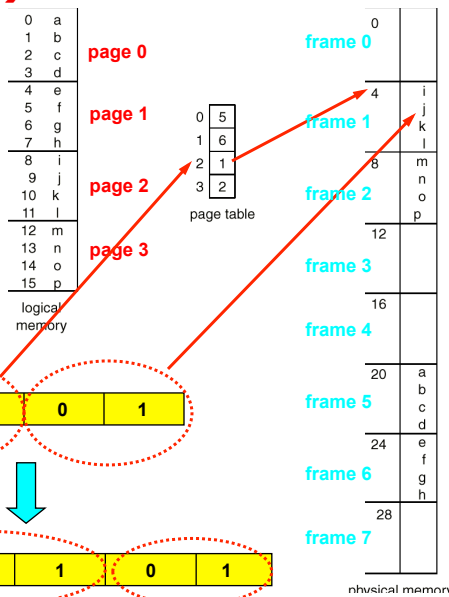
## Paging Example (2)

- Physical memory: 32-byte ( $2^{**5}$ ).
- Logical memory: 16-byte ( $2^{**4}$ ).
- Page size: 4-byte ( $2^{**2}$ ).
- Logical memory needs up to 4 pages: 4 entries in page table.
- $m=4, n=2$ .



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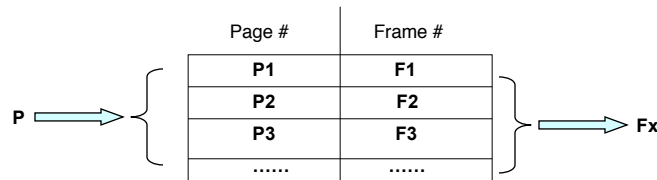


## Paging Hardware

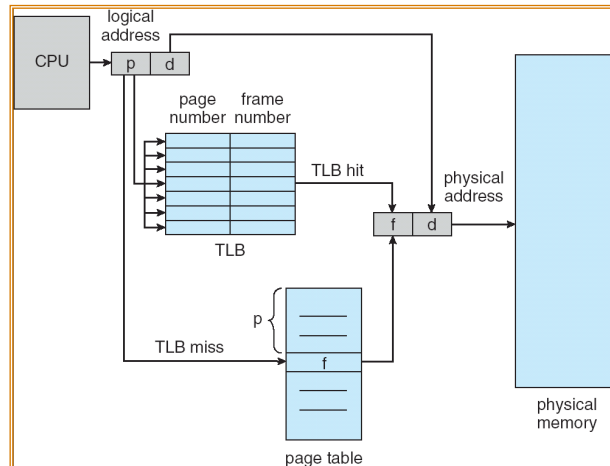
- OS maintains a page table for every process.
- All page tables are kept in physical memory.
- The currently active page table is page table of the currently running process.
- For small active page-table (<256 entries): using registers
- For large page-table: using two indexing registers
  - *page-table base register* (PTBR) points to the active page table.
  - *page-table length register* (PTLR) indicates size of the active page table.
  - In this scheme every data/instruction access requires two memory accesses. One for the page table and one for the data/instruction.

## Paging Hardware: TLB

- **Caching:** using of a special fast-lookup hardware cache called *associative registers* or **translation look-aside buffers (TLBs)**
    - Associative registers (expensive) – parallel search
    - speedup translation from page # → frame # :  
Assume page number is P:
      - If P is in associative register, get frame # out. (hit)
      - Otherwise get frame # from page table in memory (miss)
- Save to TLB for next reference, replace an old one if full



## Paging Hardware with TLB: MMU in Paging



Need to flush TLB's in context switch

## Effective Access Time of paging after TLB

- Assume memory cycle time is **a** time unit.
- One TLB Lookup = **b** time unit.
- Hit ratio – percentage of times that a page number is found in the associative registers; ration related to number of associative registers.
- Hit ratio =  $\lambda$ .
- Effective Access Time (EAT):

$$\begin{aligned} \text{EAT} &= (\mathbf{a} + \mathbf{b}) \lambda + (2\mathbf{a} + \mathbf{b})(1 - \lambda) \\ &= (2 - \lambda)\mathbf{a} + \mathbf{b} \end{aligned}$$

**Example:** **a** = 100 nanoseconds, **b** = 20 nanosecond.

If  $\lambda = 0.80$ , EAT = 140 nanoseconds (40% slower).

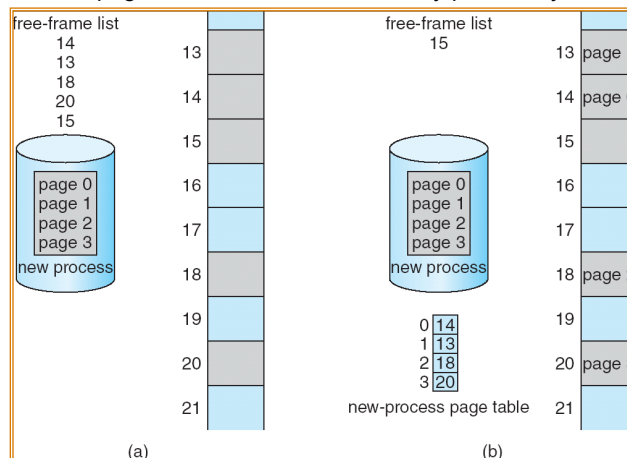
If  $\lambda = 0.98$ , EAT = 122 nanoseconds (22% slower).

## Paging (2)

- No external fragmentation in paging.
- Internal fragmentation: process size does not happen to fall on page boundaries.
  - Average one-half page per process.
- How to choose page size:
  - Smaller page size:
    - less internal fragmentation.
    - large page table (more overhead).
  - Typical 4K—8KB
- If each page table entry is 4 bytes long, it can point to one of  $2^{32}$  frames
  - Maximal physical address:  $\text{frame size} * (2^{32})$   
*(from this we can deduce the bit number in physical address)*

## Paging (3): Memory Allocation

- OS keeps track of all free frames.
- To run a program of size  $n$  pages, OS needs to find  $n$  free frames and load program.
- OS sets up a page table to translate logical to physical addresses.
- Each process has its page table and saved in memory pointed by its PCB.



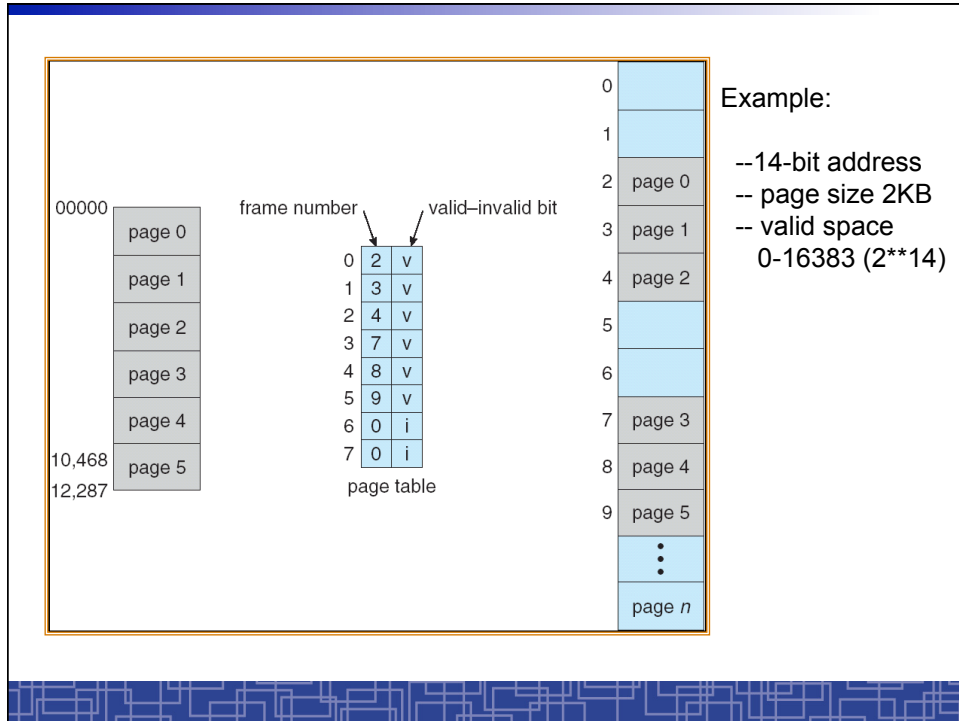
## OS data structure for Paging

- OS maintain a page table for each process in memory, pointed by the PCB of the process.
  - Used to translate logical address in a process' address space into physical address.
  - Example: one process make an I/O system call and provide an address as parameter (logical address in user space). OS must use its page-table to produce the correct physical address.
- OS maintains a global **frame table**:
  - One entry for each physical frame in memory.
  - To indicate the frame is free or allocated, if allocated, to which page of which process.
- In context switch, the saved page-table is loaded by the CPU dispatcher to MMU for every memory reference and flush TLB. (This increases context switch time)

## Memory Protection in paging

- How is memory protected from different processes?
  - In paging, other process memory space is protected automatically.
- Memory protection can be implemented by associating protection bits with each frame in page table
  - One bit for read-only or read-write
  - One bit for execute-only
  - One *Valid-invalid* bit
    - “valid” indicates that the associated page is in the process' logical address space, and is thus a legal page.
    - “invalid” indicates that the page is not in the process' logical address space.
    - Use page-table length register (PTLR): to indicate the size of page table
    - *Valid-invalid* bit is mainly used for virtual memory
- In every memory reference, the protection bits are checked. Any invalid access will cause a trap into OS.

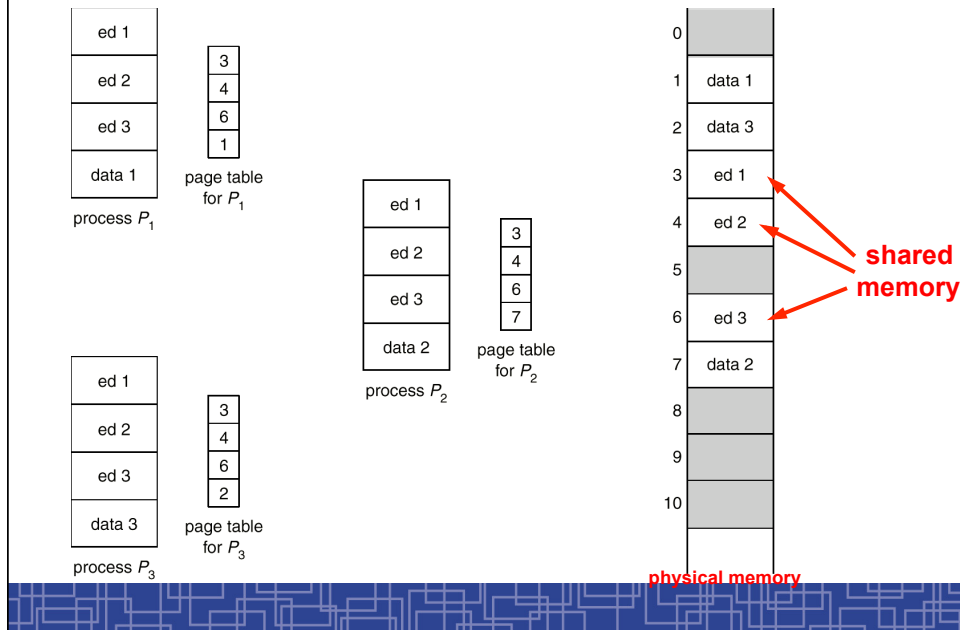




## Sharing Memory in Paging

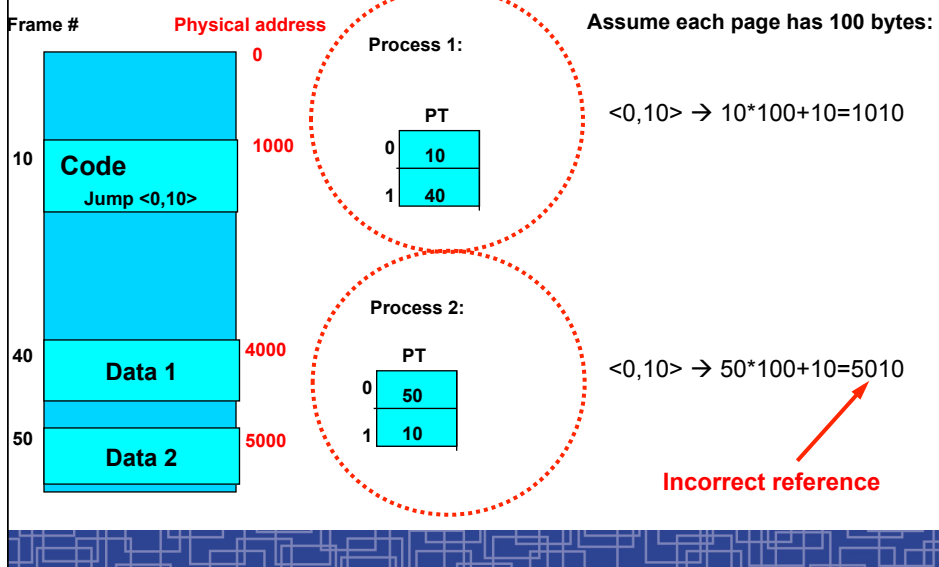
- Different pages of several processes can be mapped to the same frame to let them share memory.
- Shared-memory for inter-process communication.
- Private code and data:
  - Each process keeps a separate copy of the code and data.
  - The pages for the private code and data can appear anywhere in the logical address space.
- Shared code:
  - One copy of read-only (reentrant) code shared among processes (i.e., text editors, compilers, window systems).
  - Shared code must appear in same location in the logical address space of all processes (i.e. same locations in the page tables).

## Shared Pages Example



## Shared Pages

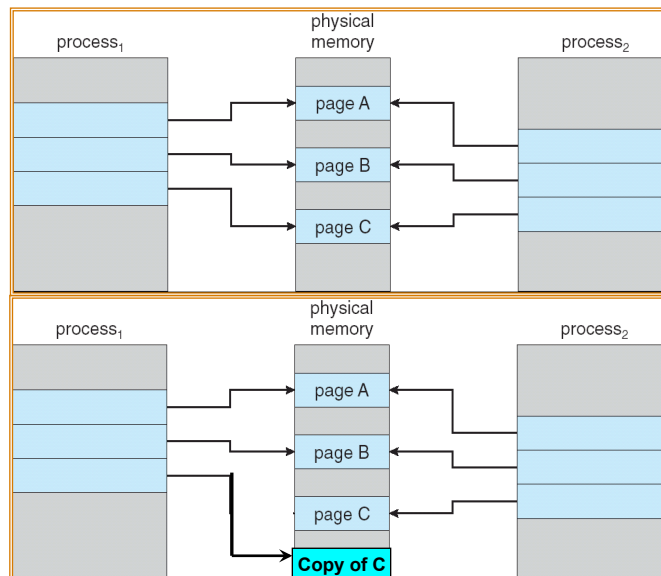
- How to share pages with code which has a direct address reference?



## Copy-on-Write

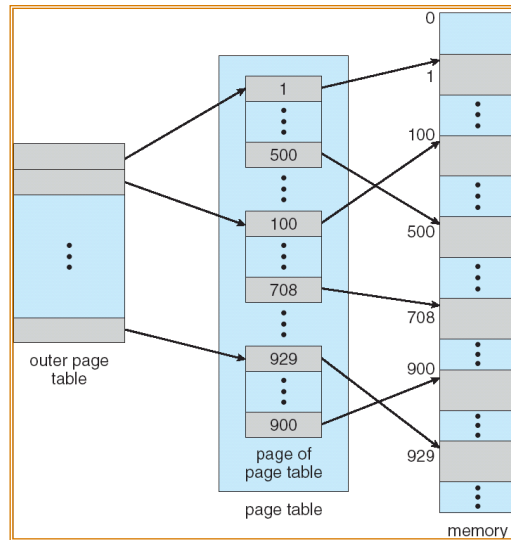
- For quick process creation: *fork()*
- Traditionally, *fork()* copies parent's address space for the child.
- **Copy-on-Write**: without copying, the parent and child process initially share the same pages, and these pages are marked as copy-on-write.
  - If either process needs to write to a shared page, a copy of the shared page is created and stop sharing this page.
- Advantages of copy-on-write:
  - Quick process creation (no copying, just modify page table for page sharing)
  - Eventually, only modified pages are copied. All non-modified pages are still shared by the parent and child processes.
    - Better memory utilization

## Copy-on-Write



## Hierarchical Paging (multilevel paging)

- In modern computer, we require a large logical-address space, which results in some huge page table.
- No contiguous memory space for the large page table.
- Hierarchical paging: using paging technique to divide the large page table into smaller pieces

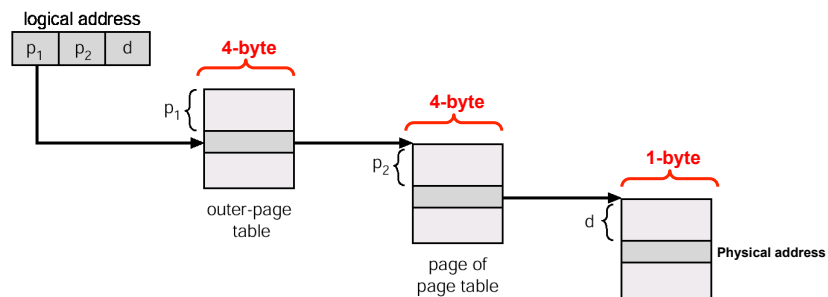


## Address-Translation in two-level paging

- Logical address 32-bit, page size 4K, maximal physical address  $2^{32}$  frames
- A logical address is divided into 20 bits page number and 12 bits page offset.
- Since page-table is paged, the logical address is as follows:

page number		page offset
$p_1$	$p_2$	$d$
10	10	12

where  $p_1$  is an index into the outer page table, and  $p_2$  is the displacement within the page of the outer page table.



## Multilevel Paging and Performance

- 64-bit logical address may require 6-level paging.
- Since each level is stored as a separate table in memory, converting a logical address to a physical one may take seven memory accesses.
- TLB-based caching permits performance to remain reasonable.
- Cache hit rate of 98 percent yields:

$$\begin{aligned}\text{effective access time} &= 0.98 \times 120 + 0.02 \times 720 \\ &= 132 \text{ nanoseconds.}\end{aligned}$$

which is only 32 percent slowdown in memory access time.

- But the overhead is too high to maintain many page-tables
- In 64-bit Linux, it uses 4-level paging to page 48-bit address.