

# EECS 4315 3.0 Mission Critical Systems

Solution of final exam

15:45–17:00 on April 10, 2019

## 1 (3 marks)

(a) What is a *native method*?

**Answer:** A method that is implemented in a language other than Java but that is invoked from a Java app.

**Marking scheme:** 1 mark for mentioning something related to “implemented in another language.”

(b) Explain the difference between a *peer* class and a *native peer* class.

**Answer:** A peer class models the behaviour of a native method as a method in Java code and this method (instead of the native method) is *model checked* by JPF’s virtual machine. A native peer class contains a method corresponding to the native method (that may call native code) and this method is *executed* by the host virtual machine.

**Marking scheme:** 1 mark for mentioning that the method in the peer class is model checked and 1 mark for mentioning that the native peer class is executed.

## 2 (2 marks)

Consider the following class that tests a JPF listener.

```
1 import gov.nasa.jpf.util.test.TestJPF;
2 import org.junit.Test;
3
4 public class SampleTest extends TestJPF {
5     /**
6      * Tests a listener.
7      */
8     @Test
9     public void test() {
10         if (!TestJPF.isJPFRun()) {
11             ...
12         }
13         if (this.verifyNoPropertyViolation(...)) {
14             ...
```

```
15     } else {
16         ...
17     }
18 }
19
20 ...
21 }
```

(a) Of the lines 10–17 of code, which lines are executed by the host virtual machine?

**Answer:** Lines 10–13 and 16.

**Marking scheme:** 0.5 mark for line 10–13 and 0.5 mark for lines 16.

(b) Of the lines 10–17 of code, which lines are executed by JPF's virtual machine?

**Answer:** Lines 10, and 13–14.

**Marking scheme:** 0.5 mark for line 10 and 0.5 mark for lines 13 and 14.

### 3 (3 marks)

Two threads share the attribute `a`. Initially, the value of `a` is 0. The first thread executes the following code.

```
1 a = a + 2;
```

The second thread executes the following code.

```
1 a = a - 2;
```

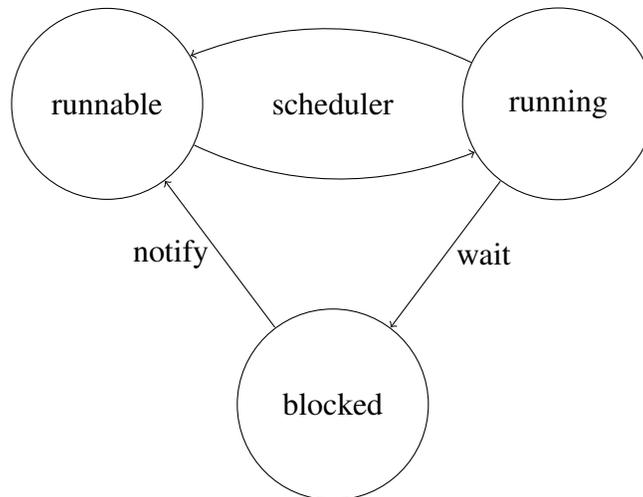
What are the possible final values of `a`? Explain your answer.

**Answer:** The statement `a = a + 2` consists of reading the value of `a`, incrementing that value by 2, and writing the new value to `a`. The statement `a = a - 2` consists of multiple bytecode instructions as well. Consider all interleavings, the final value of `a` can either, 0, 2, or -2.

**Marking scheme:** 1 marks for the observation that both statements consist of multiple bytecode instructions. 1 mark for mentioning that there are different interleavings. 1 mark for the correct final values.

## 4 (2 marks)

A thread can be in different states, as shown in the following diagram.



Consider the solution to the readers-writers problem given on pages 11–12. Using the diagram above, explain why we use `while` instead of `if` in line 12 of the `Database` class.

**Answer:** When line 14 is executed, the state of the `Reader` thread executing the code changes from `running` to `blocked`. When that `Reader` thread gets notified, its state changes from `blocked` to `runnable`. At that point, the `writing` attribute is `false`. However, before its state becomes `running`, `writing` attribute may be set to `true`. Hence, once its state becomes `running`, we should check again the value of the `writing` attribute.

**Marking scheme:** 0.5 mark for explaining the change from `running` to `blocked`. 0.5 mark for explaining the change from `blocked` to `runnable`. 1 mark for observing that the value of `writing` may change before the change from `runnable` to `running`.

## 5 (1 marks)

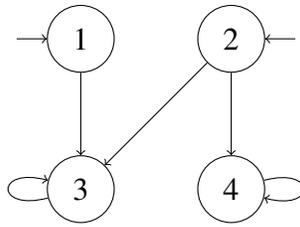
Consider the solution to the readers-writers problem given on pages 11–12. Can `notifyAll` on line 43 of the `Database` class be replaced with `notify`. Explain your answer.

**Answer:** No. It may cause a deadlock.

**Marking scheme:** 1 mark for for mentioning deadlock.

## 6 (5 marks)

Consider the following transition system



and the following labelling function

$$\begin{aligned}\ell(1) &= \{a\} \\ \ell(2) &= \{a, b\} \\ \ell(3) &= \{b, c\} \\ \ell(4) &= \{c\}\end{aligned}$$

Note that states 1 and 2 are both initial. For each of the following LTL formulas, determine if that formula holds for the above transition system. A simple yes or no suffices.

- (a)  $a$
- (b)  $b$
- (c)  $a \wedge \neg b$
- (d)  $\bigcirc(b \vee c)$
- (e)  $\bigcirc \bigcirc \neg a$
- (f)  $\diamond b$
- (g)  $\square(a \vee c)$
- (h)  $a \text{ U } b$
- (i)  $b \text{ U } a$
- (j)  $a \text{ U } ((b \vee c) \text{ U } c)$

**Answer:**

- (a) Yes.
- (b) No.
- (c) No.
- (d) Yes.
- (e) Yes.

(f) Yes.

(g) Yes.

(h) Yes.

(i) Yes.

(j) Yes.

For each of the following CTL formulas, determine if that formula holds for the above transition system. A simple yes or no suffices.

(k)  $\exists \diamond c$

(l)  $\forall \diamond c$

(m)  $\exists \diamond b$

(n)  $\forall \diamond b$

(o)  $\exists \square (\neg a \vee \neg b)$

(p)  $\forall \square (\neg a \vee \neg b)$

(q)  $\exists a \text{ U } b$

(r)  $\forall a \text{ U } b$

(s)  $\exists a \text{ U } (\exists b \text{ U } c)$

(t)  $\forall a \text{ U } (\forall b \text{ U } c)$

**Answer:**

(k) Yes.

(l) Yes.

(m) Yes.

(n) Yes.

(o) No.

(p) No.

(q) Yes.

(r) Yes.

(s) Yes.

(t) Yes.

**Marking scheme:** 0.25 mark for each correct answer.

## 7 (3 marks)

- (a) Let  $a$  and  $b$  be atomic propositions. Express “ $b$  happens never after  $a$ ” in LTL.

**Answer:**  $\Box(a \Rightarrow \bigcirc\Box\neg b)$ .

**Marking scheme:** 0.5 mark for the initial  $\Box$ . 0.5 mark for the  $a \Rightarrow$ . 0.5 mark for  $\bigcirc\Box\neg b$ .

- (b) Let  $a$  be an atomic proposition. Express “If  $a$  ever happens, then it won’t keep happening forever” in CTL.

**Answer:**  $\forall\Box(a \Rightarrow \forall\Diamond\neg a)$ .

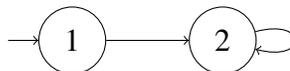
**Marking scheme:** 0.5 mark for the initial  $\forall\Box$ . 0.5 mark for the  $a \Rightarrow$ . 0.5 mark for  $\forall\Diamond\neg a$ .

## 8 (4 marks)

Let  $f$  and  $g$  be arbitrary LTL formulas. Which of the following equivalences hold? If the equivalence holds, give a proof. If the equivalence does not hold, provide a transition system (and a specific choice for  $f$  and  $g$ ) for which one of the two LTL formulas holds and the other LTL formula does not hold.

- (a)  $\bigcirc(f \cup g) \equiv (f \cup \bigcirc g) \vee g$

**Answer:** The formulas are not equivalent. For  $f$  and  $g$  we choose the atomic propositions  $a$  and  $b$ , respectively. We consider the following transition system.



and the following labelling function

$$\begin{aligned} \ell(1) &= \emptyset \\ \ell(2) &= \{b\} \end{aligned}$$

This transition system satisfies  $\bigcirc(a \cup b)$  since state 2 has label  $b$ . However, the transition system does not satisfy  $(a \cup \bigcirc b) \vee b$  since state 1 is neither labelled  $a$  nor  $b$ .

**Marking scheme:** 0.25 mark for choosing appropriate choices for  $f$  and  $g$ . 0.5 mark for an appropriate transition system. 0.25 mark for arguing why the transition satisfies the one property but not the other.

- (b)  $\bigcirc\Diamond f \equiv \Diamond\bigcirc f$

**Answer:** The formulas are equivalent. Let  $TS$  be an arbitrary transition system. Let  $p$  be a path starting in an initial state. Then

$$\begin{aligned}
& p \models \bigcirc \diamond f \\
& \text{iff } p[1..] \models \diamond f \\
& \text{iff } \exists i \geq 0 : p[1..][i..] \models f \\
& \text{iff } \exists i \geq 0 : p[(i+1)..] \models f \\
& \text{iff } \exists i \geq 0 : p[i..][1..] \models f \\
& \text{iff } \exists i \geq 0 : p[i..] \models \bigcirc f \\
& \text{iff } p \models \diamond \bigcirc f
\end{aligned}$$

**Marking scheme:** 0.25 mark for expanding the definition of  $\bigcirc$ . 0.25 mark for expanding the definition of  $\diamond$ . 0.5 mark for the remainder of the proof.

Let  $f$  and  $g$  be arbitrary CTL formulas. Which of the following equivalences hold? If the equivalence holds, give a proof. If the equivalence does not hold, provide a transition system (and a specific choice for  $f$  and  $g$ ) for which one of the two CTL formulas holds and the other CTL formula does not hold.

(c)  $\exists(f \cup g) \equiv g \vee (f \wedge \exists \bigcirc \exists(f \cup g))$

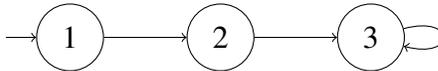
**Answer:** The formulas are equivalent. Let  $TS$  be an arbitrary transition system. Let  $s$  be an initial state. Then

$$\begin{aligned}
& s \models \exists(f \cup g) \\
& \text{iff } \exists p \in \text{Paths}(s) : p \models f \cup g \\
& \text{iff } \exists p \in \text{Paths}(s) : \exists i \geq 0 : p[i] \models g \wedge \forall 0 \leq j < i : p[j] \models f \\
& \text{iff } \exists p \in \text{Paths}(s) : p[0] \models g \vee (\exists i \geq 1 : p[i] \models g \wedge (p[0] \models f \wedge \forall 1 \leq j < i : p[j] \models f)) \\
& \text{iff } \exists p \in \text{Paths}(s) : p[0] \models g \vee (p[0] \models f \wedge (\exists i \geq 1 : p[i] \models g \wedge \forall 1 \leq j < i : p[j] \models f)) \\
& \text{iff } s \models g \vee (s \models f \wedge (\exists p \in \text{Paths}(s) : \exists i \geq 1 : p[i] \models g \wedge \forall 1 \leq j < i : p[j] \models f)) \\
& \text{iff } s \models g \vee (s \models f \wedge (\exists p \in \text{Paths}(s) : \exists i \geq 0 : p[i+1] \models g \wedge \forall 0 \leq j < i : p[j+1] \models f)) \\
& \text{iff } s \models g \vee (s \models f \wedge (\exists p \in \text{Paths}(s) : \exists i \geq 0 : p[1][i] \models g \wedge \forall 0 \leq j < i : p[1][j] \models f)) \\
& \text{iff } s \models g \vee (s \models f \wedge (\exists p \in \text{Paths}(s) : \exists q \in \text{Paths}(p[1]) : \exists i \geq 0 : q[i] \models g \wedge \forall 0 \leq j < i : q[j] \models f)) \\
& \text{iff } s \models g \vee (s \models f \wedge (\exists p \in \text{Paths}(s) : \exists q \in \text{Paths}(p[1]) : q \models f \cup g)) \\
& \text{iff } s \models g \vee (s \models f \wedge (\exists p \in \text{Paths}(s) : p[1] \models \exists(f \cup g))) \\
& \text{iff } s \models g \vee (s \models f \wedge (\exists p \in \text{Paths}(s) : p \models \bigcirc \exists(f \cup g))) \\
& \text{iff } s \models g \vee (s \models f \wedge s \models \exists \bigcirc \exists(f \cup g)) \\
& \text{iff } s \models g \vee (f \wedge \exists \bigcirc \exists(f \cup g))
\end{aligned}$$

**Marking scheme:** 0.25 mark for expanding the definition of  $\exists$ . 0.25 mark for expanding the definition of  $\cup$ . 0.25 mark for expanding the definition of  $\bigcirc$ . 0.25 mark for the remainder of the proof.

(d)  $\forall(f \cup g) \equiv f \wedge \forall \diamond g$

**Answer:** The formulas are not equivalent. For  $f$  and  $g$  we choose the atomic propositions  $a$  and  $b$ , respectively. We consider the following transition system.



and the following labelling function

$$\begin{aligned} \ell(1) &= \{a\} \\ \ell(2) &= \emptyset \\ \ell(3) &= \{b\} \end{aligned}$$

This transition system satisfies  $a \wedge \forall \diamond b$  since state 1 has label  $a$  and state 3 has label  $b$ . However, the transition system does not satisfy  $\forall(a \cup b)$  since state 2 is not labelled  $b$ .

**Marking scheme:** 0.25 mark for choosing appropriate choices for  $f$  and  $g$ . 0.5 mark for an appropriate transition system. 0.25 mark for arguing why the transition satisfies the one property but not the other.

## 9 (1 mark)

We extend the syntax of CTL with the operator  $\exists^!$ . Let  $g$  be a path formula. Then the state formula  $\exists^!g$  captures that there exists a *unique* path satisfying  $g$ . Formally,

$$s \models \exists^!g \text{ iff } \exists p \in Paths(s) : p \models g \wedge \forall q \in Paths(s) : q \neq p \Rightarrow q \not\models g$$

Recall that  $Sat(f) = \{s \in S \mid s \models f\}$ . Express  $Sat(\exists^! \bigcirc f)$  in terms of  $Sat(f)$ .

**Answer:**  $Sat(\exists^! \bigcirc f) = \{s \in S \mid |succ(s) \cap Sat(f)| = 1\}$ .

**Marking scheme:** 0.5 mark for considering successors. 0.5 mark for limiting to one element.

## 10 (2 marks)

Consider the following method.

```

1 public void example(int x, int y) {
2   if (x >= 0) {
3     if (y > x) {

```

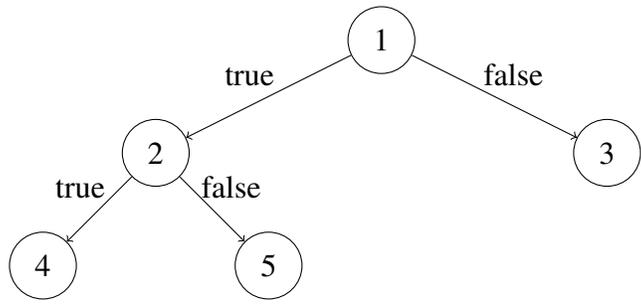
```

4     System.out.println("y is positive");
5 } else {
6     System.out.println("x is nonnegative");
7 }
8 } else {
9     System.out.println("x is nonnegative");
10 }
11 }

```

Assume that both  $x$  and  $y$  are symbolic. Draw the symbolic execution tree and for each node of the tree provide the corresponding path condition.

**Answer:** The symbolic execution tree looks like the following.



The corresponding path conditions are the following.

state	path condition
1	true
2	$x \geq 0$
3	$x < 0$
4	$x \geq 0 \wedge y > x$
5	$x \geq 0 \wedge \neg(y > x)$

**Marking scheme:** 1 mark for a tree of the right shape. 0.2 mark for each correct path condition.

## 11 (1 mark)

Give an estimate of the (yearly world-wide) cost of debugging.

**Answer:** US \$312 billion.

**Marking scheme:** 1 mark for something in the order of 100's of billions of US \$.

## 12 (1 bonus mark)



(a) From left to right (circle the correct answer):

- Dijkstra, Clarke, Emerson, Sifakis, Lamport, Pnueli
- Sifakis, Clarke, Pnueli, Dijkstra, Lamport, Emerson
- Lamport, Clarke, Emerson, Sifakis, Dijkstra, Pnueli
- Dijkstra, Clarke, Pnueli, Sifakis, Lamport, Emerson
- Lamport, Pnueli, Emerson, Sifakis, Dijkstra, Clarke

**Answer:** The last combination.

**Marking scheme:** 0.5 mark for the correct answer.

(b) Which award have they all won?

**Answer:** The Turing award.

**Marking scheme:** 0.5 for the correct answer.

## Reader class

```
1 public class Reader extends Thread {
2     private Database database;
3
4     public Reader(Database database) {
5         super();
6         this.database = database;
7     }
8
9     public void run() {
10        this.database.read();
11    }
12 }
```

## Writer class

```
1 public class Writer extends Thread {
2     private Database database;
3
4     public Writer(Database database) {
5         super();
6         this.database = database;
7     }
8
9     public void run() {
10        this.database.write();
11    }
12 }
```

## Database class

```
1 public class Database {
2     private boolean writing;
3     private int readers;
4
5     public Database() {
6         this.writing = false;
7         this.readers = 0;
8     }
9 }
```

```

8   }
9
10  public void read() {
11      synchronized(this) {
12          while (this.writing) {
13              try {
14                  this.wait();
15              } catch (InterruptedException e) {
16                  e.printStackTrace();
17              }
18          }
19      }
20      // read
21      synchronized(this) {
22          this.readers--;
23          if (this.readers == 0) {
24              this.notifyAll();
25          }
26      }
27  }
28
29  public void write() {
30      synchronized(this) {
31          while (this.writing || this.readers > 0) {
32              try {
33                  this.wait();
34              } catch (InterruptedException e) {
35                  e.printStackTrace();
36              }
37          }
38          this.writing = true;
39      }
40      // write
41      synchronized(this) {
42          this.writing = false;
43          this.notifyAll();
44      }
45  }
46  }

```

## Definitions

**Definition 1.** A transition system is a tuple  $\langle S, L, I, \rightarrow, \ell \rangle$  consisting of

- a set  $S$  of states,
- a set  $L$  of labels,
- a set  $I \subseteq S$  of initial states,
- a transition relation  $\rightarrow \subseteq S \times S$ , and
- a labelling function  $\ell : S \rightarrow 2^L$ .

**Definition 2.** Linear temporal logic (LTL) is defined by the grammar

$$f ::= a \mid f \wedge f \mid \neg f \mid \bigcirc f \mid f \text{ U } f$$

where  $a \in L$ .

We use the following syntactic sugar.

$$\begin{aligned} f \vee g &= \neg(\neg f \wedge \neg g) \\ \text{true} &= a \vee \neg a \\ \diamond f &= \text{true U } f && \text{(eventually } f\text{)} \\ \square f &= \neg \diamond \neg f && \text{(always } f\text{)} \end{aligned}$$

**Definition 3.**  $Paths(s)$  is the set of (execution) paths starting in state  $s$ . Let  $p \in Paths(s)$  and  $n \geq 0$ . Then  $p[n]$  is the  $(n + 1)^{\text{th}}$  state of the path  $p$  and  $p[n..]$  is the suffix of  $p$  starting with the  $(n + 1)^{\text{th}}$  state.

**Definition 4.** The relation  $\models$  is defined by

$$\begin{aligned} p \models a &\text{ iff } a \in \ell(p[0]) \\ p \models f \wedge g &\text{ iff } p \models f \text{ and } p \models g \\ p \models \neg f &\text{ iff } \text{not}(p \models f) \\ p \models \bigcirc f &\text{ iff } p[1..] \models f \\ p \models f \text{ U } g &\text{ iff } \exists i \geq 0 : p[i..] \models g \text{ and } \forall 0 \leq j < i : p[j..] \models f \end{aligned}$$

and

$$\langle S, L, I, \rightarrow, \ell \rangle \models f \text{ iff } \forall s \in I : \forall p \in Paths(s) : p \models f$$

**Definition 5.** Computation tree logic (CTL) is defined as follows. The state formulas are defined by

$$f ::= a \mid f \wedge f \mid \neg f \mid \exists g \mid \forall g$$

where  $a \in L$ . The path formulas are defined by

$$g ::= \bigcirc f \mid f \text{ U } f$$

**Definition 6.** The relation  $\models$  is defined by

$$\begin{aligned}
s \models a & \text{ iff } a \in \ell(s) \\
s \models f \wedge g & \text{ iff } s \models f \text{ and } s \models g \\
s \models \neg f & \text{ iff } \text{not}(s \models f) \\
s \models \exists g & \text{ iff } \exists p \in \text{Paths}(s) : p \models g \\
s \models \forall g & \text{ iff } \forall p \in \text{Paths}(s) : p \models g
\end{aligned}$$

and

$$\begin{aligned}
p \models \bigcirc f & \text{ iff } p[1] \models f \\
p \models f \text{ U } g & \text{ iff } \exists i \geq 0 : p[i] \models g \text{ and } \forall 0 \leq j < i : p[j] \models f
\end{aligned}$$

and

$$\langle S, L, I, \rightarrow, \ell \rangle \models f \text{ iff } \forall s \in I : s \models f$$

**Definition 7.** The satisfaction set  $Sat(f)$  is defined by

$$Sat(f) = \{ s \in S \mid s \models f \}.$$

**Definition 8.** LTL/CTL formulas  $f$  and  $g$  are equivalent, denoted  $f \equiv g$ , if  $\langle S, L, I, \rightarrow, \ell \rangle \models f$  iff  $\langle S, L, I, \rightarrow, \ell \rangle \models g$  for all transition systems  $\langle S, L, I, \rightarrow, \ell \rangle$ .